

Mathematics Curriculum Intent

Contents

Introduction	Page 3
Knowledge progression overview	Page 6
Foundation stage progression	Page 85
Arithmetic progression	Page 87
Vocabulary progression	Page 105

Introduction

Introduction

This document outlines the knowledge, skills and strategies that should be taught in Mathematics. It includes:

- A knowledge progression document to show key declarative knowledge children should learn throughout their education at Sheep Dip Lane Academy
- Foundation stage knowledge and skills yearly overview
- Arithmetic progression document
- Progression of vocabulary throughout each area of Mathematics

Other documents to support include:

- A calculation policy that outlines the procedural and conditional knowledge should learn throughout their education at Sheep Dip Lane Academy.
- Key Performance Indicators document which outlines the knowledge children should learn as matched to the National curriculum and Ready-To-Progress criteria
- Foundation stage yearly progression document

It is influenced by documents and research, including:

[National curriculum in England: mathematics programmes of study - GOV.UK \(www.gov.uk\)](https://www.gov.uk/government/publications/national-curriculum-in-england-mathematics-programmes-of-study)

[Teaching mathematics in primary schools - GOV.UK \(www.gov.uk\)](https://www.gov.uk/government/publications/teaching-mathematics-in-primary-schools)

[Research review series: mathematics - GOV.UK \(www.gov.uk\)](https://www.gov.uk/government/publications/research-review-series-mathematics)

Intent

Our intent in Mathematics is to provide a sound foundation for the development of mathematics skills throughout school with depth of learning through the use of White Rose Maths scheme of learning. This includes showing pupils how the different areas of Maths are interconnected, linked to real life and allow them to explore these links fully.

We recognise that a good mathematician needs fluency and automaticity in number work which is achieved through varied and frequent practice including - but not limited to – place value/number facts, times tables, calculation skill and the ability to apply these quickly and accurately

They also require the ability to apply these skills in reasoning and problem solving tasks which become increasingly progressive as children move through the academy. Children need the skills to break down these problems into small steps and persevere in seeking solutions.

At Sheep Dip Lane Academy, we recognise that all learners can achieve and we expect all learners to move through the curriculum at roughly the same pace. Children who grasp concepts quickly should be challenged in their learning, not through acceleration through content, but by broadening their experiences and deepening

their understanding with problem-solving tasks and application. Children who are yet to be fully confident with a concept must first secure their understanding through additional practise before moving on. They may require concrete models or same day intervention to build confidence with mathematical concepts.

Inclusion is at the heart of our Mathematics teaching and all children are given the support and opportunities they need to thrive in this subject and grant them the necessary skills and knowledge to be successful in later life.

Knowledge is taught through the three key knowledge strands:

Content categories	Type I	Type II
Declarative	Facts, formulae	Knowledge of <i>relationships</i> between facts/concepts
Procedural	Methods, algorithms	Knowledge of <i>relationships</i> between facts, steps and missing facts/principles & mechanisms
Conditional	Strategies (PK + DK)	Knowledge of <i>relationships</i> between known information, strategy choices and unknown information/reasoning

- Declarative knowledge is the knowing of this or that, e.g. knowing double 5 is 10 or 2 and 8 is a number bond that is equal to 10.
- Procedural knowledge is the knowing how to do things or the steps/strategies involved in how to do things, e.g. the steps involved in multiplying mixed numbers or the best ways to make a tuna sandwich.
- Conditional knowledge involves knowing the when and the why to apply the other two types of knowledge, e.g. readers skim newspapers to get the gist, but apply close reading to literature or difficult texts to develop deeper understandings.

At Sheep Dip Lane Academy, we adapt and enrich maths to ensure our high quality maths curriculum details the core facts, concepts, methods and strategies that give pupils the best chance of developing proficiency in the subject. To be able to develop this proficiency we nurture the different types of knowledge and aim to have mathematicians that are able to explain what they know, how they use it and when they use it.

Implementation

Our staff implement this through following the White Rose Maths curriculum, supported by carefully chosen additional resources including NCETM, Classroom Secrets, Reflex, Mathletics and Times Table Rockstars. Staff focus on quality first teaching and having the highest expectations of all learners. This is achieved through a

progression of understanding from concrete to pictorial and, finally, abstract thinking. Mathematical concepts are introduced using concrete apparatus (manipulatives) and pictures to allow all learners to fully grasp key learning points of those concepts. Only when children are confident using manipulatives and pictorial representations do they move to the abstract way of working. This allows for fluid differentiation in classes where all learners can work on the same learning but use different methods to complete it.

Children are assessed regularly in lessons to adapt support and at summative termly points throughout their time at Sheep Dip Lane. This allows for any gaps to be filled swiftly through same day interventions. This ensures that all children have their needs met for the mathematics curriculum.

Impact

The impact of our mathematics curriculum is that children understand the relevance and importance of what they are learning in relation to real world concepts. Children have a positive view of maths due to learning in an environment where maths is promoted as being an exciting and enjoyable subject in which they can investigate and ask questions; they know that it is reasonable to make mistakes because this can strengthen their learning through the journey to finding an answer. Children are confident to 'have a go' and choose the equipment they need to help them to learn along with the strategies they think are best suited to each problem. Our children have a good understanding of their strengths and targets for development in maths and what they need to do to improve. Our maths books evidence work of a high standard of which children clearly take pride; the components of the teaching sequences demonstrate good coverage of fluency, reasoning and problem solving. Our feedback and interventions support children to strive to be the best mathematicians they can be, ensuring a high proportion of children are on track or above.

Our pupils will have:

- Become fluent, competent and efficient mathematicians.
- The ability to recall facts and procedures, including the recollection of times tables.
- The ability to recognise relationships and make connections in maths.
- The ability to clearly explain their reasoning and justify their thought processes.
- The flexibility to move between different contexts and representations of maths.
- High aspirations, which will see them through to further study, work and a successful adult life.

Mathematics – Knowledge progression

Progression overview

	EYFS	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Number, Counting and Place Value	<p>Have a deep understanding of number to 10, including the composition of each number</p> <p>Subitise (recognise quantities without counting) up to 5</p> <p>Verbally count beyond 20, recognising the pattern of the counting system</p> <p>Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity</p> <p>Explore and represent patterns within numbers up to 10, including evens and odds</p>	<ul style="list-style-type: none"> count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number count, read and write numbers to 100 in numerals; count in multiples of twos, fives and tens given a number, identify one more and one less identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least read and write numbers from 1 to 20 in numerals and words. 	<ul style="list-style-type: none"> count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward recognise the place value of each digit in a two-digit number (tens, ones) identify, represent and estimate numbers using different representations, including the number line compare and order numbers from 0 up to 100; use and = signs read and write numbers to at least 100 in numerals and in words use place value and number facts to solve problems. 	<ul style="list-style-type: none"> count from 0 in multiples of 4, 8, 50 and 100; find 10 or 100 more or less than a given number recognise the place value of each digit in a three-digit number (hundreds, tens, ones) compare and order numbers up to 1000 identify, represent and estimate numbers using different representations read and write numbers up to 1000 in numerals and in words solve number problems and practical problems involving these ideas. 	<ul style="list-style-type: none"> count in multiples of 6, 7, 9, 25 and 1000 find 1000 more or less than a given number count backwards through zero to include negative numbers recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) order and compare numbers beyond 1000 identify, represent and estimate numbers using different representations round any number to the nearest 10, 100 or 1000 solve number and practical problems that involve all of the above and with increasingly large positive numbers read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value. 	<ul style="list-style-type: none"> read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero round any number up to 1 000 000 to the nearest 10, 100, 1000, 10 000 and 100 000 solve number problems and practical problems that involve all of the above read Roman numerals to 1000 (M) and recognise years written in Roman numerals. 	<ul style="list-style-type: none"> read, write, order and compare numbers up to 10 000 000 and determine the value of each digit round any whole number to a required degree of accuracy use negative numbers in context, and calculate intervals across zero solve number and practical problems that involve all of the above.
Addition and Subtraction	<p>Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10, including double facts.</p>	<ul style="list-style-type: none"> read, write and interpret mathematical statements involving addition (+), subtraction (−) and equals (=) signs represent and use number bonds and related subtraction facts within 20 add and subtract one-digit and two-digit numbers to 20, including zero solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$. 	<p>Solve problems with addition and subtraction:</p> <ul style="list-style-type: none"> using concrete objects and pictorial representations, including those involving numbers, quantities and measures applying their increasing knowledge of mental and written methods recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 <p>Add and subtract numbers using concrete objects, pictorial representations, and mentally, including:</p>	<p>Add and subtract numbers mentally, including:</p> <ul style="list-style-type: none"> a three-digit number and ones a three-digit number and tens a three-digit number and hundreds <p>add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction</p> <ul style="list-style-type: none"> estimate the answer to a calculation and use inverse operations to check answers solve problems, including missing number problems, using number facts, place 	<ul style="list-style-type: none"> add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate estimate and use inverse operations to check answers to a calculation solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why. 	<ul style="list-style-type: none"> add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) add and subtract numbers mentally with increasingly large numbers use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy solve addition and subtraction multi-step problems in contexts, deciding which operations 	<ul style="list-style-type: none"> perform mental calculations, including with mixed operations and large numbers use their knowledge of the order of operations to carry out calculations involving the four operations solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why solve problems involving addition, subtraction, multiplication and division

			<ul style="list-style-type: none"> ♣ a two-digit number and ones ♣ a two-digit number and tens ♣ two two-digit numbers ♣ adding three one-digit numbers ♣ show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot ♣ recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. 	value, and more complex addition and subtraction.		and methods to use and why.	<ul style="list-style-type: none"> ♣ use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.
Multiplication and Division	Understand double facts and how quantities can be distributed equally.	<ul style="list-style-type: none"> ♣ solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. 	<ul style="list-style-type: none"> ♣ recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers ♣ calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (\times), division (\div) and equals ($=$) signs ♣ show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot ♣ solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts. 	<ul style="list-style-type: none"> ♣ recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables ♣ write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods ♣ solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects. 	<ul style="list-style-type: none"> ♣ recall multiplication and division facts for multiplication tables up to 12×12 ♣ use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers ♣ recognise and use factor pairs and commutativity in mental calculations ♣ multiply two-digit and three-digit numbers by a one-digit number using formal written layout ♣ solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects. 	<ul style="list-style-type: none"> ♣ identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers ♣ know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers ♣ establish whether a number up to 100 is prime and recall prime numbers up to 19 ♣ multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers ♣ multiply and divide numbers mentally drawing upon known facts ♣ divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context ♣ multiply and divide whole numbers and those involving decimals by 10, 100 and 1000 	<ul style="list-style-type: none"> ♣ multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication ♣ divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context ♣ divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context ♣ perform mental calculations, including with mixed operations and large numbers ♣ identify common factors, common multiples and prime numbers ♣ use their knowledge of the order of operations to carry out calculations involving the four operations ♣ solve problems involving addition, subtraction, multiplication and division ♣ use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.
Fractions	Children are not explicitly taught fractions in the early	<ul style="list-style-type: none"> ♣ recognise, find and name a half as one of two equal 	<ul style="list-style-type: none"> ♣ recognise, find, name and write fractions $\frac{1}{3}$, $\frac{1}{4}$, 	<ul style="list-style-type: none"> ♣ recognise, find and write fractions of a discrete set of 	<ul style="list-style-type: none"> ♣ recognise and show, using diagrams, families of 	<ul style="list-style-type: none"> ♣ compare and order fractions whose 	<ul style="list-style-type: none"> ♣ use common factors to simplify fractions; use

	years but when exploring capacity, they refer to things being half full, full, empty and nearly empty which is a pre-fraction skill as it is building understanding of wholes and halves.	parts of an object, shape or quantity ♣ recognise, find and name a quarter as one of four equal parts of an object, shape or quantity.	2/4 and ¾ of a length, shape, set of objects or quantity ♣ write simple fractions for example, ½ of 6 = 3 and recognise the equivalence of 2/4 and ½ .	objects: unit fractions and non-unit fractions with small denominators ♣ recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators ♣ recognise and show, using diagrams, equivalent fractions with small denominators ♣ add and subtract fractions with the same denominator within one whole [for example, $5/7 + 1/7 = 6/7$] ♣ compare and order unit fractions, and fractions with the same denominators ♣ solve problems that involve all of the above.	common equivalent fractions ♣ solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number ♣ add and subtract fractions with the same denominator ♣ recognise and write decimal equivalents of any number of tenths or hundredths ♣ recognise and write decimal equivalents to ¼, ½ and ¾ ♣ solve simple measure and money problems involving fractions and decimals to two decimal places.	denominators are all multiples of the same number ♣ identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths ♣ recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number [for example, $2/5 + 4/5 = 6/5 = 1 \frac{1}{5}$] ♣ add and subtract fractions with the same denominator and denominators that are multiples of the same number ♣ multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams ♣ read and write decimal numbers as fractions [for example, $0.71 = 71/100$] ♣ solve problems which require knowing percentage and decimal equivalents of ½ ¼ 1/5 , 2/5 4/5 and those fractions with a denominator of a multiple of 10 or 25.	common multiples to express fractions in the same denomination ♣ compare and order fractions, including fractions > 1 ♣ add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions ♣ multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, $1/4 \times 1/2 = 1/8$] ♣ divide proper fractions by whole numbers [for example, $1/3 \div 2 = 1/6$] ♣ associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, 3/8]
Decimals and percentages				♣ count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 ♣ recognise and write decimal equivalents to ¼ ½ and ¾ ♣ find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths ♣ round decimals with one decimal place to the nearest whole number ♣ compare numbers with the same number of decimal places up to two decimal places	♣ count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten. ♣ recognise and write decimal equivalents to ¼ ½ and ¾ ♣ find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths ♣ round decimals with one decimal place to the nearest whole number ♣ compare numbers with the same number of decimal places up to two decimal places	♣ multiply and divide whole numbers and those involving decimals by 10, 100 and 1000 ♣ read and write decimal numbers as fractions [for example, $0.71 = 71/100$] ♣ recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents ♣ round decimals with two decimal places to the nearest whole number and to one decimal place ♣ read, write, order and compare numbers with up to three decimal places ♣ solve problems involving number up to three decimal places ♣ recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred', and write	♣ associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, 3/8] ♣ identify the value of each digit in numbers given to three decimal places and multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places ♣ multiply one-digit numbers with up to two decimal places by whole numbers ♣ use written division methods in cases where the answer has up to two decimal places ♣ solve problems which require answers to be rounded to specified degrees of accuracy

						percentages as a fraction with denominator 100, and as a decimal <ul style="list-style-type: none"> ♣ solve problems which require knowing percentage and decimal equivalents of $\frac{1}{2}$ $\frac{1}{4}$ $\frac{1}{5}$, $\frac{2}{5}$ $\frac{4}{5}$ and those fractions with a denominator of a multiple of 10 or 25. 	<ul style="list-style-type: none"> ♣ recall and use equivalences between simple fractions, decimals and percentages, including in different contexts. ♣ solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison
Shape and patterns	<p>Copy, continue and create their own simple repeating patterns with at least three full units of repeat. AB, ABB, AABB, AAB, AABBB</p> <p>Including a range of shapes, colours and sizes</p> <p>Recall names for 2D shapes</p> <p>Recall some names for 3D shapes</p> <p>Explore which 3D shapes stack and roll</p>	<p>Recognise and name common 2-D and 3-D shapes, including: ♣ 2-D shapes [for example, rectangles (including squares), circles and triangles]</p> <p>♣ 3-D shapes [for example, cuboids (including cubes), pyramids and spheres].</p>	<ul style="list-style-type: none"> ♣ identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line ♣ identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces ♣ identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid] ♣ compare and sort common 2-D and 3-D shapes and everyday objects. 	<ul style="list-style-type: none"> ♣ draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them ♣ identify horizontal and vertical lines and pairs of perpendicular and parallel lines. 	<ul style="list-style-type: none"> ♣ compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes ♣ identify lines of symmetry in 2-D shapes presented in different orientations ♣ complete a simple symmetric figure with respect to a specific line of symmetry. 	<ul style="list-style-type: none"> ♣ identify 3-D shapes, including cubes and other cuboids, from 2-D representations ♣ use the properties of rectangles to deduce related facts and find missing lengths and angles ♣ distinguish between regular and irregular polygons based on reasoning about equal sides and angles. 	<ul style="list-style-type: none"> ♣ draw 2-D shapes using given dimensions and angles ♣ recognise, describe and build simple 3-D shapes, including making nets ♣ compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons ♣ illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius
Angles				<ul style="list-style-type: none"> ♣ recognise angles as a property of shape or a description of a turn ♣ identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle 	<ul style="list-style-type: none"> ♣ identify acute and obtuse angles and compare and order angles up to two right angles by size 	<ul style="list-style-type: none"> ♣ know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles ♣ draw given angles, and measure them in degrees (o) <p>identify:</p> <ul style="list-style-type: none"> ♣ angles at a point and one whole turn (total 360o) ♣ angles at a point on a straight line and 2 1 a turn (total 180o) ♣ other multiples of 90o 	<ul style="list-style-type: none"> ♣ draw 2-D shapes using given dimensions and angles ♣ recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles.
Position and direction	<p>Respond to positional language in practical situations e.g. when tidying up, put the blocks next to the beads.</p> <p>Begin to use positional language to describe where things are in relation to each other</p>	<p>Describe position, direction and movement, including whole, half, quarter and three-quarter turns.</p>	<ul style="list-style-type: none"> ♣ order and arrange combinations of mathematical objects in patterns and sequences ♣ use mathematical vocabulary to describe position, direction and movement, including movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anti-clockwise). 	<ul style="list-style-type: none"> ♣ recognise angles as a property of shape or a description of a turn 	<ul style="list-style-type: none"> ♣ describe positions on a 2-D grid as coordinates in the first quadrant ♣ describe movements between positions as translations of a given unit to the left/right and up/down ♣ plot specified points and draw sides to complete a given polygon 	<ul style="list-style-type: none"> ♣ identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed. 	<ul style="list-style-type: none"> ♣ describe positions on the full coordinate grid (all four quadrants) ♣ draw and translate simple shapes on the coordinate plane, and reflect them in the axes.

Money	<p>Money is not explicitly taught in EYFS but children will still explore coins within provision to familiarise the concept of money being used to pay for things. Children may count 1p coins but not others as they are still learning to understand the concept of unitising.</p>	<ul style="list-style-type: none"> recognise and know the value of different denominations of coins and notes 	<ul style="list-style-type: none"> recognise and use symbols for pounds (£) and pence (p); combine amounts to make a particular value find different combinations of coins that equal the same amounts of money solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change 	<ul style="list-style-type: none"> add and subtract amounts of money to give change, using both £ and p in practical contexts 	<ul style="list-style-type: none"> estimate, compare and calculate different measures, including money in pounds and pence 	<ul style="list-style-type: none"> use all four operations to solve problems involving measure [for example, length, mass, volume, money] using decimal notation, including scaling. 	
Measurement	<p>Compare and order objects by size and mass and describe using mathematical language</p> <p>Sort objects based on their size and mass</p> <p>Use balance scales to explore mass</p> <p>Apply their understanding of language into practical tasks e.g. build a taller tower</p> <p>Explore basic capacity practically e.g. how many scoops of sand will this container hold; how many cups of water will this bucket hold</p> <p>Measure using non-standard units of measure e.g. 3 hands long</p>	<p>Compare, describe and solve practical problems for:</p> <ul style="list-style-type: none"> lengths and heights [for example, long/short, longer/shorter, tall/short, double/half] mass/weight [for example, heavy/light, heavier than, lighter than] capacity and volume [for example, full/empty, more than, less than, half, half full, quarter] time [for example, quicker, slower, earlier, later] <p>Measure and begin to record the following:</p> <ul style="list-style-type: none"> lengths and heights mass/weight capacity and volume time (hours, minutes, seconds) 	<ul style="list-style-type: none"> choose and use appropriate standard units to estimate and measure length/height in any direction (m/cm); mass (kg/g); temperature (°C); capacity (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels compare and order lengths, mass, volume/capacity and record the results using >, < and = 	<ul style="list-style-type: none"> measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml) 	<ul style="list-style-type: none"> Convert between different units of measure [for example, kilometre to metre; hour to minute] estimate, compare and calculate different measures, including money in pounds and pence 	<ul style="list-style-type: none"> convert between different units of metric measure (for example, kilometre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre) understand and use approximate equivalences between metric units and common imperial units such as inches, pounds and pints use all four operations to solve problems involving measure [for example, length, mass, volume, money] using decimal notation, including scaling. 	<ul style="list-style-type: none"> solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation up to three decimal places convert between miles and kilometres
Time	<p>Order key events in daily routines</p> <p>Use language to describe when events happen – day, night, morning, afternoon, before, after, today, tomorrow, now, next, later</p> <p>Informally measure time e.g. how many jumps can I do before the sand timer runs out or use a calendar to count down how many days until an event</p>	<ul style="list-style-type: none"> sequence events in chronological order using language [for example, before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] recognise and use language relating to dates, including days of the week, weeks, months and years tell the time to the hour and half past the hour and draw the hands on a clock face to show these times. 	<ul style="list-style-type: none"> compare and sequence intervals of time tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times know the number of minutes in an hour and the number of hours in a day. 	<ul style="list-style-type: none"> tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes and hours; use vocabulary such as o'clock, a.m./p.m., morning, afternoon, noon and midnight know the number of seconds in a minute and the number of days in each month, year and leap year compare durations of events [for example to 	<ul style="list-style-type: none"> read, write and convert time between analogue and digital 12- and 24-hour clocks solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days. 	<ul style="list-style-type: none"> solve problems involving converting between units of time 	<p>use, read, write and convert between standard units, converting measurements of time from a smaller unit of measure to a larger unit, and vice versa,</p>

				calculate the time taken by particular events or tasks]. ♣ measure the perimeter of simple 2-D shapes			
Area, perimeter and volume					♣ measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres ♣ find the area of rectilinear shapes by counting squares	♣ measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres ♣ calculate and compare the area of rectangles (including squares), and including using standard units, square centimetres (cm ²) and square metres (m ²) and estimate the area of irregular shapes ♣ estimate volume [for example, using 1 cm ³ blocks to build cuboids (including cubes)] and capacity [for example, using water]	♣ recognise that shapes with the same areas can have different perimeters and vice versa ♣ recognise when it is possible to use formulae for area and volume of shapes ♣ calculate the area of parallelograms and triangles ♣ calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm ³) and cubic metres (m ³), and extending to other units [for example, mm ³ and km ³].
Statistics			♣ interpret and construct simple pictograms, tally charts, block diagrams and simple tables ♣ ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity ♣ ask and answer questions about totalling and comparing categorical data.	♣ interpret and present data using bar charts, pictograms and tables ♣ solve one-step and two-step questions [for example, 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables.	♣ interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs. ♣ solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs.	♣ solve comparison, sum and difference problems using information presented in a line graph ♣ complete, read and interpret information in tables, including timetables.	♣ interpret and construct pie charts and line graphs and use these to solve problems ♣ calculate and interpret the mean as an average.
Ratio					integer scaling problems and harder correspondence problems such as n objects are connected to m objects.	use all four operations to solve problems involving measure [for example, length, mass, volume, money] using decimal notation, including scaling.	♣ solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts ♣ solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison ♣ solve problems involving similar shapes where the scale factor is known or can be found ♣ solve problems involving unequal sharing and grouping using knowledge of fractions and multiples.
Algebra							♣ use simple formulae ♣ generate and describe linear number sequences ♣ express missing number problems algebraically ♣ find pairs of numbers that satisfy an equation with two unknowns

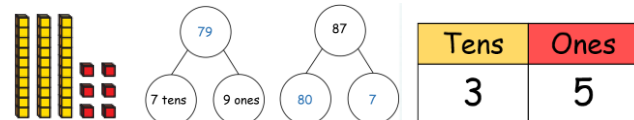
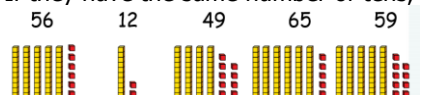
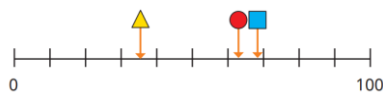



							★ enumerate possibilities of combinations of two variables.
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Number, Counting and Place Value

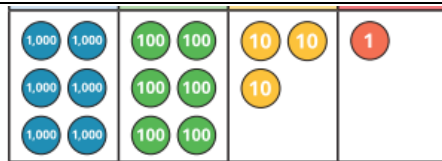
Progression of Knowledge	This is the fundamental area of mathematics. It is essential that children leave each year group having acquired a firm understanding of the knowledge and procedures linked to number, counting and place value to enable them to progress throughout the curriculum as numbers become larger and concepts from other areas of Maths are applied to increasingly larger numbers. This is why this strand is always covered at the outset of a year as it is the foundation of all learning. The only exception being EYFS and Year 1 where children study number, counting and place value regularly throughout the year so that deep early number experiences are prioritised. Early number sense is essential here and the counting skills developed in EYFS are crucial for mastering an understanding of number.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'																				
EYFS	<table><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr></table> <p>To count we need to:</p> <ul style="list-style-type: none">• Say the number words in order• Point to the objects• Count one number name per object• Not miss any out• The last number counted is the total <p>Zero is when there are no objects and no number</p> <p>Subitise = recognising small numbers without having to count them</p> <div><div><div><div></div><div></div></div><div><div></div><div></div></div></div><div><div><div></div><div></div><div></div></div><div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div></div></div> <p>We can break numbers down into smaller parts</p> <div><div><div></div><div></div><div></div></div><div><div></div><div></div><div></div></div></div> <p>5 is made of 4 and 1</p>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	<p>Verbally count beyond 20, recognising the pattern of the counting system</p> <p>Have a deep understanding of number to 10, including the composition of each number</p> <p>Subitise (recognise quantities without counting) up to 5 (regular arrangements and some irregular arrangements)</p> <div><div><div></div><div></div></div><div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div></div> <p>Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity</p>	<p>Solve simple practical problems in familiar contexts led by the teacher</p> <p>e.g. Ben, Sam and Tom are playing dominoes Ben's domino has fewer than 5 spots Sam's domino has 5 spots Tom's domino has greater than 5 spots</p> <p>Which pieces could they have?</p>
1	2	3	4	5	6	7	8	9	10														
11	12	13	14	15	16	17	18	19	20														

	<p>Greater than = one set or number has more</p> <p>Less than = one set or number has fewer</p> <p>Equal to = the same as</p> <p>Even numbers = share equally into groups of 2</p> <p>Odd numbers = will not share equally into groups of 2</p>	<p>Explore and represent patterns within numbers up to 10, including evens and odds</p>																																																																																																					
Year 1	<table><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr><tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr><tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr><tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr><tr><td>61</td><td>62</td><td>63</td><td>64</td><td>65</td><td>66</td><td>67</td><td>68</td><td>69</td><td>70</td></tr><tr><td>71</td><td>72</td><td>73</td><td>74</td><td>75</td><td>76</td><td>77</td><td>78</td><td>79</td><td>80</td></tr><tr><td>81</td><td>82</td><td>83</td><td>84</td><td>85</td><td>86</td><td>87</td><td>88</td><td>89</td><td>90</td></tr><tr><td>91</td><td>92</td><td>93</td><td>94</td><td>95</td><td>96</td><td>97</td><td>98</td><td>99</td><td>100</td></tr></table> <p>We can make groups of ten to make it easier to count</p> <p>Ten ones = one ten</p> <p>We can represent the tens and ones in a number in different ways</p> <p>Multiples of 2 – 2, 4, 6, 8, 10, 12, 14, 16, 18, 20</p> <p>Multiples of 5 – 5, 10, 15, 20, 25, 30, 35, 40, 45, 50</p> <p>Multiples of 10 – 10, 20, 30, 40, 50, 60, 70, 80, 90, 100</p> <p>One more = the number after, adding one</p> <p>One less = the number before, subtracting one</p> <p>Equal to = the same as</p>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	<p>Count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number</p> <p>Read and write numbers to 100 in numerals</p> <p>Partition a number into tens and ones</p> <p>Count in multiples of twos, fives and tens</p> <p>Given a number, identify one more and one less</p> <p>Identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least</p> <p>Read and write numbers from 1 to 20 in numerals and words.</p>	<p>Use place value and number facts to solve problems.</p> <p>Mo is playing a game.</p> <p>He scores 10 points for every bean bag that lands in the hoop.</p> <p>He scores 50 points in total.</p> <p>How many bean bags does Mo get in the hoop?</p> <p>Ben scores 10 fewer points than Mo.</p> <p>How many points does Ben score?</p>
1	2	3	4	5	6	7	8	9	10																																																																																														
11	12	13	14	15	16	17	18	19	20																																																																																														
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61	62	63	64	65	66	67	68	69	70																																																																																														
71	72	73	74	75	76	77	78	79	80																																																																																														
81	82	83	84	85	86	87	88	89	90																																																																																														
91	92	93	94	95	96	97	98	99	100																																																																																														

	<p>More than = greater Less than = fewer</p>										
Year 2	<p>A number can be split into tens and ones Ten ones = one ten</p> <div></div> <p>To write numbers in words, we need to know the numbers to 20 and:</p> <table><tr><td>Thirty</td><td>Forty</td><td>Fifty</td><td>Sixty</td></tr><tr><td>Seventy</td><td>Eighty</td><td>Ninety</td><td>One-hundred</td></tr></table> <p>We can then put them together e.g seventy-nine</p> <p>Counting in 2s – 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24 Counting in 3s – 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36 Counting in 5s – 5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60</p> <p>Counting on in tens from a number – keep adding one to the tens column e.g. 23, 33, 43, 53, 63</p> <p>Counting back in tens from a number – keep subtracting one to the tens column e.g. 85, 75, 65, 55, 45</p> <p>> greater than < less than = equal to</p> <p>Numbers with the greatest number of tens are bigger If they have the same number of tens, we look to the ones</p> <div></div>	Thirty	Forty	Fifty	Sixty	Seventy	Eighty	Ninety	One-hundred	<p>Count in steps of 2, 3, and 5 from 0</p> <p>read and write numbers to at least 100 in numerals and in words</p> <p>count in tens from any number, forward and backward</p> <p>recognise the place value of each digit in a two-digit number (tens, ones)</p> <p>identify, represent and estimate numbers using different representations, including the number line</p> <div></div> <p>use < > and = signs to compare numbers up to 100</p> <p>order numbers from 0 up to 100</p> <div></div>	<p>Use place value and number facts to solve problems.</p> <p>Max labels an odd number on the number line. He spills some paint over his number. What could Max's number be?</p> <div></div> <p>Jo needs 72 candles.</p> <div></div> <p>How many more candles does Jo need?</p>
Thirty	Forty	Fifty	Sixty								
Seventy	Eighty	Ninety	One-hundred								
Year 3	<p>Ten tens = one hundred 3 digit numbers have hundreds, tens and ones</p> <table><tr><td>Hundreds</td><td>Tens</td><td>Ones</td></tr></table>	Hundreds	Tens	Ones	<p>Count from 0 in multiples of 4, 8, 50 and 100</p> <p>read and write numbers up to 1000 in numerals and in words</p>	<p>Solve number problems and practical problems involving these ideas.</p>					
Hundreds	Tens	Ones									

	<div><div><div>4</div><div>2</div><div>5</div></div><div><div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div></div><div><div><div></div><div></div></div><div><div></div><div></div></div><div><div></div><div></div></div></div><div>4 hundreds, 2 tens and 5 ones $400 + 20 + 5 = 425$</div></div><div><p>To write bigger numbers, we use the numbers to hundred and put ____ hundred in front of it e.g. four-hundred and twenty-five</p><p>Multiples of 4 – 4, 8, 12, 16, 20, 24, 28, 32, 36, 40, 44, 48 Multiples of 8 – 8, 16, 24, 32, 40, 48, 56, 64, 72, 80, 88, 96 Multiples of 50 – 50, 100, 150, 200, 250, 300, 350, 400.. Multiples of 100 – 100, 200, 300, 400, 500...</p><p>Adding and subtracting 10 or 100 from a number can be done mentally Identify the tens or hundreds column and adjust this It may lead to surrounding columns needing to change if there is a 0 or 9 in the column</p><p>When comparing and ordering numbers, we can use a place value chart. The greater the number of hundreds, the greater the number. If they have the same amount of hundreds, we look to the tens and so on.</p></div></div>	<div><p>Find 10 or 100 more or less than a given number</p><p>Recognise the place value of each digit in a three-digit number (hundreds, tens, ones)</p><p>Compare numbers up to 1000</p><div><table><tr><td>Alex</td><td>428 cm</td></tr><tr><td>Annie</td><td>395 cm</td></tr><tr><td>Mo</td><td>403 cm</td></tr><tr><td>Rosie</td><td>083 cm</td></tr></table></div><p>Order numbers up to 1000</p><p>identify, represent and estimate numbers using different representations</p><div><div></div><div>0</div><div></div><div>1,000</div></div></div>	Alex	428 cm	Annie	395 cm	Mo	403 cm	Rosie	083 cm	<div><p>Each number has the same digit missing.</p><div><div>__56 < 7__3 < 75__</div></div><p>What could the missing digits be?</p></div>
Alex	428 cm										
Annie	395 cm										
Mo	403 cm										
Rosie	083 cm										
Year 4	<div><p>Multiples of 6 – 6, 12, 18, 24, 30, 36, 42, 48, 54, 60, 66, 72 Multiples of 7 – 7, 14, 21, 28, 35, 42, 49, 56, 63, 70, 77, 84 Multiples of 9 – 9, 18, 27, 36, 45, 54, 63, 72, 81, 90, 99 108 Multiples of 25 – 25, 50, 75, 100, 125, 150, 175, 200, 225... Multiples of 1000 – 1000, 2000, 3000, 4000, 5000 ...</p><p>The thousands column comes before the hundreds column – it is ten times bigger Ten hundreds = one thousand</p><div><table><tr><td>Thousands</td><td>Hundreds</td><td>Tens</td><td>Ones</td></tr><tr><td>6</td><td>6</td><td>3</td><td>1</td></tr></table></div></div>	Thousands	Hundreds	Tens	Ones	6	6	3	1	<div><p>Count in multiples of 6, 7, 9, 25 and 1000</p><p>Find 1000 more or less than a given number by adjusting the thousands column</p><p>Count backwards through 0 to include negative numbers</p><p>Determine the value of each digit in a 4-digit number and partition</p><p>Compare numbers with 4 digits</p></div>	<div><p>solve number and practical problems that involve all of the above and with increasingly large positive numbers</p><p>There are 2,458 children in a school.</p><div><div></div><div></div></div><p>a) Round the number of children to the nearest 10</p></div>
Thousands	Hundreds	Tens	Ones								
6	6	3	1								

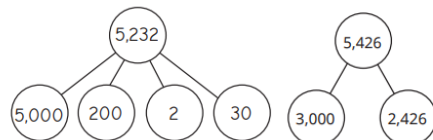


6 **thousands**, 6 **hundreds**, 3 **tens** and 1 **one**

$$6000 + 600 + 30 + 1 =$$

6631

We can **partition** numbers in different ways



We use a comma after the **thousands** – these are used to help with reading and writing longer numbers

6,631

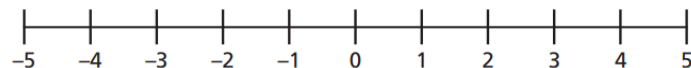
Six-thousand, three-hundred and thirty-one

Adding and subtracting 1000 from a number can be done **mentally**

Identify the **thousands column** and adjust this

It may lead to surrounding columns needing to change if there is a 0 or 9 in the thousands column

We can count backwards past **zero** into **negative numbers**



When **rounding** numbers, we decide which **multiple** it is closest to

To the nearest ten – the multiple of 10 that it is closest to

To the nearest hundred – the multiple of 100 that it is closest to

To the nearest thousand – the multiple of 1000 that it is closest to

01234 – rounds down to the multiple before

56789 – rounds up to the multiple after

Roman numerals were used in the past for numbers.

Over time, the numeral system changed to include the concept of **zero** and **place value**.

The Roman system does not have a zero or place holders.

It uses letters to represent numbers

Order sets of numbers with 4 digits

Mountain	Height (m)
Mount Elbrus	5,642
Kilimanjaro	5,895
Aconcagua	6,962
Mont Blanc	4,810
Mount Everest	8,848

Write the names of the mountains in order starting with the highest.

Thousands	Hundreds	Tens	Ones
5	6	4	2
5	8	9	5
6	9	6	2
4	8	1	0
8	8	4	8

Round any number to the nearest 10, 100 or 1000

Read Roman numerals to 100 (I to C)

Teddy and Scott have some digit cards.



Teddy makes the number 4,571

Scott says his number is greater than Teddy's.

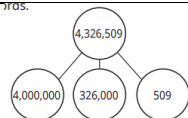
Teddy says Scott's number must start with a 5

Is Teddy correct? _____

	<p>$I = 1$ $V = 5$ $X = 10$ $L = 50$ $C = 100$</p> <p>There would never be more than 3 numerals the same next to each other $XXX = 30$</p> <p>A smaller numeral in front of a bigger numeral means one less than e.g. XL means 10 less than 50 = 40</p>																																												
Year 5	<p>Ten thousands = 1 ten thousand 10 ten thousands = 1 hundred thousand Every column is ten times bigger</p> <table><tr><th>HTh</th><th>TTh</th><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td>●●●●</td><td>●●</td><td>●●</td><td>●●●●</td><td>●●●●</td><td>●</td></tr></table> <p>We use the help us read numbers 422,441</p> <table><tr><td>4</td><td>2</td><td>2</td><td>4</td><td>4</td><td>1</td></tr><tr><td>400,000</td><td>20,000</td><td>2,000</td><td>400</td><td>40</td><td>1</td></tr></table> <p>Four-hundred and twenty-two THOUSAND four-hundred and forty-one</p> <p>When solving problems with negative numbers, we use a number line</p> <p>—5 —4 —3 —2 —1 0 1 2 3 4 5</p> <p>You can round a number to any degree of accuracy – nearest ten, hundred...hundred thousand Digits 0,1,2,3,4 will round down to the multiple before Digits 5,6,7,8,9 will round up to the multiple after</p> <p>The Roman numerals system does not have a zero or place holders. It uses letters to represent numbers $I = 1$ $V = 5$ $X = 10$</p>	HTh	TTh	Th	H	T	O	●●●●	●●	●●	●●●●	●●●●	●	4	2	2	4	4	1	400,000	20,000	2,000	400	40	1	<p>Read and write numbers to at least 1 000 000</p> <p>Determine the value of each digit in numbers to at least 1 000 000</p> <p>order and compare numbers to at least 1 000 000</p> <p>65,000 ○ 60,700</p> <p>List the towns and cities in descending order of population.</p> <table><tr><th>Town or city</th><th>Population</th></tr><tr><td>Halifax</td><td>88,134</td></tr><tr><td>Brighouse</td><td>32,360</td></tr><tr><td>Leeds</td><td>792,925</td></tr><tr><td>Huddersfield</td><td>146,234</td></tr><tr><td>Wakefield</td><td>343,932</td></tr><tr><td>Bradford</td><td>536,986</td></tr></table> <p>count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000</p> <p>interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero</p> <p>round any number up to 1 000 000 to the nearest 10, 100, 1000, 10 000 and 100 000</p>	Town or city	Population	Halifax	88,134	Brighouse	32,360	Leeds	792,925	Huddersfield	146,234	Wakefield	343,932	Bradford	536,986	<p>solve number and practical problems that involve understanding of place value</p> <p>The children choose one of these number cards each.</p> <table><tr><td>29,000</td><td>290</td><td>2,900</td><td>290,000</td></tr></table> <p>Tommy: My number is ten times the size of Annie's. Whitney: Dexter's number is one-tenth the size of my number. Annie: My number has two hundreds. Dexter: My number is one hundred times the size of Annie's.</p> <p>Which number does each child have?</p> <p>Solve problems requiring rounding to a degree of accuracy</p> <p>328,154 people buy tickets for a festival. Tickets are printed in batches of 10,000 How many batches of tickets should the organisers print?</p> <p>Solve simple negative number problems in contexts The temperature on Monday was 4°C. a) That night the temperature fell by 7°C. What was the temperature at night?</p>	29,000	290	2,900	290,000
HTh	TTh	Th	H	T	O																																								
●●●●	●●	●●	●●●●	●●●●	●																																								
4	2	2	4	4	1																																								
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29,000	290	2,900	290,000																																										

	<p>L = 50 C = 100 D = 500 M = 1000</p> <p>There would never be more than 3 numerals the same next to each other CCC = 300</p> <p>A smaller numeral in front of a bigger numeral means one less than e.g. CD means 100 less than 500 = 400</p> <p>We can use the bigger letters to represent dates e.g. MMXXI</p>	<p>read Roman numerals to 1000 (M) and recognise years written in Roman numerals.</p>																																											
Year 6	<table><tr><th>Millions</th><th colspan="3">Thousands</th><th colspan="3">Ones</th></tr><tr><th>O</th><th>H</th><th>T</th><th>O</th><th>H</th><th>T</th><th>O</th></tr><tr><td>4</td><td>2</td><td>8</td><td>7</td><td>2</td><td>9</td><td>5</td></tr></table> <p>The millions column comes before the hundred thousand</p> <p>column – it is ten times bigger Ten hundred thousands = one million</p> <p>When writing bigger numbers, we mark every third digit from the ones with a comma – we can use this to help us read the numbers</p> <p>4,326,509</p> <p>Four million, three-hundred and twenty-six thousand, five-hundred and nine</p> <p>When partitioning numbers, we can count the columns after the digit to determine how many 0s a number will have.</p> <table><tr><th>Millions</th><th colspan="3">Thousands</th><th colspan="3">Ones</th></tr><tr><th>O</th><th>H</th><th>T</th><th>O</th><th>H</th><th>T</th><th>O</th></tr><tr><td>4</td><td>2</td><td>8</td><td>7</td><td>2</td><td>9</td><td>5</td></tr></table> <p>4,000,000 200,000 80,000 7,000 200 90 5</p> <p>Numbers can be partitioned in different ways</p>	Millions	Thousands			Ones			O	H	T	O	H	T	O	4	2	8	7	2	9	5	Millions	Thousands			Ones			O	H	T	O	H	T	O	4	2	8	7	2	9	5	<p>Read and write numbers up to 10 000 000</p> <p>Determine the value of each digit of numbers up to 10 000 000</p> <p>Order and compare numbers up to 10 000 000</p> <p>Round any whole number to any degree of accuracy</p> <p>Use negative numbers in context, and calculate intervals across zero</p>	<p>Solve number and practical problems showing understanding of the place value of numbers</p> <p>Here are some clues to a 7-digit number.</p> <ul style="list-style-type: none">There is nothing in the thousands or hundreds columns.The tens digit is 1 less than the millions digit.The ones digit is 1 less than the tens digit.The hundred-thousands digit is 4The digit sum is 15 <p>a) What could the number be?</p> <p>Understand the contexts when rounding is useful and solve problems involving rounding</p> <p>A and B are integers.</p> <p>A = 300,000 to the nearest 100,000 B = 300,000 to the nearest 10,000</p> <p>a) What is the greatest possible value of A + B?</p> <p>Solve problems using negative numbers in real-life contexts</p> <p>A ship sits in the sea.</p> <ul style="list-style-type: none">The base of the ship is 5 m below sea level.The top of the ship is 11 m above sea level. <p>How tall is the ship?</p>
Millions	Thousands			Ones																																									
O	H	T	O	H	T	O																																							
4	2	8	7	2	9	5																																							
Millions	Thousands			Ones																																									
O	H	T	O	H	T	O																																							
4	2	8	7	2	9	5																																							

1705.



To **order** and **compare** numbers, put them into a **place value grid**

Start at the biggest column

If it is the same, move onto the next column

212,731 < 233,814

M	HTh	TTh	Th	H	T	O
	2	1	2	7	3	1
	2	3	3	8	1	4

Rounding is useful to **approximate** larger numbers

You can round a number to any degree of accuracy – nearest ten, hundred...million. The degree of accuracy will depend on the context

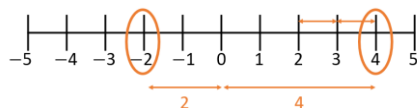
Digits 0,1,2,3,4 will round down

Digits 5,6,7,8,9 will round up

Negative numbers are numbers below zero


Common contexts include temperature and bank accounts

To calculate across zero, a number line is useful



Addition and Subtraction

Progression of Knowledge	<p>Once children are secure with numbers and counting, they move towards addition. Once secure with addition, they will progress towards subtracting, noting the links between the two operations through use of consistent visual representations such as part-whole models and bar models.</p> <p>Children learn the concept of addition and subtraction in the Early Years along with key facts, bonds and double facts. This extends in Year 1 so that children can confidently recall all addition and subtraction facts needed to formalise methods in Key Stage 2. Formal written methods are learnt to automaticity throughout Key Stage 2 as children apply these methods to bigger numbers, decimals and mixed operations.</p> <p>At all stages, it is important that emphasis and thought is given to which calculations would be better done mentally and which would be more efficient with a method.</p>
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'																																																							
EYFS	<p>We combine groups to make a total The quantity of a group can be changed by adding more The quantity of a group can be changed by taking away Addition facts within 5</p> <table><tr><td>+</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>0</td><td>0 + 0</td><td>0 + 1</td><td>0 + 2</td><td>0 + 3</td><td>0 + 4</td><td>0 + 5</td></tr><tr><td>1</td><td>1 + 0</td><td>1 + 1</td><td>1 + 2</td><td>1 + 3</td><td>1 + 4</td><td></td></tr><tr><td>2</td><td>2 + 0</td><td>2 + 1</td><td>2 + 2</td><td>2 + 3</td><td></td><td></td></tr><tr><td>3</td><td>3 + 0</td><td>3 + 1</td><td>3 + 2</td><td></td><td></td><td></td></tr><tr><td>4</td><td>4 + 0</td><td>4 + 1</td><td></td><td></td><td></td><td></td></tr><tr><td>5</td><td>5 + 0</td><td></td><td></td><td></td><td></td><td></td></tr></table> <p>Including related subtraction facts e.g 5-2</p> <p>Number bonds to 10</p> <table><tr><td>0 + 10</td><td>1 + 9</td><td>2 + 8</td><td>3 + 7</td><td>4 + 6</td><td>5 + 5</td></tr></table> <p>Including related subtraction facts</p>	+	0	1	2	3	4	5	0	0 + 0	0 + 1	0 + 2	0 + 3	0 + 4	0 + 5	1	1 + 0	1 + 1	1 + 2	1 + 3	1 + 4		2	2 + 0	2 + 1	2 + 2	2 + 3			3	3 + 0	3 + 1	3 + 2				4	4 + 0	4 + 1					5	5 + 0						0 + 10	1 + 9	2 + 8	3 + 7	4 + 6	5 + 5	<p>Combine two groups to find a total in many contexts using real objects (encourage to subitise for the groups)</p> <p>Reduce a group by taking away</p>	<p>Solve simple one-step problems that involve addition and subtraction, using concrete objects and in familiar and known contexts e.g 3 people are on the bus and 2 more get on.</p> <p>Represent number stories using ten frames</p>  <p>First there were 5 people on the bus. Then 2 people got off the bus. Now there are 3 people on the bus.</p>
+	0	1	2	3	4	5																																																				
0	0 + 0	0 + 1	0 + 2	0 + 3	0 + 4	0 + 5																																																				
1	1 + 0	1 + 1	1 + 2	1 + 3	1 + 4																																																					
2	2 + 0	2 + 1	2 + 2	2 + 3																																																						
3	3 + 0	3 + 1	3 + 2																																																							
4	4 + 0	4 + 1																																																								
5	5 + 0																																																									
0 + 10	1 + 9	2 + 8	3 + 7	4 + 6	5 + 5																																																					
Year 1	<p>The + symbol – plus, add The – symbol – subtract, take away The = symbol – equals, is equal to</p> <p>Addition facts to 10 fluently including related subtraction facts</p>	<p>read, write and interpret mathematical statements involving addition (+), subtraction (–) and equals (=) signs</p> <p>represent and use number bonds and related subtraction facts within 20</p>	<p>Solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = ? – 9.</p>																																																							

+	0	1	2	3	4	5	6	7	8	9	10
0	0+0	0+1	0+2	0+3	0+4	0+5	0+6	0+7	0+8	0+9	0+10
1	1+0	1+1	1+2	1+3	1+4	1+5	1+6	1+7	1+8	1+9	
2	2+0	2+1	2+2	2+3	2+4	2+5	2+6	2+7	2+8		
3	3+0	3+1	3+2	3+3	3+4	3+5	3+6	3+7			
4	4+0	4+1	4+2	4+3	4+4	4+5	4+6				
5	5+0	5+1	5+2	5+3	5+4	5+5					
6	6+0	6+1	6+2	6+3	6+4						
7	7+0	7+1	7+2	7+3							
8	8+0	8+1	8+2								
9	9+0	9+1									
10	10+0										

For **near doubles**, we can double the number and then add or subtract one as needed.
e.g. $7 + 8$
double 7 is 14 and one more is 15

add and subtract one-digit and two-digit numbers to 20, including zero



8 more
than my number
is 14

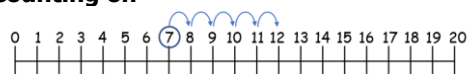
What number is Kim thinking of?

Number bonds to 20

$1 + 19$	$2 + 18$	$3 + 17$	$4 + 16$	$5 + 15$
$6 + 14$	$7 + 13$	$8 + 12$	$9 + 11$	$10 + 10$

We can add by:

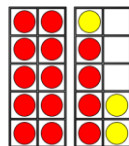
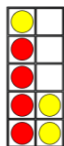
Counting on



Using **number bonds** and the **addition facts** that we know

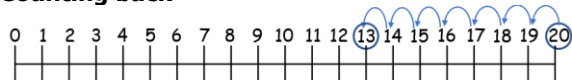
$$4 + 3 = 7$$

$$14 + 3 = 17$$

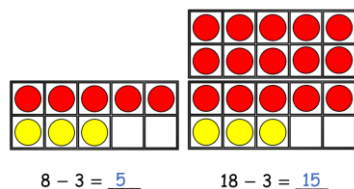


We can subtract by:

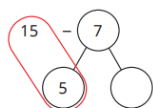
Counting back



Using the **number bonds** and **subtraction facts** that we know



Partitioning the number that we are subtracting using our **addition facts**



Finding the difference = subtract the smallest number from the biggest number

Fact families

If we know an **addition fact**, we also know other **related facts**

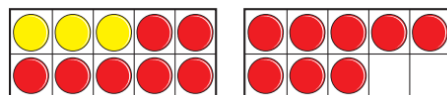
12	
4	8
4 + 8 = 12	12 - 4 = 8
8 + 4 = 12	12 - 8 = 4
12 = 4 + 8	4 = 12 - 8
12 = 8 + 4	8 = 12 - 4

Year 2

Addition and subtraction facts to 20

1 + 19	2 + 18	3 + 17	4 + 16	5 + 15
6 + 14	7 + 13	8 + 12	9 + 11	10 + 10

We can use addition facts to find out other **related facts** with **fact families**



$$\begin{aligned} 3 + 15 &= 18 \\ 15 + 3 &= 18 \\ 18 - 3 &= 15 \\ 18 - 15 &= 3 \end{aligned}$$

We can use **number bonds** to work out bigger numbers
e.g. 3 + 5 = 8, 3 tens + 5 tens = 8 tens, 30 + 50 = 80

Use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100

Add and subtract numbers using concrete objects, pictorial representations, and mentally, including:

- a two-digit number and ones
- a two-digit number and tens
- two two-digit numbers
- adding three one-digit numbers

compare calculations

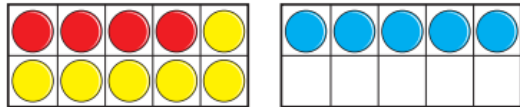
Solve problems with addition and subtraction:

- using concrete objects and pictorial representations, including those involving numbers, quantities and measures
- applying their increasing knowledge of mental and written methods

Bonds to 100:

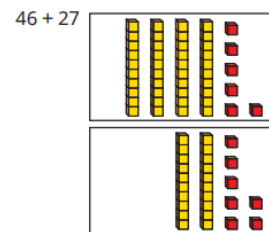
0 + 100	10 + 90	20 + 80	30 + 70	40 + 60	50 + 50
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When adding 3 one-digit numbers, this can be done in any order. Look for **number bonds** or **near doubles** to make it easier



$$4 + 6 + 5 = \underline{\quad}$$

To find 10 more or 10 less, **adjust** the **tens column** only



To add or subtract two numbers, we can **partition** them and add/subtract the ones and the tens

Ten ones = one ten
This can be **exchanged**

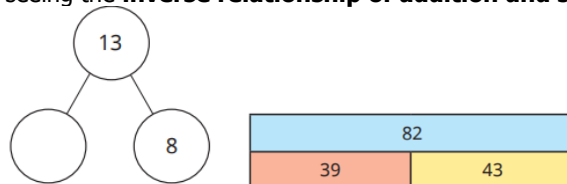
Addition of two numbers can be done in any order (commutative)

Subtraction of one number from another cannot be done in any order

Addition and **subtraction** are the **inverse** of each other

They are the opposite

Bar models and part whole models are useful representations for seeing the **inverse relationship of addition and subtraction**



There are two different subtractions that you can do

Addition is **commutative**; **subtraction** is not

$$35 + 12 \quad \bigcirc \quad 41 - 18$$

Recognise and use the inverse relationship between addition and subtraction and use this to check calculations

$$9 + 9 = 10 + \star$$

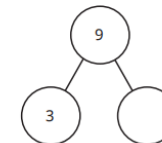
$$\star + \star = \triangle$$

$$27 + \triangle = \bigcirc$$

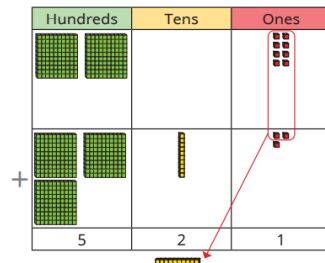
$$\square + \bigcirc = 87$$

Use the inverse relationship between addition and subtraction to check calculations and solve missing number problems.

$$53 - 9 = 50 - \underline{\quad}$$



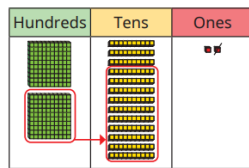
Year 3



H	T	O
2	0	8
+	3	1
5	2	1

ten **ones** can be **exchanged** for one **ten**

ten **tens** can be **exchanged** for one **hundred**



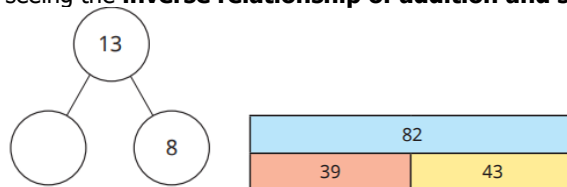
H	T	O
1	4	1
-	1	4
		1

If the numbers have a different number of **digits**, **place value columns** must be lined up accurately

H	T	O
2	5	5
+	5	4

We can **estimate** answers by using a number line and thinking what a number is close to

Addition and **subtraction** are the **inverse** of each other
They are the opposite
Bar models and part whole models are useful representations for seeing the **inverse relationship of addition and subtraction**



Add and subtract numbers mentally, including:

- a three-digit number and ones
- a three-digit number and tens
- a three-digit number and hundreds

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

$$\begin{array}{r} 789 \\ + 642 \\ \hline 1431 \end{array}$$

789 + 642 becomes 1431
Answer: 1431

$$\begin{array}{r} 932 \\ - 457 \\ \hline 475 \end{array}$$

932 - 457 becomes 475
Answer: 475

estimate the answer to a calculation and use inverse operations to check answers

calculate complements to 100

solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction.

Start

378	+ 100	+ 200	- 200	+ 300
- 100	+ 300	- 500	+ 100	- 100
+ 500	- 300	+ 200	+ 200	- 100
- 200	+ 100	+ 100	- 100	+ 200
- 100	+ 300	- 500	+ 200	778

Finish

Find a path from the start to the finish so that your end number is 778

A tablet costs £329

▶ A laptop costs £154 more than the tablet.

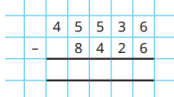



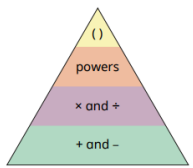
How much does the laptop cost?

▶ A TV costs £107 more than the laptop.

How much does the TV cost?

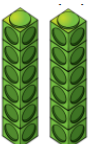
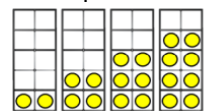
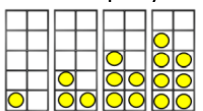
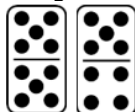


	<p>There are two different subtractions that you can do Addition is commutative; subtraction is not</p>																																										
Year 4	<p>Adding and subtracting 1000 from a number can be done mentally Identify the thousands column and adjust this It may lead to surrounding columns needing to change if there is a 0 or 9 in the thousands column</p> <p>If the numbers being added together have a different number of digits, place value columns must be lined up accurately</p> <table border="1"><tr><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>Th</td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td>2</td><td>7</td><td>0</td><td>6</td></tr><tr><td></td><td>+</td><td></td><td>1</td><td>0</td><td>3</td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td></tr></table> <p>Knowledge around exchange is the same as Year 3 but extended to apply to 4 digit numbers</p> <p>We can estimate answers by rounding both addends or subtrahends and calculating mentally</p> <p>We can also use the inverse to check answers</p> <p>Bar models and part whole models are useful representations for seeing the inverse relationship of addition and subtraction</p> <div><div><div>2,300</div><div></div><div>1,500</div></div><div>Complete the bar model for $3,582 - 2,236 = 1,346$</div><div><table border="1"><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table></div></div>									Th	H	T	O			2	7	0	6		+		1	0	3																	<p>add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate</p> <div><div><div>789 + 642 ----- 1431 ----- Answer: 1431</div><div>789 + 642 becomes</div></div><div><div>932 - 457 ----- 475 ----- Answer: 475</div><div>932 - 457 becomes</div></div></div> <p>estimate and use inverse operations to check answers to a calculation</p>	<p>solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why.</p> <p>1,235 people go on a school trip.</p> <p>There are 1,179 children and 27 teachers.</p> <p>The rest are parents.</p> <p>How many parents are there?</p>
		Th	H	T	O																																						
		2	7	0	6																																						
	+		1	0	3																																						
Year 5	<p>Rounding helps us check whether an answer is broadly accurate. e.g. $4836 + 1976$ rounded would be $5000 + 2000$ so the answer should be close to 7000.</p> <p>If you subtract one from each addend, the answer will be the same. This can help efficient calculations</p>	<p>add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)</p>	<p>solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.</p>																																								

	<p>e.g. $7000 - 4537$ would be $6999 - 4536$ and this would require no exchange</p>	 <p>add and subtract numbers mentally with increasingly large numbers</p> <p>use rounding to check answers to calculations</p> <p>Use knowledge of the inverse from previous years to solve calculations with larger numbers</p> <p>▶ $______ - 100 = 5,823$ ▶ $______ - 1,000 = 5,823$ ▶ $5,423 + ______ = 5,823$ ▶ $3,623 + ______ = 5,823$</p>	<p>Mr Rose is buying items for his home. He has a budget of £1,500</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> <p>washing machine</p>  <p>£699</p> </div> <div style="text-align: center;"> <p>tumble dryer</p>  <p>£479</p> </div> <div style="text-align: center;"> <p>dishwasher</p>  <p>£329</p> </div> </div> <p>He buys a washing machine and a tumble dryer. Does he have enough money left to buy the dishwasher?</p> <p>use rounding to determine, in the context of a problem, levels of accuracy</p>
Year 6	<p>If you subtract one from each addend, the answer will be the same. This can help efficient calculations Context of decimals e.g. $7 - 3.24$ would be $6.99 - 3.23$ and this would require no exchange</p> <p>When calculations have mixed operations, the order matters. Addition and subtraction would be done last</p>  <p>Estimating answers helps us check whether an answer is broadly accurate. We can do this by loosely rounding a number and calculating mentally</p>	<p>perform mental calculations, including with mixed operations and large numbers</p> <p>use their knowledge of the order of operations to carry out calculations involving the four operations</p> <p>use estimation to check answers to calculations</p>	<p>solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why</p> <p>solve multi-step problems involving addition, subtraction, multiplication and division including applying addition and subtraction procedures into other strands of mathematics. Problems should explore mixed operations in multi-steps</p> <p>In the context of a problem, use estimation to check an appropriate degree of accuracy.</p>

Multiplication and Division

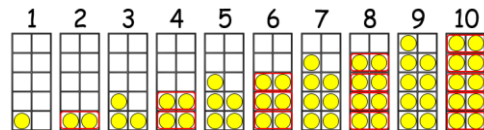
Progression of Knowledge	<p>Children start to progress in multiplication when they are secure with additive structures. In the Early Years, pupils will have many hands on and concrete experiences of sharing and making groups and this is built upon in Year 1 where pupils continue to group and share and explore arrays. Children are only introduced to the multiplication and division symbols in Year 2 where they start to understand how to represent these in number statements. At this stage, children will explore repeated addition and subtraction as well as informal methods of grouping and sharing to ensure that they leave KS1 with a firm understanding of the concept of multiplication and division. Throughout KS2, as their understanding of place value develops, children learn to apply this understanding to increasingly bigger numbers and more formalised methods to ensure accuracy and efficiency. Knowledge of table facts begins in Year 2 and progresses sequentially to allow deep learning links to be made through the learning of times tables. All children will leave Year 4 proficient in rapid recall of times table facts up to 12 x 12 to prepare them for the formalised methods of multiplication and division throughout Upper Key Stage 2.</p>
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
EYFS	<p>Double means twice as many</p> <p>Double 1 is 2 Double 2 is 4 Double 3 is 6 Double 4 is 8 Double 5 is 10</p>  <p>Sharing must be done equally – this means they are all the same amount</p> <p>Some quantities will share equally into 2 groups – these are even Some quantities will not share equally into 2 groups – these are odd</p>   <p>Even numbers Odd numbers</p>	<p>Understand double facts</p> <p>Build simple doubles</p> <p>Recognise doubles</p>  <p>Understand how quantities can be distributed equally.</p>	<p>Solve simple practical and contextual problems through familiar scenarios with the use of concrete objects to support e.g. these 3 teddy bears are coming to the teddy bear's picnic and we need to share the buns equally</p>

<div>Year 1</div>	<div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div>02468101214161820</div></div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div>05101520253035404550</div></div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div>0102030405060708090100</div></div></div><div><p>When sharing and grouping, groups have to be equal – this means the same amount in each group.</p><div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div></div><p>An array is arranging the groups in rows and columns</p><div><div><div></div><div></div><div></div></div><div><div></div><div></div><div></div></div><div><div></div><div></div><div></div></div></div><p>Doubling is 2 groups of a number or amount</p><table><tr><td>1 + 1 = 2</td><td>2 + 2 = 4</td><td>3 + 3 = 6</td><td>4 + 4 = 8</td><td>5 + 5 = 10</td></tr><tr><td>6 + 6 = 12</td><td>7 + 7 = 14</td><td>8 + 8 = 16</td><td>9 + 9 = 18</td><td>10 + 10 = 20</td></tr></table></div></div>	1 + 1 = 2	2 + 2 = 4	3 + 3 = 6	4 + 4 = 8	5 + 5 = 10	6 + 6 = 12	7 + 7 = 14	8 + 8 = 16	9 + 9 = 18	10 + 10 = 20	<div>Count in 2s, 5s and 10s</div> <div>Make and add equal groups</div> <div><div><div></div><div></div><div></div></div><div>There are 3</div><div></div><div>They each have 2 dots.</div><div>There are 3 equal groups of 2</div><div>There are 6 dots.</div></div> <div>Make arrays</div> <div>Share an amount into equal groups</div>	<div>Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.</div> <div>Ron needs to share 20 bananas between 5 boxes.</div> <div><div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div></div></div> <div>How many bananas will there be in each box?</div>
1 + 1 = 2	2 + 2 = 4	3 + 3 = 6	4 + 4 = 8	5 + 5 = 10									
6 + 6 = 12	7 + 7 = 14	8 + 8 = 16	9 + 9 = 18	10 + 10 = 20									
<div>Year 2</div>	<div><p>Multiplication is equal groups</p><p>The multiplication symbol is x</p><p>3 x 5 means 3 equal groups of 5</p><p>We can add the equal groups 5 + 5 + 5</p><div><div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div></div></div><div><div><div>2 times table</div><div>1 x 2 = 2</div><div>2 x 2 = 4</div><div>3 x 2 = 6</div><div>4 x 2 = 8</div><div>5 x 2 = 10</div><div>6 x 2 = 12</div><div>7 x 2 = 14</div><div>8 x 2 = 16</div><div>9 x 2 = 18</div><div>10 x 2 = 20</div><div>11 x 2 = 22</div><div>12 x 2 = 24</div></div><div><div>5 times table</div><div>1 x 5 = 5</div><div>2 x 5 = 10</div><div>3 x 5 = 15</div><div>4 x 5 = 20</div><div>5 x 5 = 25</div><div>6 x 5 = 30</div><div>7 x 5 = 35</div><div>8 x 5 = 40</div><div>9 x 5 = 45</div><div>10 x 5 = 50</div><div>11 x 5 = 55</div><div>12 x 5 = 60</div></div><div><div>10 times table</div><div>1 x 10 = 10</div><div>2 x 10 = 20</div><div>3 x 10 = 30</div><div>4 x 10 = 40</div><div>5 x 10 = 50</div><div>6 x 10 = 60</div><div>7 x 10 = 70</div><div>8 x 10 = 80</div><div>9 x 10 = 90</div><div>10 x 10 = 100</div><div>11 x 10 = 110</div><div>12 x 10 = 120</div></div></div></div>	<div>Recognise, make and add equal groups, relating this to multiplication</div> <div>Use multiplication and division facts for the 2, 5 and 10 multiplication tables</div> <div>Recognise odd and even numbers</div> <div>Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (x), division (÷) and equals (=) signs</div>	<div>Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.</div> <div>Kim buys 5 lollipops.</div> <div><div><div></div><div></div><div></div><div></div><div></div></div></div> <div>It costs 50p.</div> <div>How much do 2 lollipops cost?</div>										

Odd and even

Even numbers can be grouped into 2s; **odd numbers** cannot

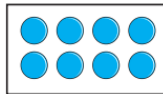


1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50

Even numbers will have 0,2,4,6 or 8 in the ones column

Odd numbers will have 1,3,5,7 or 9 in the ones column

Multiplication of two numbers can be done in any order (**commutative**)

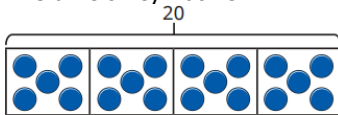


2 x 4 is the same as 4 x 2

Division of one number by another cannot be done in any order

Division is **sharing equally**

The division symbol is \div



$$20 \div 4 = 5$$

Doubling a number is multiplying by 2

Halving a number is dividing by 2

Multiplication is **equal groups**

We can show these equal groups using an **array**



2 times table

1 x 2 = 2
2 x 2 = 4
3 x 2 = 6
4 x 2 = 8
5 x 2 = 10
6 x 2 = 12
7 x 2 = 14
8 x 2 = 16
9 x 2 = 18
10 x 2 = 20
11 x 2 = 22

3 times table

1 x 3 = 3
2 x 3 = 6
3 x 3 = 9
4 x 3 = 12
5 x 3 = 15
6 x 3 = 18
7 x 3 = 21
8 x 3 = 24
9 x 3 = 27
10 x 3 = 30
11 x 3 = 33

4 times table

1 x 4 = 4
2 x 4 = 8
3 x 4 = 12
4 x 4 = 16
5 x 4 = 20
6 x 4 = 24
7 x 4 = 28
8 x 4 = 32
9 x 4 = 36
10 x 4 = 40
11 x 4 = 44

5 times table

1 x 5 = 5
2 x 5 = 10
3 x 5 = 15
4 x 5 = 20
5 x 5 = 25
6 x 5 = 30
7 x 5 = 35
8 x 5 = 40
9 x 5 = 45
10 x 5 = 50
11 x 5 = 55

8 times table

1 x 8 = 8
2 x 8 = 16
3 x 8 = 24
4 x 8 = 32
5 x 8 = 40
6 x 8 = 48
7 x 8 = 56
8 x 8 = 64
9 x 8 = 72
10 x 8 = 80
11 x 8 = 88

10 times table

1 x 10 = 10
2 x 10 = 20
3 x 10 = 30
4 x 10 = 40
5 x 10 = 50
6 x 10 = 60
7 x 10 = 70
8 x 10 = 80
9 x 10 = 90
10 x 10 = 100
11 x 10 = 110

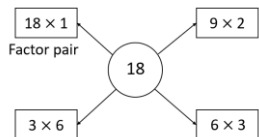
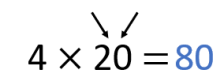
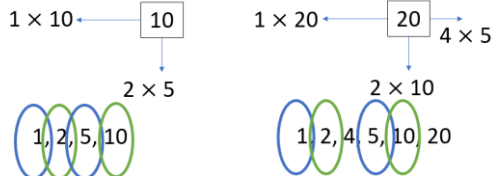
Year 3

Use multiplication and division facts for the 3, 4 and 8 multiplication tables

Write and calculate mathematical statements for multiplication and

Solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.

	<p>Multiplication is the opposite of division If I know $3 \times 4 = 12$, I know $12 \div 3 = 4$ and $12 \div 4 = 3$ These are called inverse division facts</p> <p>We can use multiplication facts to work out related facts</p> <div><div><div>1</div><div>1</div><div>1</div><div>1</div></div><div><div>10</div><div>10</div><div>10</div><div>10</div></div></div> <div><div><div>1</div><div>1</div><div>1</div><div>1</div></div><div><div>10</div><div>10</div><div>10</div><div>10</div></div></div> <div><div><div>1</div><div>1</div><div>1</div><div>1</div></div><div><div>10</div><div>10</div><div>10</div><div>10</div></div></div> <p>$3 \times 4 = 12$ $30 \times 4 = 120$</p> <p>Remainder is what is left over when we divide</p>	<p>division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods</p> <div><div><div>Tens</div><div>Ones</div></div><div><div>40</div><div>8</div></div><div><div>48</div><div>40</div><div>8</div></div><div><div><div><div><div>4</div><div>0</div></div><div><div>4</div><div>0</div></div></div><div><div>8</div><div>0</div></div></div><div><div><div>4</div><div>0</div></div><div><div>8</div><div>0</div></div></div></div><div><div>48</div><div>40</div><div>8</div></div><div><div><div><div>4</div><div>0</div></div><div><div>8</div><div>0</div></div></div><div><div>8</div><div>0</div></div></div><div><div><div>4</div><div>0</div></div><div><div>8</div><div>0</div></div></div></div> <div><div>48</div><div>40</div><div>8</div></div> <div><div><div><div>4</div><div>0</div></div><div><div>8</div><div>0</div></div></div><div><div>8</div><div>0</div></div></div> <div><div><div>4</div><div>0</div></div><div><div>8</div><div>0</div></div></div> <div><div>48</div><div>40</div><div>8</div></div> 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	<p>Factor pairs are pairs of numbers that multiply together to make a given number</p>  <p>Multiply by 0 – when one of the factors is 0, the product will always be 0 Multiply by 1 – when one of the factors is 1, the product will be the other factor Dividing by 1 – number remains the same A number divided by itself will always = 1</p> <p>Multiplication is commutative – the order doesn't matter $3 \times 4 = 4 \times 3$ Multiplying 3 numbers together – the order doesn't matter $4 \times 4 \times 5 =$  $4 \times 20 = 80$</p> <p>We can use multiplication facts to work out related facts e.g. $3 \times 4 = 12$ $30 \times 4 = 120$ $300 \times 4 = 1200$</p>	<table border="1" data-bbox="1198 199 1355 359"> <tr> <td></td><td>H</td><td>T</td><td>O</td></tr> <tr> <td></td><td>2</td><td>1</td><td>7</td></tr> <tr> <td>x</td><td></td><td></td><td>4</td></tr> <tr> <td></td><td></td><td></td><td></td></tr> <tr> <td></td><td></td><td></td><td></td></tr> </table>		H	T	O		2	1	7	x			4									
	H	T	O																				
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x			4																				
Year 5	<p>Factors = numbers that a number is divisible by without a remainder Factors can be found by working systematically Factors come in pairs Common factors = 2 or more numbers having the same factor</p>  <p>Common factors: 1, 2, 5, 10</p> <p>Multiples = the result of multiplying a number by something Multiples can be found by counting in jumps of that number or repeatedly adding the number on Common multiples = 2 or more numbers having the same multiple</p>	<p>Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers</p> <p>Establish whether a number up to 100 is prime and recall prime numbers up to 19 applying accurate vocabulary</p> <p>Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers</p>	<p>Solve multi-step problems with mixed operations applying the facts and procedures that they know</p> <p>A multipack of water contains 6 bottles of water. A box holds 3 multipacks of water. A shop orders 24 boxes of water. How many bottles of water have they ordered?</p>																				

Multiples of 6:

6, 12, 18, 24, 36, 42, 48

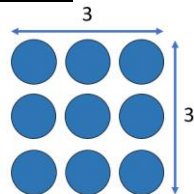
Multiples of 8:

8, 16, 24, 30, 40, 48

Prime numbers = a number with exactly 2 factors: 1 and itself

If a number is not prime, it is **composite**

Square numbers



The array makes a square

$$3 \times 3 = 9$$

The product of an integer multiplied by itself is a square number.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

$$\begin{aligned} 1^2 &= 1 \\ 2^2 &= 4 \\ 3^2 &= 9 \\ 4^2 &= 16 \\ 5^2 &= 25 \\ 6^2 &= 36 \\ 7^2 &= 49 \\ 8^2 &= 64 \\ 9^2 &= 81 \\ 10^2 &= 100 \\ 11^2 &= 121 \\ 12^2 &= 144 \end{aligned}$$

Cube numbers

2741 \times 6 becomes

$$\begin{array}{r} 2741 \\ \times 6 \\ \hline 16446 \end{array}$$

Answer: 16 446

124 \times 26 becomes

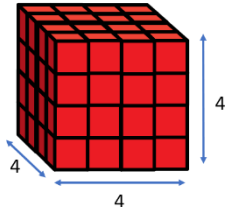
$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \end{array}$$

Answer: 3224

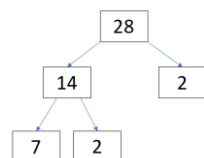
Multiply and divide numbers mentally drawing upon known facts

Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

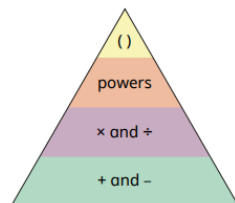
Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000

	 <p> $4 \times 4 \times 4 = 64$ 16 </p> <p> $1^3 = 1$ $2^3 = 8$ $3^3 = 27$ $4^3 = 64$ $5^3 = 125$ $6^3 = 216$ $7^3 = 343$ $8^3 = 512$ $9^3 = 729$ $10^3 = 1000$ </p> <p>The result of multiplying a number by itself and then by itself again</p>		
Year 6	<p>Factors = numbers that a number is divisible by without a remainder Factors can be found by working systematically Factors come in pairs Common factors = 2 or more numbers having the same factor</p> <p> $1 \times 10 \rightarrow 10$ $1 \times 20 \rightarrow 20$ 4×5 2×5 2×10 (1, 2, 5, 10) (1, 2, 4, 5, 10, 20) </p> <p>Common factors: 1, 2, 5, 10</p> <p>Multiples = the result of multiplying a number by something Multiples can be found by counting in jumps of that number or repeatedly adding the number on Common multiples = 2 or more numbers having the same multiple Multiples of 6: 6, 12, 18, 24, 36, 42, 48 Multiples of 8: 8, 16, 24, 30, 40, 48</p> <p>Prime numbers = a number with exactly 2 factors: 1 and itself If a number is not prime, it is composite 1 is not a prime number 2 is the only even prime number</p>	<p>Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication</p> <p>124 \times 26 becomes</p> <pre> 1 2 4 x 2 6 ----- 7 4 4 2 4 8 0 ----- 3 2 2 4 </pre> <p>Answer: 3224</p> <p>Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context</p> <p>432 \div 15 becomes</p> <pre> 2 8 15 4 3 2 3 0 0 --- 1 3 2 1 2 0 --- 1 2 </pre> <p>Answer: 28 r 12 Remainder as a fraction: $\frac{12}{15} = \frac{4}{5}$</p>	<p>Solve problems involving addition, subtraction, multiplication and division</p> <p>Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.</p> <p>Bottles of water can be bought in packs of either 6 or 9 A school needs to buy enough water for 268 pupils for Sports Day. A pack of 6 bottles costs £4 A pack of 9 bottles costs £5 Is it cheaper to buy only packs of 6 bottles or only packs of 9 bottles? How much cheaper?</p>

Prime factors = keep factorising a number until you reach **factors** that are prime numbers



When calculating with more than one operation, the **order** matters:



Divide numbers up to 4 digits by a one-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context

$$142 \div 4 = 35 \text{ r}2$$

$$\begin{array}{r} 035 \cdot 5 \\ 4 \overline{)142} \cdot 0 \end{array}$$

Perform mental calculations, including with mixed operations and large numbers

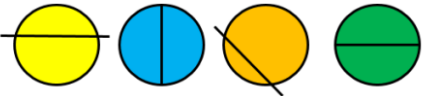
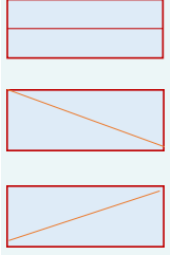



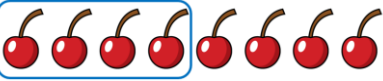
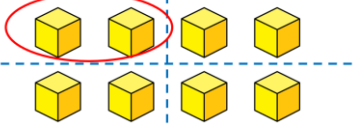
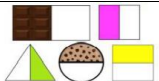




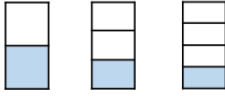
Identify common factors, common multiples and prime numbers



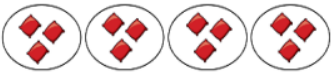
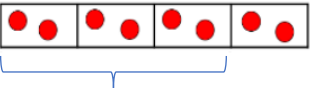


Use their knowledge of the order of operations to carry out calculations involving the four operations

Use estimation to check answers to calculations

Fractions

Progression of Knowledge	Pupil formally start to learn fractions in Year 1 where they learn the concept of a half and a quarter and how to find a half or a quarter. They widen their knowledge of different fractions in Year 2 where they explore thirds and three quarters and start to find fractions of numbers. The majority of declarative knowledge is imparted throughout lower key stage 2 where pupils learn to write, order, compare, add, subtract and find equivalences. They extend this in Year 5 and 6 where they work with fractions with different denominators and learn procedures around calculating with a range of fractions.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
EYF S	Children are not explicitly taught fractions in the early years but when exploring capacity, they refer to things being half full, full, empty and nearly empty which is a pre-fraction skill as it is building understanding of wholes and halves.		
Year 1	<p>Half = one of two equal parts Quarter = one of four equal parts Whole = all of the parts</p> <p>The parts must be equal</p>   <p>But don't have to look the same All of these represent halves of the rectangle They have 2 equal parts</p>	<p>Find half or quarter of a shape or object</p>    <p>Find half or quarter of a quantity or set of objects</p>  	Recognising simple contexts where fractions might apply e.g. Ben has lost a quarter of his sweets
Year 2	    	<p>Recognise halves, quarters and thirds What fraction is shaded in each diagram?</p> 	Solve simple problems applying the declarative and procedural knowledge from KS1

	<p>We write a half like this. $\frac{1}{2}$ 2 parts make the whole and we have 1 of them.</p> <p>We write a quarter like this. $\frac{1}{4}$ 4 parts make the whole and we have 1 of them.</p> <p>We write three quarters like this. $\frac{3}{4}$ 4 parts make the whole and we have 3 of them.</p> <p>We write a third like this. $\frac{1}{3}$ 3 parts make the whole and we have 1 of them.</p> <p>$\frac{1}{2}$ is equivalent to $\frac{2}{4}$ (same value)</p>   <p>We can find a fraction of a number by sharing it (dividing) into equal groups</p> <p>$\frac{1}{4}$ of 12 </p> <p>We can also use a bar model</p> <p>$\frac{3}{4}$ of 8 </p>	<p>Find fractions of a length, shape, set or objects or quantity.</p> <p>Circle half the cakes.</p>  <p>Shade $\frac{1}{3}$ of each shape.</p>  <p>write simple fractions for example, $\frac{1}{2}$ of 6 = 3</p> <p>$\frac{1}{2}$ of 12 = <input type="text"/> $\frac{1}{4}$ of 12 = <input type="text"/></p>	<p>I am thinking of a number.</p> <p>?</p> <p>One third of my number is 12</p> <p>Which will be greater, one half of my number or one quarter of my number?</p>
Year 3	<p>Writing fractions</p> <p>Denominator shows how many equal parts the whole has been divided into</p> <p>Numerator shows how many of those parts we have</p>	<p>Write unit and non-unit fractions</p> <p>Count in fractions on a number line</p>	<p>Solve problems involving finding a fraction of a set of objects</p>

Numerator
How many parts
are we looking at?

Denominator
How many equal
parts are there?

$\frac{1}{4}$

Unit fractions have a numerator of 1



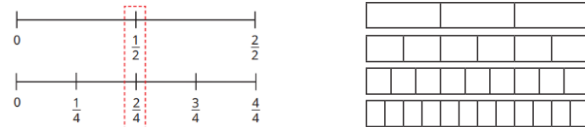
Non-unit fractions have a numerator greater than 1

They are made up of a quantity of unit fractions e.g. $\frac{1}{4} + \frac{1}{4} + \frac{1}{4} = \frac{3}{4}$



Equivalent means same value or amount

We can see these on double number lines or fraction walls



To **add and subtract fractions** with the same **denominator**, the **denominator** stays the same and you add or subtract the **numerator**.

$$\frac{1}{7} + \frac{2}{7} = \frac{3}{7}$$



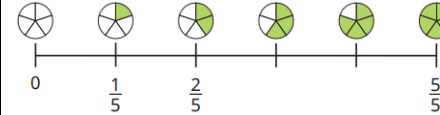
one seventh + two sevenths = three sevenths

$$\frac{5}{7} - \frac{3}{7} = \frac{2}{7}$$



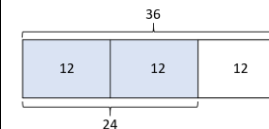
Comparing and ordering

When the **numerators** are the same, the bigger the **denominator**, the smaller the fraction. The smaller the **denominator**, the bigger the fraction.



Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators

$$\frac{2}{3} \text{ of } 36 = 24$$



recognise and show, using diagrams, equivalent fractions with small denominators

add and subtract fractions with the same denominator within one whole [for example, $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$]

compare and order unit fractions, and fractions with the same denominators

Eva has a bag of 20 sweets.



She eats $\frac{1}{4}$ of the sweets.

She gives $\frac{1}{5}$ of the sweets that are left to Dora and 2 sweets to her mum.

How many sweets does Eva have left?

Solve problems involving adding and subtracting fractions

Jack has $\frac{7}{8}$ of a chocolate bar.

He eats $\frac{4}{8}$ of the chocolate bar.



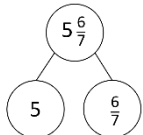

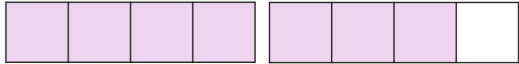
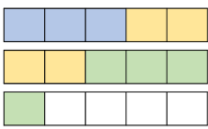

What fraction of the chocolate bar does he have left?

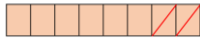

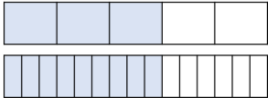
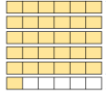

Solve problems involving comparing and ordering fractions

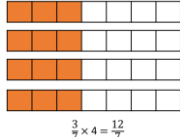
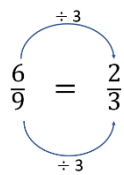
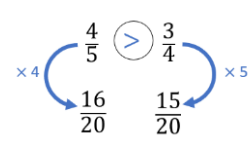
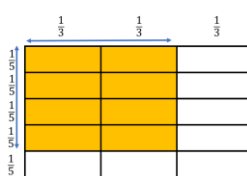
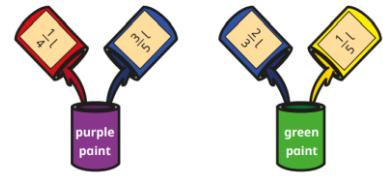
Use the digit cards to work out what the fractions could be.

You can use the digit cards more than once each time.

1 2 4 5 9 $\frac{2}{9} < \square < \square < 1$

	<p>$\frac{1}{4} < \frac{1}{3}$</p>  <p>$\frac{1}{4}$ is <u>smaller than</u> $\frac{1}{3}$</p> <p>When the denominators are the same, the bigger the numerator, the bigger the fraction. The smaller the numerator, the smaller the fraction.</p>  <p>$\frac{3}{5} < \frac{4}{5}$ $\frac{6}{7} > \frac{2}{7}$</p>	
Year 4	<p>Equivalent fractions can be found by multiplying or dividing both the numerator and denominator by the same amount</p>  <p>Mixed numbers are made up of whole numbers and a fraction Improper fractions will have a numerator greater than a denominator</p>  <p>It can be written as either</p>  <p>$\frac{7}{4}$ $1\frac{3}{4}$</p> <p>Recognise and show, using diagrams, families of common equivalent fractions</p> <p>Count in fractions beyond 1</p> <p>Calculate fractions of amounts with non-unit fractions and larger numbers</p> <p>Convert between improper fractions and mixed numbers</p> <p>Add and subtract fractions with the same denominator – the answer may exceed 1 whole</p> <p>$\frac{3}{5} + \frac{4}{5} + \frac{4}{5} = \frac{11}{5} = 2\frac{1}{5}$</p>  <p>Subtract from the whole</p>	<p>solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number</p> <p>solve problems involving adding and subtracting fractions, including answers greater than one whole and subtracting from the whole</p> <p>A chocolate bar has been split into 10 equal parts.</p>  <p>Rosie eats $\frac{3}{10}$ of the bar.</p> <p>Dexter eats $\frac{1}{10}$ of the bar more than Rosie.</p> <p>What fraction of the chocolate bar is left?</p>

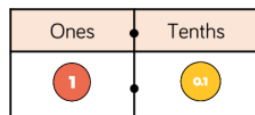
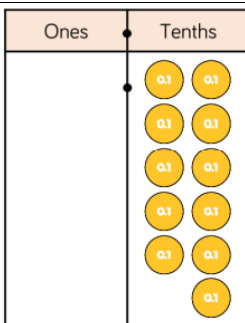
		$\frac{8}{8} - \frac{2}{8} = \frac{6}{8}$  <p>Subtract from a mixed number</p> $2\frac{4}{8} - \frac{7}{8} = 1\frac{5}{8}$ 	
Year 5	<p>To find an equivalent fraction, we can multiply the numerator and denominator by the same number.</p>  $\frac{3}{5} = \frac{9}{15}$ <p>To add, subtract, compare and order fractions, the denominators must be the same.</p> <p>When the denominators are multiples of each other, we can find the equivalent fraction</p> $\frac{1}{3} + \frac{1}{9} = \frac{4}{9}$ <p>x 3</p> $\frac{3}{9} + \frac{1}{9} = \frac{4}{9}$ <p>Multiplying fractions is the same as repeated addition e.g. $\frac{3}{4} \times 3$ is the same as $\frac{3}{4} + \frac{3}{4} + \frac{3}{4}$</p>	<p>identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths</p> <p>Find a common denominator</p> <p>compare and order fractions whose denominators are all multiples of the same number</p> <p>recognise mixed numbers and improper fractions and convert from one form to the other</p> $5\frac{1}{6} = \frac{31}{6}$  $5 \times \frac{6}{6} = \frac{30}{6}$ $\frac{30}{6} + \frac{1}{6} = \frac{31}{6}$ <p>add and subtract fractions with the same denominator and denominators that are multiples of the same number</p> <p>multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams</p>	<p>Solve a range of problems involving all procedural knowledge, including two-step problems</p> <p>On Saturday, Alex cycles for $\frac{2}{3}$ of an hour.</p> <p>On Sunday, she cycles for $\frac{5}{12}$ of an hour.</p> <p>a) How many more hours does Alex cycle on Saturday than Sunday?</p> 

		 $\frac{3}{4} \times 4 = \frac{12}{4}$																					
Year 6	<p>Simplifying fractions means finding an equivalent fraction with smaller numbers to make it easier to work with To simplify, we divide the numerator and denominator by the same factor</p> <p>If a fraction cannot be simplified any further, it is in its simplest form</p> <p><u>Finding a common denominator</u> Fractions are easier to order, compare, add and subtract if they have the same denominator. To express fractions in the same denominator:</p> <ul style="list-style-type: none"> • See if one is a multiple of the other • Find the lowest common multiple • Multiply the denominators together <p>Whatever you do to the denominator, you must do to the numerator to ensure that it is equivalent</p>  	<p>use common factors to simplify fractions</p> <p>use common multiples to express fractions in the same denominator</p> <p>compare and order fractions, including fractions > 1</p> <p>add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions</p> <p>multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$]</p>  <p>divide proper fractions by whole numbers [for example, $\frac{1}{3} \div 2 = \frac{1}{6}$]</p>	<p>Solve multi-step and non-straightforward problems involving multiplying, dividing, adding and subtracting fractions – including mixed numbers and different denominators</p> <p>A painter uses the following mixtures. How much more green paint does she have than purple paint?</p>  <table border="1"> <tbody> <tr> <td>$1\frac{1}{4}$</td> <td></td> <td>$\frac{1}{4}$</td> <td>$= 3\frac{3}{5}$</td> </tr> <tr> <td>$\frac{1}{25}$</td> <td>$1\frac{3}{20}$</td> <td></td> <td>$= 3\frac{39}{100}$</td> </tr> <tr> <td></td> <td>$1\frac{1}{50}$</td> <td>$1\frac{3}{100}$</td> <td>$= 5\frac{9}{20}$</td> </tr> <tr> <td>$=$</td> <td>$=$</td> <td>$=$</td> <td></td> </tr> <tr> <td><input type="text"/></td> <td><input type="text"/></td> <td><input type="text"/></td> <td></td> </tr> </tbody> </table>	$1\frac{1}{4}$		$\frac{1}{4}$	$= 3\frac{3}{5}$	$\frac{1}{25}$	$1\frac{3}{20}$		$= 3\frac{39}{100}$		$1\frac{1}{50}$	$1\frac{3}{100}$	$= 5\frac{9}{20}$	$=$	$=$	$=$		<input type="text"/>	<input type="text"/>	<input type="text"/>	
$1\frac{1}{4}$		$\frac{1}{4}$	$= 3\frac{3}{5}$																				
$\frac{1}{25}$	$1\frac{3}{20}$		$= 3\frac{39}{100}$																				
	$1\frac{1}{50}$	$1\frac{3}{100}$	$= 5\frac{9}{20}$																				
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Decimals and Percentages

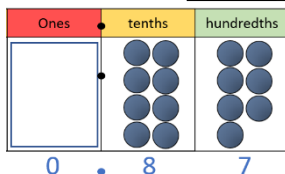
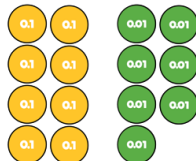
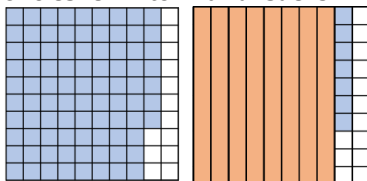
Progression of Knowledge	Children are introduced to decimals in Year 3 once they have a firm understanding of whole numbers in the number system. They start by exploring tenths and relating fractions to decimals. During Year 4, children are introduced to hundredths and gain some depth of understanding regarding the place value of decimals and how to manipulate them to divide by 10 and 100, round, order and compare. They then apply this to decimal notation in Money in Year 4. At the start of Upper Key Stage 2, children are introduced to thousandths and look at ways of calculating using decimals. They start to explore the link between fractions, decimals and percentages which is built upon in Year 6 along with confidence in using all 4 operations with decimals and exploring problem solving and conditional knowledge linked to decimals.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'																										
Year 3	<p>Tenths arise from dividing one whole into ten equal parts Tenths can be written as fractions or as decimals</p> <div><div><div>$\frac{4}{10}$</div></div><div><table><tr><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td></tr></table><div>4 tenths</div><table><tr><td>0.1</td><td>0.1</td><td>0.1</td><td>0.1</td><td>0.1</td><td>0.1</td><td>0.1</td><td>0.1</td><td>0.1</td><td>0.1</td></tr></table><div>0.4</div></div></div> <p>Ten tenths = one</p> <p>After the ones column, is a decimal point and then the tenths column</p> <table><tr><td>Ones</td><td></td><td>Tenths</td></tr><tr><td>0</td><td></td><td>8</td></tr></table>	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	Ones		Tenths	0		8	<p>Counting up and down in tenths, crossing the decimal point</p> <p>Express tenths as decimals and fractions</p>	
$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$																				
0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1																				
Ones		Tenths																											
0		8																											
Year 4	<p>Ten tenths = one Can be exchanged between columns</p>	<p>Express tenths and hundredths as decimals and fractions</p>	<p>Solve money and measure problems using decimals to 2 decimal places</p>																										



The **tenths** column is ten times smaller than the ones column
When dividing by ten, the number is split into ten equal parts and is ten times smaller so we can move the digits down one column.

Hundredths arise from dividing one whole into one hundred parts
One **tenth** = ten **hundredths**



Hundredths can be written as **tenths** and **hundredths** and using the two place value columns after the **decimal point**.

Fraction	Decimal
$\frac{91}{100}$	0.91
Fraction	Decimal
$\frac{9}{100}$	0.09

They can be written as **fractions**.
Parts of one hundred

Dividing one- and two-digit numbers by 10

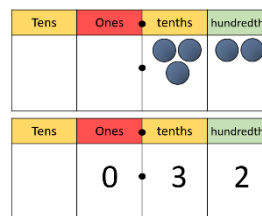
$$32 \div 10 = 3.2$$



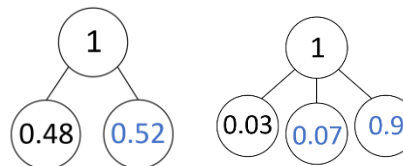
Counting up and down in hundredths

Dividing one- and two-digit numbers by 100

$$32 \div 100 =$$

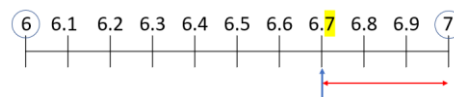


Use bonds to 100 to make one whole using tenths and hundredths



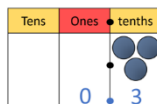
Compare and order numbers with the same number of decimal places (up to hundredths)

Round decimals with one decimal place to the nearest whole numbers



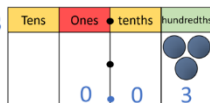
Dividing by 100 is the same as dividing by ten and then dividing by ten again.

$$3 \div 10 = 0.3$$



Move the digits down 2 place value columns to make a number 100 times smaller

$$3 \div 100 = 0.03$$

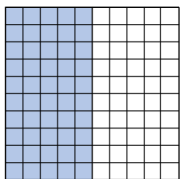


To **round decimals** to the nearest **whole number**, look at the digit in the **tenths** column to decide whether to round up or not.

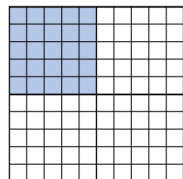
5,6,7,8,9 – **rounds up** to the next whole number

0,1,2,3,4 – **rounds down** to the whole number before

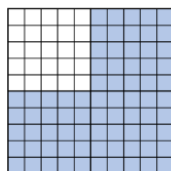
Halves and **quarters** can be written as **decimals**



$$\frac{1}{2} = \frac{5}{10} = \frac{50}{100} = 0.5$$



$$\frac{1}{4} = \frac{25}{100} = 0.25$$



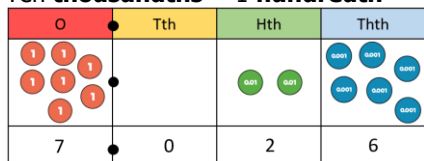
$$\frac{3}{4} = \frac{75}{100} = 0.75$$

Year 5

One **thousandth** = 1 whole split into 1000 parts

It is the columns after **hundredths**

Ten **thousandths** = 1 **hundredth**



Thousandths can be expressed as **fractions** and **decimals**

Order and compare decimals with up to 3 decimal places, including with different decimal places

Tens	Ones	Tth	Hth
7	6	3	
3	5	0	3
7	6	4	1

Round decimals to the nearest whole number

Solve 1 and 2 step problems involving adding and subtracting decimals up to 3 decimal places.

Solve problems involving multiplying and dividing by 10, 100 and 1000

O	Tth	Hth	Thth
	0.1 0.1	0.01 0.01	0.001 0.001
	0.01 0.01	0.001 0.001	0.0001 0.0001
			0.00001 0.00001

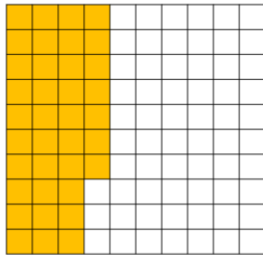
$$\frac{83}{1000}$$

0.253

Per cent = number of parts per hundred

We use this symbol to represent **percentages %**

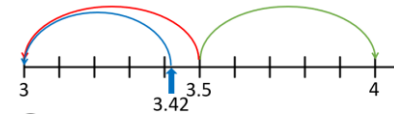
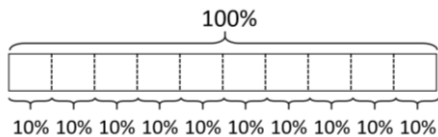
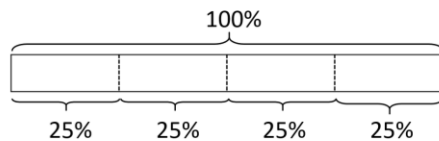
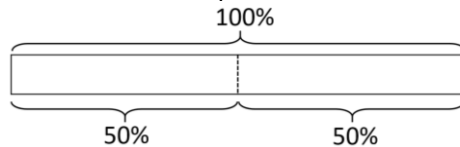
If the whole is split into 100 equal parts, each part is worth 1%



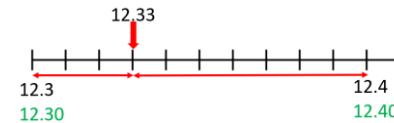
There are $\frac{37}{100}$ parts out of a hundred shaded.
This is $\frac{37}{100}$ %

Percentages can be written as fractions with a denominator of 100

We can use some equivalent fractions to see **percentages**



Round decimals to the nearest tenth



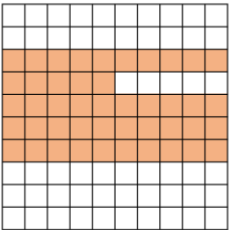
Express percentages as decimals and fractions

Add and subtract decimals with the same and a different number of decimal places including crossing the whole

$$\begin{array}{r} 3 \ 2 \ . \ 8 \\ + \ 1 \ . \ 2 \ 7 \\ \hline 3 \ 4 \ . \ 0 \ 7 \\ 1 \end{array}$$

decimal place value
is essential

Multiply and divide decimals by 10, 100 and 1000

	<p>Percentages can be written as decimals – using the tenths and hundredths column as the percentage out of 100.</p> <p>We can represent the same values as fractions, decimals and percentages – they are all ways of representing part of a whole</p>  <p>45 out of 100 $\frac{45}{100} = 45\% = 0.45$</p> <p>When calculating with decimals, we use the same methods as whole numbers but apply what we know about decimal place value</p> <table border="1" data-bbox="376 775 524 892"> <tr><td>3</td><td>2</td><td>8</td><td></td></tr> <tr><td>+</td><td></td><td>1</td><td>2</td></tr> <tr><td></td><td></td><td></td><td>7</td></tr> <tr><td>3</td><td>4</td><td>0</td><td>7</td></tr> <tr><td></td><td></td><td></td><td>1</td></tr> </table> <p>Empty columns can be filled with a zero as a place holder</p> <p>We use decimal place value to multiply and divide by 10, 100 and 1000</p> <p>Multiplied by 10 = move one place to the left Multiplied by 100 = move two places to the left Multiplied by 1000 = move 3 places to the left Divided by 10 = move one place to the right Divided by 100 = move two places to the right Divided by 1000 = move three places to the right</p>	3	2	8		+		1	2				7	3	4	0	7				1		
3	2	8																					
+		1	2																				
			7																				
3	4	0	7																				
			1																				
Year 6	<p>Multiplying decimals is the same methods as multiplying whole numbers but the place value is different</p>	<p>Calculate all four operations using decimals</p> <p>Express remainders as decimals</p> <p>Express fractions, decimals and percentages as representations of each other</p>	<p>Solve multi-step problems involving adding, subtracting, multiplying and dividing decimals in context</p> <p>Recognising multiplicative and division structures and applying procedural knowledge of decimals</p>																				

$$\begin{array}{r} 21.3 \\ \times 4 \\ \hline 85.2 \end{array}$$

$$\begin{array}{r} 21.3 \\ \times 4 \\ \hline 85.2 \end{array}$$

However many **decimal places** there are in the number that you are multiplying, there will be that many in the **product**.

Dividing decimals is the same methods as dividing whole numbers but the place value is different

$$\begin{array}{r} 1.32 \\ 4 \overline{) 5.28} \end{array}$$

When dividing, **remainders** can be expressed as decimals by showing empty tenths/ hundredths columns as appropriate

$$\begin{array}{r} 0.875 \\ 8 \overline{) 7.000} \end{array}$$

To find a fraction as a **percentage**, we would find an **equivalent fraction** in **hundredths** to find the parts per hundred

$$\frac{3}{5} = \frac{60}{100} = 60\%$$

Equivalent fractions, decimals and percentages
Tenths and hundredths using place value, also:

Fraction	Decimal	Percentage
$\frac{1}{2}$	0.5	50%
$\frac{1}{4}$ $\frac{3}{4}$	0.25 0.75	25% 75%
$\frac{1}{3}$ $\frac{2}{3}$	0.33 0.66	33% 66%
$\frac{1}{5}$ $\frac{2}{5}$ $\frac{3}{5}$ $\frac{4}{5}$	0.2 0.4 0.6 0.8	20% 40% 60% 80%

Order fractions, decimals and percentages

Find a percentage of an amount

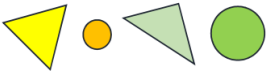

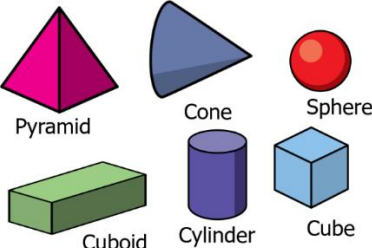

Solve problems involving percentages, including finding the whole

Solve multistep problems involving fractions, decimals and percentages

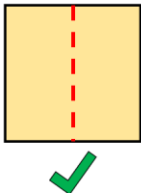
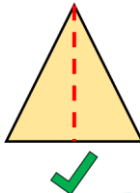
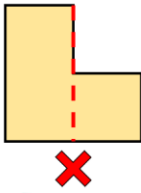
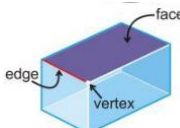


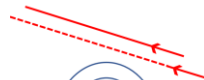

	<p>Percentages of amounts:</p> <p>To find 50%, divide by 2 because $50\% = \frac{1}{2}$</p> <p>To find 25%, divide by 4 because $25\% = \frac{1}{4}$</p> <p>To find 10%, divide by 10 because $10\% = \frac{1}{10}$</p> <p>To find 1%, divide by 100 because $1\% = \frac{1}{100}$</p> <p>To find 5%, divide by 10 and then halve it</p> <p>To find any multiple of 10%, find 10% then multiply by that number.</p> <p>10% of 120 = 12</p> <p>20% of 120 = 24</p> <p>To find any multiple of 1%, find 1% then multiply by that number.</p> <p>To find any percentage, partition it, find the parts and recombine it.</p>		
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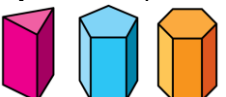
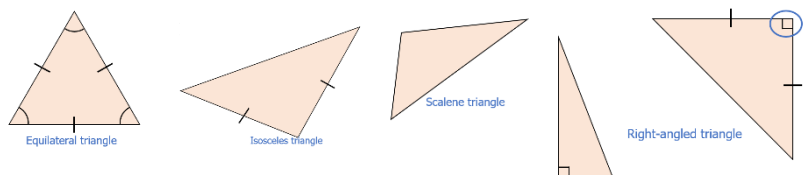
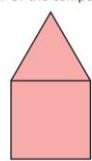
Shape and Pattern

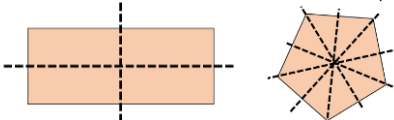
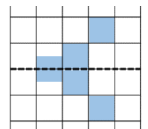
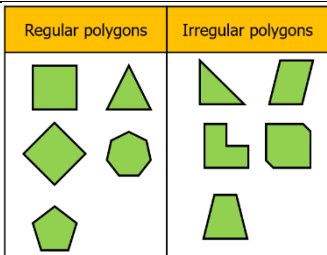
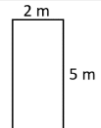
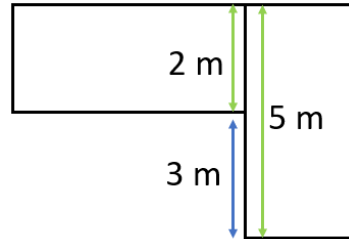
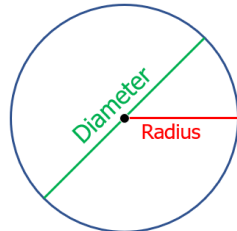
Progression of Knowledge	Shape knowledge features heavily in the Early Years curriculum and pupils enter Year 1 with an awareness of shape names. Throughout KS1 they learn to describe them with accuracy and during KS2, they are exposed to more complicated shapes and learn the procedures of geometry and classification. At all stages, pupils solve problems to apply their knowledge.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
EYF S	<p>Circles have one curved side Triangles have 3 straight sides</p>  <p>Squares and rectangles have 4 straight sides and 4 corners</p>  <p>3D shapes</p>  <p>Pyramid Cone Sphere Cuboid Cylinder Cube</p> <p>Patterns can use shapes and colours to repeat</p> 	<p>Copy, continue and create their own simple repeating patterns with at least three full units of repeat. AB, ABB, AABB, AAB, AABBB</p> <p>Including a range of shapes, colours and sizes</p> <p>Recall names for 2D shapes</p> <p>Recall some names for 3D shapes</p> <p>Explore which 3D shapes stack and roll</p>	<p>Use what children know to explore situations and challenges e.g we need to build a tower for Rapunzel, which 3D shapes would be best and why?</p> <p>Pose problems to discuss relating to patterns e.g. this repeating pattern is all muddled up, can you help to sort it out?</p>

<p>Year 1</p>	<div data-bbox="309 212 674 363"> </div> <div data-bbox="712 268 925 296"> <p>Triangles – 3 sides</p> </div> <div data-bbox="309 379 674 531"> </div> <div data-bbox="712 427 846 456"> <p>Rectangles</p> </div> <div data-bbox="309 547 674 699"> </div> <div data-bbox="712 638 1014 667"> <p>Squares – 4 sides the same</p> </div> <div data-bbox="309 722 674 874"> </div> <div data-bbox="712 798 790 826"> <p>Circles</p> </div> <div data-bbox="320 914 723 1193"> <div data-bbox="331 1026 421 1074">Pyramid</div> <div data-bbox="521 1026 577 1058">Cone</div> <div data-bbox="656 1026 723 1058">Sphere</div> <div data-bbox="331 1090 477 1169">Cuboid</div> <div data-bbox="521 1090 600 1169">Cylinder</div> <div data-bbox="656 1090 701 1169">Cube</div> </div>	<p>Recognise, name and sort 2D shapes in different orientations and different sizes</p> <p>Recognise, name and sort 3D shapes</p> <p>Describe and repeat patterns using 2D and 3D shapes</p>	<p>Using knowledge of shapes and descriptions to explore and solve simple problems e.g. my shape rolls what could it be?</p>
<p>Year 2</p>	<div data-bbox="297 1233 510 1265"> <p>2D shapes are flat</p> </div> <div data-bbox="320 1281 723 1509"> <div data-bbox="342 1361 376 1377">Square</div> <div data-bbox="499 1361 533 1377">Rectangle</div> <div data-bbox="656 1361 689 1377">Triangle</div> <div data-bbox="342 1489 376 1505">Circle</div> <div data-bbox="432 1489 465 1505">Pentagon</div> <div data-bbox="566 1489 600 1505">Hexagon</div> <div data-bbox="656 1489 689 1505">Octagon</div> </div> <div data-bbox="835 1233 1081 1265"> <p>3D shapes are not flat</p> </div> <div data-bbox="824 1265 1171 1509"> <div data-bbox="857 1345 925 1377">Pyramid</div> <div data-bbox="958 1345 1003 1377">Cube</div> <div data-bbox="1037 1345 1081 1377">Sphere</div> <div data-bbox="1104 1345 1149 1377">Cylinder</div> <div data-bbox="824 1473 969 1505">Triangular Prism</div> <div data-bbox="992 1473 1070 1505">Cuboid</div> <div data-bbox="1081 1473 1126 1505">Cone</div> </div>	<p>Identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line</p>	<p>Work out which shape has been described by visualising, including visualising new shapes e.g. I have placed a triangle on top of a square</p>

	<p>We can describe 2D shapes by:</p> <ul style="list-style-type: none">the number of sidesthe number of vertices (corners)If they have a line of symmetry <p>A shape is symmetrical if both sides of the line are equal – the line is called a line of symmetry</p> <div><div></div><div></div><div></div></div> <p>We can fold a shape to see if it is symmetrical</p> <p>We can describe 3D shapes by:</p> <ul style="list-style-type: none">the number of facesthe number of verticesthe number of edges <div></div> <p>We can see 2D shapes on the faces of 3D shapes</p>	<p>Identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces</p> <p>Identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid]</p> <p>Compare and sort common 2-D and 3-D shapes and everyday objects.</p> <p>Make patterns with 2D and 3D shapes</p>	<p>to make a new shape, how many vertices does it have?</p> <p>Applying procedural knowledge to consider the odd one out or how a group of shapes have been sorted</p>									
Year 3	<p>Horizontal line  across</p> <p>Vertical line  down</p> <p>Parallel lines – always the same distance apart. They will never meet</p> <div></div> <p>Perpendicular lines – meet at right angles</p> <div></div>	<p>Identify horizontal and vertical lines and pairs of perpendicular and parallel lines.</p> <p>Draw 2D shapes</p> <p>Make 3D shapes using modelling materials</p> <p>Recognise 3D shapes in different orientations and describe them</p>	<p>Use knowledge and procedures to sort shapes based on multiple criteria</p> <p>Sort a selection of 3-D shapes using the criteria in the table.</p> <table><tr><th></th><th>At least one triangular face</th><th>No triangular faces</th></tr><tr><td>Prism</td><td></td><td></td></tr><tr><td>Not a prism</td><td></td><td></td></tr></table>		At least one triangular face	No triangular faces	Prism			Not a prism		
	At least one triangular face	No triangular faces										
Prism												
Not a prism												

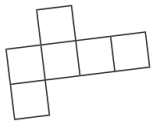
	 <p>Shapes are still the same shape even if in different orientations</p>  <p>A prism is any 3D shape where the same 2D face is joined by rectangles</p> 		
Year 4	<p>Triangle is a 3 sided shape – there are different types</p> <p>Equilateral = all 3 sides are equal length and all 3 angles are equal size</p> <p>Isosceles = 2 sides have equal length and 2 angles are equal size</p> <p>Scalene = no equal sides or angles</p> <p>Right angled triangle = one angle is a right angle. Could be scalene or isosceles.</p>  <p>Quadrilateral = 2D closed shape with 4 straight sides</p> <div style="display: flex; flex-wrap: wrap;"> <div style="width: 50%;"> <p>Rectangle</p> <p>2 pairs of parallel sides</p> <p>2 pairs of equal sides</p> <p>All angles equal (all right angles)</p> </div> <div style="width: 50%;"> <p>Square</p> <p>2 pairs of parallel sides</p> <p>All sides are equal</p> <p>All angles equal (all right angles)</p> <p>All squares are rectangles.</p> </div> <div style="width: 50%;"> <p>Trapezium</p> <p>1 pair of parallel sides</p> </div> <div style="width: 50%;"> <p>Rhombus</p> <p>2 pairs of parallel sides</p> <p>All sides are equal</p> </div> <div style="width: 50%;"> <p>Parallelogram</p> <p>Opposite angles are equal</p> <p>2 pairs of parallel sides</p> <p>2 pairs of equal sides</p> </div> </div>	<p>Compare and classify geometric shapes based on their properties and size</p> <p>Identify lines of symmetry in 2D shapes presented in different orientations</p> <p>Complete a simple symmetric figure with respect to a line of symmetry</p>	<p>Solve problems involving applying knowledge and procedures of shapes learnt so far, including applying knowledge from other sequences of learning like measurement e.g. involving properties of triangles and quadrilaterals</p> <p>The diagram shows an equilateral triangle and a square. The perimeter of the square is 100 cm. Work out the perimeter of the compound shape.</p> 

	<p>Shapes can have more than one line of symmetry</p>  <p>Patterns can have lines of symmetry as long as it is a reflection</p> 		
Year 5	<p>Polygon = closed shape made of straight lines</p> <p>Regular polygon:</p> <ul style="list-style-type: none"> all sides equal in length all interior angles the same size <p>If this is not the case, it is an irregular polygon</p>  <p>Rectangles will always have 4 right angles and opposite sides will be equal in length</p> 	<p>Identify 3D shapes from 2D representations</p> <p>Distinguish between regular and irregular polygons</p>	<p>Use knowledge about rectangles to work out missing sides and angles</p> 
Year 6	<p>Circumference = measurement around the edge of a circle</p> <p>Diameter is twice the radius</p> <p>Centre of the circle is called the origin</p> $\text{Radius} = \frac{\text{diameter}}{2}$ $\text{Diameter} = \text{radius} \times 2$ <p>A net is a 3D shape unfolded. From this, we can see the 2D shapes on each of its faces</p> 	<p>Compare and classify shapes based on properties and sizes.</p> <p>Calculate the diameter and radius and vice versa, given the other</p> <p>Draw shapes accurately using a ruler and protractor</p>	<p>Solve problems involving all shape knowledge and applying understanding of properties of shapes to find missing lengths, angles and dimensions</p> <p>Solve problems involving nets of 3D shapes and visualising constructions</p>

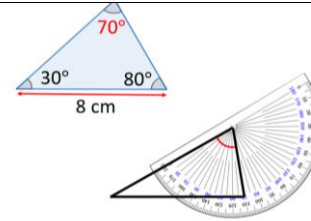
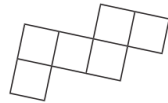
Shape	Name	Net
	Cone	
	Cuboid	
	Cube	
	Triangular prism	
	Cylinder	
	Tetrahedron	
	Square based pyramid	

Different **nets** can make the same **3D shapes** if they will fold up

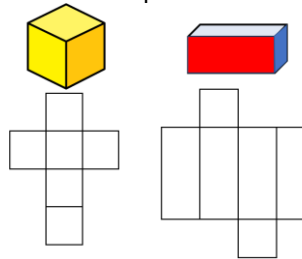
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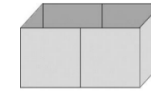
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Recognise, describe and draw
nets of 3D shapes

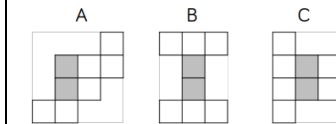


Here is an open box.



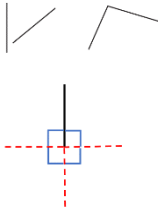

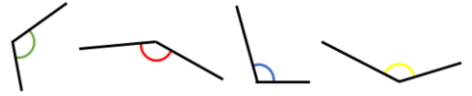
Which of the nets will fold together to
make the box?

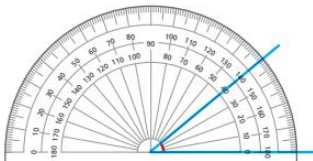
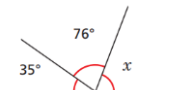
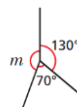


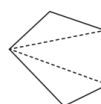
The grey squares show the base.



Angles

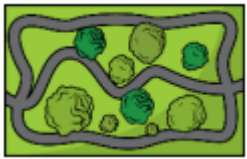
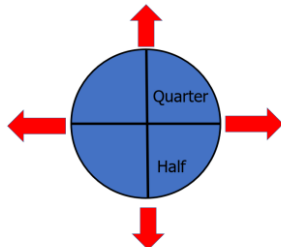
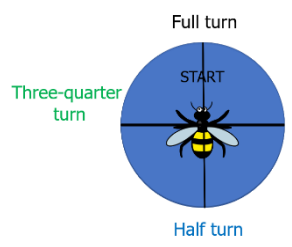
Progression of Knowledge	<p>Children are introduced to the concept of an angle in the Year 3 Maths curriculum. Throughout KS1, children have developed their knowledge of polygons and turns in preparation for introduction to angles in KS2.</p> <p>Children start by learning the concept of an angle and the different types and facts around this area. They learn the procedures for working with angles as they progress throughout KS2.</p> <p>It is only in UKS2 that children start to deploy this into problem solving and familiarise with the conditions where these facts and procedures are useful.</p>
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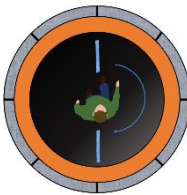
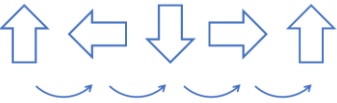

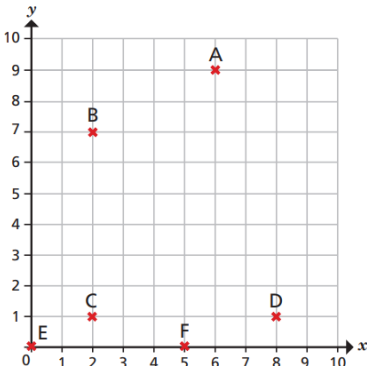
	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
Year 3	<p>An angle is where 2 straight lines meet</p> <p>A right angle is a quarter turn</p> <p>There are 2 right angles in a half turn</p> <p>There are 3 right angles in a 3 quarter turn</p> <p>There are 4 right angles in a full turn</p> <p>Angles are measured in degrees</p> <p>A right angle is 90 degrees</p> <p>A straight line is 180 degrees</p> 	Identifying right angles, acute and obtuse angles	
Year 4	<p>An acute angle is smaller than 90 degrees</p>  <p>An obtuse angle is greater than 90 degrees but smaller than 180 degrees</p> 	Comparing angles and ordering by size	
Year 5	<p>A reflex angle is greater than 180 degrees but less than 360 degrees</p> <p>A protractor (angle measurer) can be used to draw and measure angles</p>	<p>Measuring angles using a protractor</p> <p>Drawing angles using a protractor</p>	Applying facts and procedures to find missing angles on a straight line and around a point.

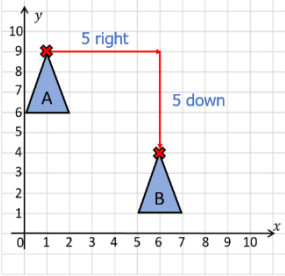
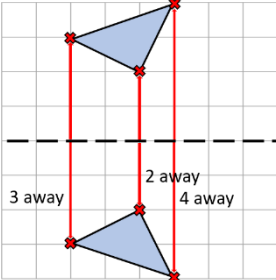
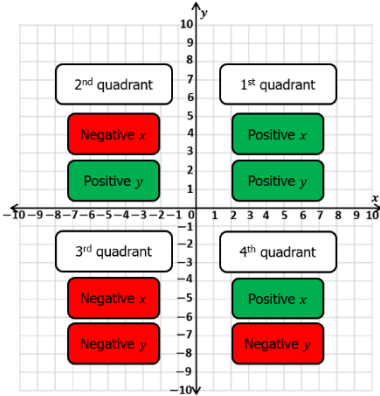
	<div></div> <p>Angles on a straight line will always add up to 180 degrees</p> <div></div> <p>Angles around a point will always add up to 360 degrees</p> <div></div>	Finding missing angles on a straight line and around a point									
Year 6	<p>Where two straight lines cross, the angles opposite each other are called vertically opposite. Vertically opposite angles will always be equal</p> <div></div> <p>Interior angles are the angles inside a polygon. Interior angles of a triangle will equal 180 degrees Interior angles of a quadrilateral will equal 360 degrees</p> <div></div> <p>To find the sum of interior angles of a polygon, split it into the smallest number of triangles x 180 degrees.</p>	<p>Find missing angles in triangles and quadrilaterals</p> <p>Finding the interior angles of a regular polygon</p> <div></div> <table><tr><td>number of sides =</td><td>5</td></tr><tr><td>number of triangles =</td><td>3</td></tr><tr><td>$3 \times 180 =$</td><td>540</td></tr><tr><td>The sum of the interior angles of a pentagon is</td><td>540°</td></tr></table>	number of sides =	5	number of triangles =	3	$3 \times 180 =$	540	The sum of the interior angles of a pentagon is	540°	Applying facts and procedures to find missing angles inside quadrilaterals, triangles and regular polygons and solve problems with more than one missing angle.
number of sides =	5										
number of triangles =	3										
$3 \times 180 =$	540										
The sum of the interior angles of a pentagon is	540°										

Position and Direction

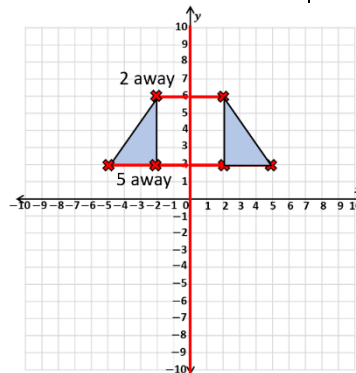
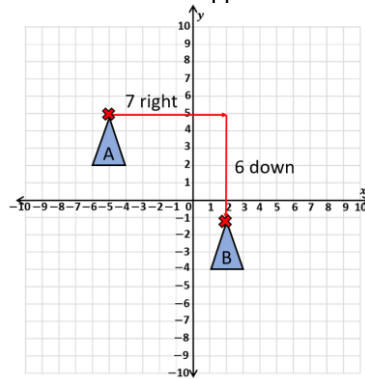
Progression of Knowledge	This unit of learning comes AFTER the fractions sequence of learning in Year 1 so that children have deep knowledge of the concept of a half and a quarter before applying this to half and quarter-turns. It also comes BEFORE the time sequence of learning in Year 1 as it gives children a deep understanding of quarters and halves as a 360 turn so that they can then see this on a clock face and apply this to half and quarter past. During year 3, no new declarative knowledge is acquired but the ability to consolidate and apply the knowledge from Key Stage 1 is practised alongside linking this to the learning of angles. Throughout the rest of Key Stage 2, pupils start to develop their understanding of coordinates on the first quadrant and translation and reflection before moving to all 4 quadrants in Year 6.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
EYFS	<p>Words can be used to describe where things are: on, next to, over, under, around, through, above, below</p> <p>We can use maps to show where places are</p> 	<p>Respond to positional language in practical situations e.g. when tidying up, put the blocks next to the beads.</p> <p>Begin to use positional language to describe where things are in relation to each other</p>	
Year 1	<p>A turn is to rotate about a point.</p>   <p>Position is where something is. Left, right, above, below and in between can be used to describe position. Direction is where something is going. Left, right, forwards and backwards can be used to describe direction.</p>	<p>Describing positions using mathematical language</p> <p>Describing directions using mathematical language</p> <p>Describing movement as turns including half, quarter and three-quarter turns</p>	

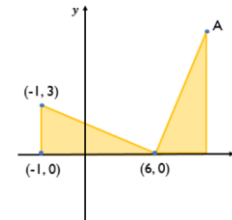
Year 2	<p>Positions on a grid can be described using left, right, up and down. Turns can go in different directions. Clockwise is to your right (like the hands of a clock move)</p>  <p>Anti-clockwise is to your left</p>	<p>Describing patterns using position and direction language</p>  <p>Anti-clockwise A quarter turn</p> <p>Continuing patterns that apply the rules Ordering and arranging objects in patterns and sequences</p>	Applying facts and procedures to continue patterns of mathematical objects in a sequence.
Year 3	<p>Direction and size of turns can be combined to describe movements. Different descriptions of turns can get you to the same position.</p>  <p>e.g – the crab turns to face the shell. It could have done.. A quarter turn anti-clockwise OR A three-quarter turn</p> <p>clockwise</p>	Recognising angles as a description of a turn	
Year 4	<p>The coordinates going horizontally are the x coordinates. The coordinates going vertically are the y coordinates. Coordinates are written (x,y) Translation is a movement on a grid Points and shapes can move combinations of up, down, left and right. E.g. 4 up, 2 left The shape will not change if being translated, just move.</p> 	<p>Efficient and accurate methods for first quadrant grid construction.</p> <p>Plotting points and describing the position as coordinates in the first quadrant.</p> <p>Describing movements between positions as translations of a given unit to the left/right and up/down</p> <p>Plotting points and drawing sides to complete a given polygon.</p>	

<p>Year 5</p>	<p>Translation is the movement of a shape on a grid.</p> <p>The language up, down, left and right can describe a translation.</p> <p>When translating a shape, choose just one point.</p>  <p>Reflection uses the axis as a mirror line. It is like a line of symmetry.</p> <p>To reflect a shape, count how many squares away from the mirror line each point is to plot the points.</p> <p>It can be checked using a mirror</p>  <p>Translation the shape doesn't change, just moves. Reflection the shape will look the opposite of the original.</p>	<p>Identifying whether a movement is a reflection or a translation</p> <p>Describing the position of a shape following a reflection or translation using the appropriate language</p> <p>Representing shapes that have been translated or reflected</p>	
<p>Year 6</p>	<p>A coordinate grid has 4 quadrants</p> <p>The middle (0) is called the origin</p> <p>Negative numbers are used</p> <p>Coordinates are still written as (x,y)</p> 	<p>Efficient and accurate methods for coordinate geometry in all 4 quadrants.</p> <p>Describing positions and plotting of coordinate points in all 4 quadrants</p> <p>Translating simple shapes on the coordinate plane</p> <p>Reflecting simple shapes in the axes of the coordinate plane</p>	<p>Applying facts and procedures to find missing coordinate points by labelling the axes and applying other geometrical knowledge. E.g.</p>

The same knowledge and procedures of **translation** and **reflection** can be applied to all **four quadrants**








The diagram shows two identical triangles.
The coordinates of three points are shown.
Find the coordinates of point A.




Money

Progression of Knowledge	Children are introduced to Money in Year 1 where they learn the core knowledge of the purpose of money and what the coins and notes represent. They are then introduced to the symbols in Year 2 and start to combine amounts of pounds and pence to find totals, but do not cross over the threshold of pence to pounds at this stage. This is learnt in Year 3 where children start to convert money and apply the equivalence of pence to pounds. Knowledge of decimals acquired in Year 4 is applied to this area of Maths where pupils learn to express amounts of money using decimal notion, which they then calculate with in Year 5. There is no new declarative knowledge relating to money covered in Upper Key Stage 2. During this phase, pupils refine their procedural knowledge and develop their conditional knowledge in a range of contexts and drawing upon a range of strategies.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
EYFS	Money is not explicitly taught in EYFS but children will still explore coins within provision to familiarise the concept of money being used to pay for things. Children may count 1p coins but not others as they are still learning to understand the concept of unitising.		
Year 1	<p>Money is used to buy and pay for things Money comes in coins and notes – different ones have different values In England, we use pounds and pence These coins represent pence:</p>  <p>These coins represent pounds:</p>  <p>These notes represent pounds:</p> 	<p>Recognising coins and notes</p> <p>Determining which coins have greater value</p> <p>Using knowledge of counting in ones, fives and tens to count coins</p>	

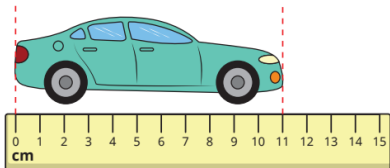





Year 2	<p>Different coins can be combined to make a value of money Coins and notes can be combined to make a value of money £ = symbol for pounds p = symbol for pence Combined amounts can be written with both e.g. £2 and 23p</p>  <p>100p = £1 Different combinations of coins can be used to make the same amount. Change = the amount remaining when you spend some money</p>	<p>Using knowledge of counting in multiples and adding to determine the value of an amount of coins (will not cross over to a pound at this stage but could be combined pounds and pence)</p> <p>Finding different combinations of coins to equal the same amounts of money</p> <p>Calculating giving change by finding the difference</p>	<p>Solving simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change.</p> <p>Changing a practical context into a calculation</p> <p>2 step problems involving adding and subtracting money</p>
Year 3	<p>Money can be represented in different ways but still have the same value. 100p = £1 When we cross over 100p, we convert this to £1 This fact can be used to convert between pounds and pence e.g 323p = £3 and 23p</p>	<p>Add coin values together to determine the value of an amount of coins crossing over 100p</p> <p>Convert pence to pounds and vice versa</p> <p>When adding amounts together, it is useful to add the pounds first, then add the pence. You can exchange the pence for pounds if needed this way.</p>  <p>Adding 99p is the same as adding £1 then taking away 1p</p> <p>When subtracting amounts of money, you may need to use knowledge of converting and exchange £1 for 100p.</p>	<p>Solving simple problems in a practical context involving addition and subtraction of money of different units, including giving change and requiring conversion of pounds and pence.</p> <p>Changing a practical context into a calculation</p> <p>2 step problems involving adding and subtracting money</p>
Year 4	<p>Amounts of money can be written using decimal notation, with the pence after the decimal point. e.g. £2 and 35p = £2.35 This means £2 and 35 hundredths of a pound as 100p = £1</p> <p>We can use rounding to estimate amounts of money</p>	<p>Compare and order amounts of money, looking at totals that include pence, pounds and pence and decimal notation.</p> <p>Estimate the total of given amounts by rounding.</p>	<p>Solving simple problems in a practical context involving addition and subtraction of money represented in a range of ways, including decimal notation.</p>

	e.g £4.89 is close to £5 This is helpful when estimating prices to find totals.	Add and subtract amounts of money given in decimal notation (not required to add and subtract decimals at this stage – children will partition and recombine or use a number line)	Changing a practical context into a calculation Multi- step problems involving adding and subtracting money.
Year 5		Add and subtract amounts of money given in decimal notation and using decimal notation in the calculation methods.	<p>Use all four operations to solve problems involving money and using decimal notation.</p> <p>Here are some items for sale in a shop.</p>  <p>a) How much more does a scarf cost than a bag of marbles? b) Esther has £15.31 She buys a pair of headphones and a bag of marbles. How much money does she have left?</p>
Year 6			<p>Use all 4 operations and multi-step problems involving money and drawing upon other strands of mathematics e.g percentages and fractions</p> <p>It costs a factory £2.32 to produce 8 key rings. The factory sells the key rings in boxes of 5 for £3.20 How much profit do they make on each key ring?</p>

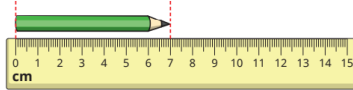
Measurement

Progression of Knowledge	Measurement is a key area of Early Mathematics where children build the language, vocabulary and understanding in a very practical and hands on approach to prepare them for the Key Stage 1 curriculum. Throughout Key Stage 1 pupils explore length, mass, capacity and volume first by measuring using non-standard units and progressing towards standard units. They will compare and solve problems at all stages. Children start to learn equivalence facts in Year 2 by simply understanding how many centimetres are in a metre and new facts are acquired and explored in each year group including imperial measurements being introduced throughout Upper Key Stage 2. Children start to convert the measures that they know in Year 3 in a simple way and do not explore decimal notation in measures until Year 4 when children are secure with knowledge of decimal place value. Conditional knowledge towards the end of Key Stage 2 is extensive and can involve multi-steps, different operations and conversions as well as calculations.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
EYFS	<p>Objects can be described by size:</p> <ul style="list-style-type: none"> • big / little • large / small • tall / short (height) • long / short (length) • wide / narrow <p>Mass can be described by:</p> <ul style="list-style-type: none"> • heavy/ heavier/ heaviest • light / lighter/ lightest <p>Smaller objects are not always lighter and bigger objects are not always heavier</p> <p>Capacity can be described by:</p> <ul style="list-style-type: none"> • empty • full • half full • nearly full • nearly empty 	<p>Compare and order objects by size and mass and describe using mathematical language</p> <p>Sort objects based on their size and mass</p> <p>Use balance scales to explore mass</p> <p>Apply their understanding of language into practical tasks e.g. build a taller tower</p> <p>Explore basic capacity practically e.g. how many scoops of sand will this container hold; how many cups of water will this bucket hold</p>	<p>Solve practical problems applying knowledge of mathematical language with familiar contexts e.g. teddy is packing his suitcase for his holiday and wants to take his lightest toys with him, which should he pack?</p>

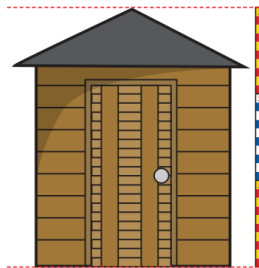
		Measure using non-standard units of measure e.g. 3 hands long	
Year 1	<p>Length = how long something is</p> <p>To describe length, we would say longer or shorter Height is a type of length usually going up – we would use the language taller or shorter</p> <p>We can measure length using objects (e.g cubes, paperclips) but we must use the same objects We can measure length in centimetres using a ruler</p>  <p>Mass = how heavy or light something is</p> <p>If the scales balance, the mass is equal If the balance scale goes lower, it is heavier If the balance scale goes higher, it is lighter</p>  <p>Capacity = amount a container can hold Volume = amount of something inside the container</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">empty </div> <div style="text-align: center;">nearly empty </div> <div style="text-align: center;">nearly full </div> <div style="text-align: center;">full </div> </div>	<p>Measure and begin to record the following:</p> <ul style="list-style-type: none"> lengths and heights (non-standard and ruler) mass/weight (in cubes) capacity and volume (non-standard- in cups) <p>Compare and describe:</p> <ul style="list-style-type: none"> lengths and heights [for example, long/short, longer/shorter, tall/short, double/half] mass/weight [for example, heavy/light, heavier than, lighter than] capacity and volume [for example, full/empty, more than, less than, half, half full, quarter] 	<p>Solve practical problems for:</p> <ul style="list-style-type: none"> lengths and heights [for example, long/short, longer/shorter, tall/short, double/half] mass/weight [for example, heavy/light, heavier than, lighter than] capacity and volume [for example, full/empty, more than, less than, half, half full, quarter]
Year 2	<p>Length and height We can measure in metres or centimetres</p>	<p>Choose and use appropriate standard units to estimate and measure: length/height in any direction (m/cm); mass (kg/g); temperature (°C); capacity (litres/ml)</p>	<p>Solve simple contextual problems involving using different measures and applying the calculations that they know</p> <p>Ben has a toy train, a toy plane and a toy car.</p> <ul style="list-style-type: none"> ▶ The train is 28 cm long. The plane is 16 cm longer. How long is the plane? ▶ The train is double the length of the car. How long is the car?

Centimetres are smaller than **metres** so we would use them to measure smaller things



Metres are bigger than **centimetres** so we would use them to measure bigger things

100 **centimetres** = 1 **metre**



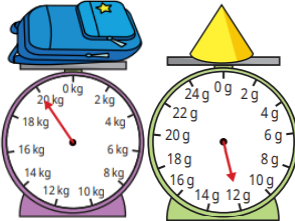
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Mass

We can measure mass in **grams** and **kilograms**

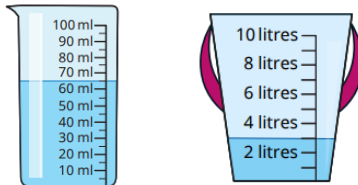
Kilograms are heavier than **grams** and used to measure heavier things.

Grams are lighter than **kilograms** and used to measure lighter things.



Volume/capacity

We can measure **volume** in **millilitres** and **litres**



Temperature

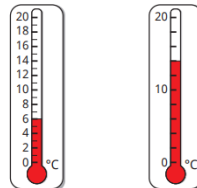
Measures how hot or cold something is.

Temperature is higher when something is warmer;

temperature is lower when something is colder.

We use a **thermometer** to measure temperature

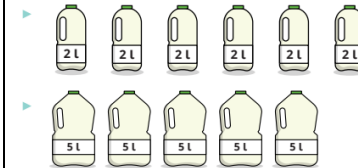
Temperature is measured in **degrees Celsius** and we write this as °C



Measure to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels

Compare and order lengths, mass, volume/capacity and record the results using >, < and =

How much milk is there altogether in each set of cartons?



Year 3

Lengths

100 centimetres = 1 metre

We can measure in **metres** AND **centimetres** e.g. 2m 12cm

Millimetres are a smaller unit of measurement

10 millimetres = 1 centimetre



We can measure in **centimetres** AND **millimetres** e.g. 1cm 6mm

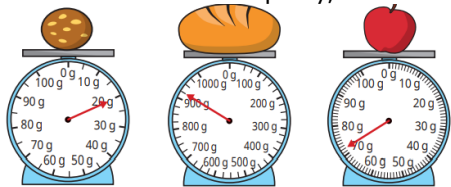
Metres are bigger than **centimetres**; **centimetres** are bigger than **millimetres**. We need to choose the most appropriate **unit of measurement** for what we are measuring

Mass

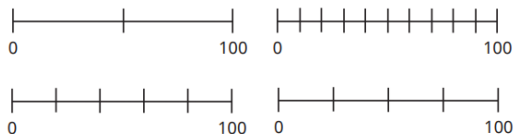
We measure **mass** in **grams**

1000 grams = 1 kilogram

To measure mass and capacity, we need to be able to read different **scales**



To work out what the scale is going up in, we can do **distance ÷ gaps**



We can measure in **kilograms** and **grams** e.g. 2kg 300g

Capacity and Volume

Capacity = maximum amount of liquid a container can hold

Volume = specific amount of liquid in a container

We measure **volume** in millilitres

Measure and compare:
lengths (m/cm/mm);
mass (kg/g);
volume/capacity (l/ml)

Add and subtract all of the
above measures

Simple conversions between
mm/cm and cm/m (not using
decimal notation at this stage)
e.g. 134cm = 1m 34cm
34mm = 3cm 4mm

Solve problems involving adding and
subtracting measures

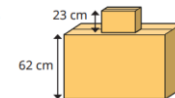
• Dora builds this tower out of boxes.

▶ How tall is Dora's tower?

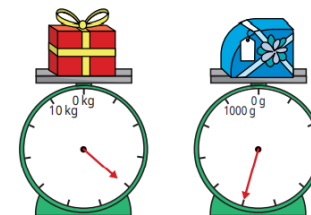
Dora puts a third box on the tower.

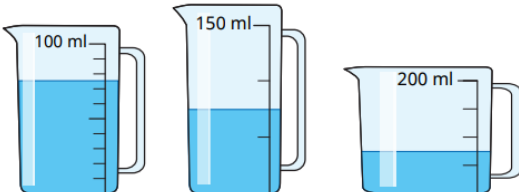
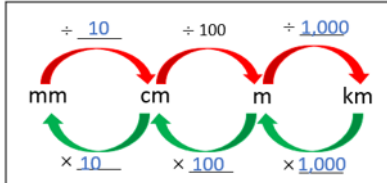
The box is 30 cm tall.


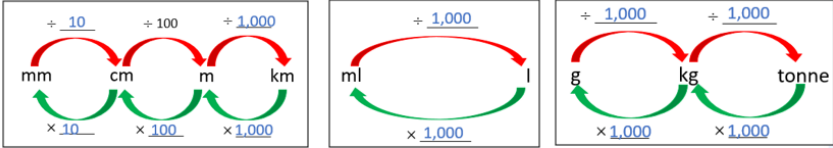

▶ How tall is Dora's tower now?



What is the total mass of the two presents?




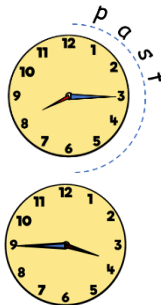

	<div></div> <p>1000 millilitres = 1 litre We can measure in litres and millilitres e.g. 2 litres 200ml</p> <p>Convert means to swap between units of measurement e.g. 134cm = 1m 34cm; 34mm = 3cm 4mm; 2300g = 2kg 300g</p> <p>When comparing, adding and subtracting measures, we should convert them all to the same unit of measurement</p>																				
Year 4	<p>10 millimetres = 1 centimetre 100 centimetres = 1 metre 1000 metres = 1 kilometre</p> <p>Kilometres are greater than metres and are used to measure greater distances.</p> <p>To convert from km to m, multiply by 1000 To convert from m to km, divide by 1000</p> <div></div>	<p>Convert between different units of measure [for example, kilometre to metre]</p> <p>Estimate, compare and calculate different measures</p>	<p>Solve problems involving conversion of different measures</p> <table><tr><th>Pupil</th><th>How far they live from school (km)</th><th>How far they live from school (m)</th></tr><tr><td>Dani</td><td>2 km</td><td></td></tr><tr><td>Scott</td><td></td><td>7,000 m</td></tr><tr><td>Kim</td><td>$\frac{1}{2}$ km</td><td></td></tr><tr><td>Nijah</td><td></td><td>2,500 m</td></tr><tr><td>Teddy</td><td>$1\frac{3}{4}$ km</td><td></td></tr></table> <p>Solve problems involving application of calculation of different measures</p> <p>Solve some 2 step problems applying procedures of measurement including recognising measures written in different ways e.g. $\frac{1}{4}$ of a kilometre</p>	Pupil	How far they live from school (km)	How far they live from school (m)	Dani	2 km		Scott		7,000 m	Kim	$\frac{1}{2}$ km		Nijah		2,500 m	Teddy	$1\frac{3}{4}$ km	
Pupil	How far they live from school (km)	How far they live from school (m)																			
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Year 5	<table><tr><td>Length</td><td>The measurement of something from end to end</td></tr><tr><td>Capacity</td><td>The maximum amount that something can contain</td></tr><tr><td>Mass</td><td>The amount of matter that makes up an object or substance</td></tr></table> <p>10 millimetres = 1 centimetre 100 centimetres = 1 metre 1000 metres = 1 kilometre 1000 millilitres = 1 litre</p>	Length	The measurement of something from end to end	Capacity	The maximum amount that something can contain	Mass	The amount of matter that makes up an object or substance	<p>Understand and use approximate equivalences between metric units and common imperial units such as inches, pounds and pints</p> <p>Convert between different units of metric measure (for example, kilometre and metre; centimetre and metre; centimetre and</p>	<p>Solve problems involving the conversions of imperial units of measure</p> <p>At sports day, the children drink a total of 60 gallons of water.</p> <p>Each child drinks 3 pints.</p> <p>How many children are at the sports day?</p>												
Length	The measurement of something from end to end																				
Capacity	The maximum amount that something can contain																				
Mass	The amount of matter that makes up an object or substance																				

	<p>1000 grams = 1 kilogram</p> <p>Convert = swap between one unit of measurement to another but the amount or size stays the same. To convert from a smaller unit of measurement to a bigger, we divide To convert from a bigger unit of measurement to a smaller, we multiply We divide and multiply by the size of the measurement that we are converting</p> <p>Metric = system for measures that uses a base 10 Imperial = older system for measures – some are still used today</p> <ul style="list-style-type: none"> 1 inch ≈ 2.5 cm 1 stone = 14 pounds 1 foot = 12 inches 1 gallon = 8 pints 1 pound = 16 ounces 	<p>millimetre; gram and kilogram; litre and millilitre)</p>	<p>Use all four operations to solve problems involving measure [for example, length, mass, volume] using decimal notation and including scaling.</p> <p>Solve 2 step problems combining calculating and converting measures</p> <p>The depth of a plank is 15 mm. 12 of the planks are stacked on top of each other. What is the depth of the stack of planks? Give your answer in centimetres.</p> 
Year 6	<p>10 millimetres = 1 centimetre 100 centimetres = 1 metre 1000 metres = 1 kilometre 1000 millilitres = 1 litre 1000 grams = 1 kilogram 1000 kilograms = 1 tonne</p> <p>Convert = swap between one unit of measurement to another but the amount or size stays the same. To convert from a smaller unit of measurement to a bigger, we divide To convert from a bigger unit of measurement to a smaller, we multiply We divide and multiply by the size of the measurement that we are converting</p>  <p>5 miles is approximately equal to 8 kilometres We can use this fact to work out other conversions e.g.</p> <div style="border: 1px solid red; padding: 5px; display: inline-block;"> <p>5 miles ≈ 8 km <u>10</u> miles ≈ 16 km</p> </div>	<p>Convert between standard units, converting measurements of length, mass and volume from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimal places</p> <p>Convert between miles and kilometres</p>	<p>Solve multi-step problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate.</p> <p>Jack wants to find out the mass of his suitcase. Jack weighs 34.5 kg. He steps onto the scales and it shows 47 kg and 200 g. How heavy is his suitcase?</p>  <p>Solve problems drawing upon and applying other strands of mathematics and notating answers accurately where stipulated</p> <p>Solve contextual problems involving the conversion of miles and kilometres</p> <p>Esther cycles 70 miles over 4 days. On day 1, she cycles 14 miles. On day 2, she cycles 32 km. On day 4, she cycles twice as far as she does on day 3 How far does she cycle on day 4? Give units with your answer.</p>

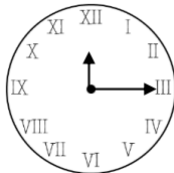

Time

Progression of Knowledge	<p>Children first explore the concept of time in EYFS where they use simple language to describe events and their daily routine. They build upon this and start to learn to tell the throughout Year 1 (to the hour and half past), Year 2 (to the nearest 5 minutes) and Year 3 (to the nearest minute). Children should leave Year 3 secure with telling the time to prepare them for learning about digital and 24-hour clocks in Year 4.</p> <p>There is no new declarative or procedural knowledge introduced throughout Upper Key Stage 2. During this phase, pupils apply their knowledge to solve problems in different ways with flexibility and deep understanding of how to manipulate and convert time. Therefore, it is essential that pupils end Year 4 being fluent and confident telling the time.</p>
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'													
EYFS	<p>Night time is when we go to bed and it gets dark</p> <p>Day time is when we wake up and it is light</p> <p>Today is the day that we are in now</p> <p>Tomorrow is the day that will be next</p> <p>Morning is when we have just woken up</p> <p>Afternoon is after lunch</p>	<p>Order key events in daily routines</p> <p>Use language to describe when events happen – day, night, morning, afternoon, before, after, today, tomorrow, now, next, later</p> <p>Informally measure time e.g. how many jumps can I do before the sand timer runs out or use a calendar to count down how many days until an event</p>														
Year 1	<p>There are 7 days in a week</p> <table><tr><td>Monday</td><td>Tuesday</td><td>Wednesday</td><td>Thursday</td><td>Friday</td><td>Saturday</td><td>Sunday</td></tr></table> <p>There are 12 months in a year</p> <table><tr><td>January</td><td>February</td><td>March</td><td>April</td><td>May</td><td>June</td></tr></table>	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday	January	February	March	April	May	June	<p>Compare and describe time using appropriate language e.g. quicker, slower, earlier, later</p>	
Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday										
January	February	March	April	May	June											


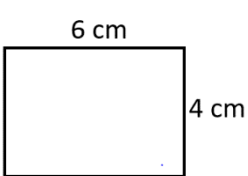
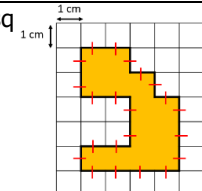
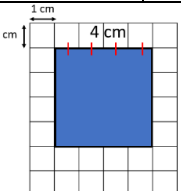
	<div>JulyAugustSeptemberOctoberNovemberDecember</div> <p>Time can be measured in seconds, minutes and hours</p> <p>Seconds = shortest measurement of time Minutes Hours = longer measurement of time</p> <p><u>Telling the time</u> A clock has a longer hand and a shorter hand The shorter hand is the hour hand; the longer hand is the minute hand When the longer hand is pointing to 12, this is ____ o'clock O'clock means on the hour. The shorter hand shows us the hour</p> <p>At half past the hour, the minute hand has travelled half-way around the clock from 12 to 6. The hour hand will be half-way between the hours.</p>	<div></div>	<p>Measure and record time in hours, minutes and seconds</p> <p>Sequence events in chronological order using appropriate language e.g. before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening</p> <p>Use language relating to dates e.g. days, weeks, months and year</p> <p>Tell the time to the hour and half past the hour and draw the hands on a clock face to show these times</p>	
Year 2	<p>60 minutes = 1 hour 24 hours = 1 day</p> <p><u>Telling the time</u> At quarter past, the minute hand has travelled a quarter of the way around the clock and is pointing at 3. The hour hand will be just past the hour</p> <p>At quarter to, the minute hand has travelled $\frac{3}{4}$ of the way around the clock and has only $\frac{1}{4}$ to go until the next hour. The minute hand will point at 9 and the hour hand will be nearly at the next hour.</p> <p>Every number on the clock face represents 5 minutes We can use counting in multiples of 5 to help us work out the minutes</p>	<div></div>	<p>Compare and sequence intervals of time</p> <p>Tell and write time to the nearest 5 minutes, including quarter past/to and draw the hands on a clock face to show these times</p>	<p>Solve simple word problems involving time</p> <p>Aisha and Kim both started their homework at 6 o'clock.</p> <div></div> <p>Aisha finished her homework at 25 past 6 Kim's homework took her 10 minutes longer. What time did Kim finish her homework?</p>

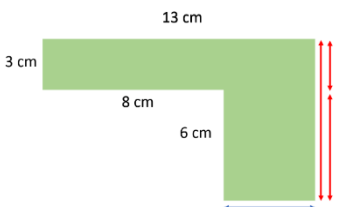
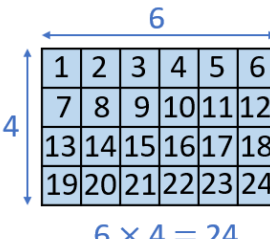
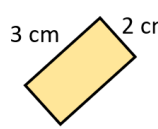
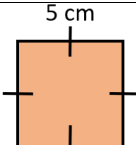
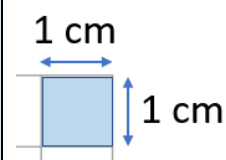
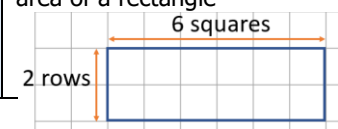
	<div><div><div><div><div>55</div><div>60</div><div>5</div></div><div><div>50</div><div>10</div><div>15</div></div><div><div>45</div><div>20</div><div>25</div></div><div><div>40</div><div>30</div><div>35</div></div></div><div><div><div>12</div><div>1</div><div>2</div><div>3</div><div>4</div><div>5</div><div>6</div><div>7</div><div>8</div><div>9</div><div>10</div><div>11</div></div><div><div>12</div><div>11</div><div>10</div><div>9</div><div>8</div><div>7</div><div>6</div><div>5</div><div>4</div><div>3</div><div>2</div><div>1</div></div></div><div><div>The second half of the clock is 'to' the hour so we would need to count how many minutes (in 5s) 'to' the hour this is</div></div></div><div><div><div>5 to</div><div>O'clock</div><div>5 past</div><div>10 past</div><div>Quarter past</div><div>20 past</div><div>25 past</div><div>Half past</div><div>25 to</div><div>20 to</div><div>Quarter to</div><div>10 to</div><div>5 to</div></div><div><div><div>12</div><div>1</div><div>2</div><div>3</div><div>4</div><div>5</div><div>6</div><div>7</div><div>8</div><div>9</div><div>10</div><div>11</div></div><div><div>12</div><div>11</div><div>10</div><div>9</div><div>8</div><div>7</div><div>6</div><div>5</div><div>4</div><div>3</div><div>2</div><div>1</div></div></div></div></div>														
Year 3	<div><div>60 seconds = 1 minute</div><div>Different months have a different number of days</div><div><table><tr><td>January 31</td><td>February 28 (29)</td><td>March 31</td><td>April 30</td><td>May 31</td><td>June 30</td></tr><tr><td>July 31</td><td>August 31</td><td>September 30</td><td>October 31</td><td>November 30</td><td>December 31</td></tr></table></div><div><div>365 days = 1 year</div><div>366 days (extra day in February) = leap year (every 4 years)</div><div><div>There are 24 hours in a day; there are 12 hours on a clock.</div><div>To complete a day, the clock will go around twice.</div><div>Once is am; the other is pm</div><div>am = morning</div><div>12pm = noon</div><div>pm = afternoon/evening</div><div>12am = midnight</div></div><div><div><div>Telling the time to the nearest minute</div><div>Use the 5-minute intervals</div><div>Count the individual minutes between the 5-minute markers</div><div>Consider past and to</div></div><div><div><div>5 to</div><div>10 to</div><div>quarter to</div><div>20 to</div><div>25 to</div><div>half past</div><div>25 past</div><div>20 past</div><div>quarter past</div><div>10 past</div><div>5 past</div><div>o'clock</div></div><div><div><div>12</div><div>1</div><div>2</div><div>3</div><div>4</div><div>5</div><div>6</div><div>7</div><div>8</div><div>9</div><div>10</div><div>11</div></div><div><div>12</div><div>11</div><div>10</div><div>9</div><div>8</div><div>7</div><div>6</div><div>5</div><div>4</div><div>3</div><div>2</div><div>1</div></div></div><div><div>23 minutes past</div></div></div></div></div><div><div>Some clocks show the numbers using roman numerals</div></div></div>	January 31	February 28 (29)	March 31	April 30	May 31	June 30	July 31	August 31	September 30	October 31	November 30	December 31	<div><div>Tell and write the time from an analogue clock (including roman numerals) to the nearest minute</div><div>Record time in seconds, minutes and hours</div><div>Compare durations of events e.g. the time taken by different tasks</div></div>	<div><div>Solve simple one-step time problems with familiar contexts</div><div><div>Whitney is baking a cake.</div><div>She looks at the clock before she puts the cake into the oven.</div><div><div><div><div>Flour</div></div><div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div></div></div></div><div><div><div><div>12</div><div>1</div><div>2</div><div>3</div><div>4</div><div>5</div><div>6</div><div>7</div><div>8</div><div>9</div><div>10</div><div>11</div></div><div><div>12</div><div>11</div><div>10</div><div>9</div><div>8</div><div>7</div><div>6</div><div>5</div><div>4</div><div>3</div><div>2</div><div>1</div></div></div><div><div>30 minutes</div></div></div></div><div><div>The cake needs to be in the oven for 30 minutes.</div><div>At what time should she take the cake out of the oven?</div></div></div></div>
January 31	February 28 (29)	March 31	April 30	May 31	June 30										
July 31	August 31	September 30	October 31	November 30	December 31										

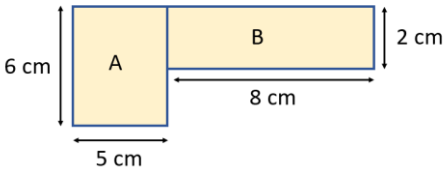
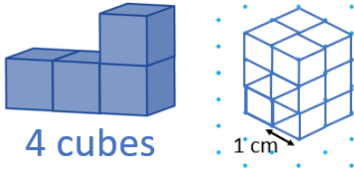
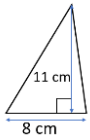
																																																			
Year 4	<p>Time can be displayed in 2 different ways</p> <p>1. Analogue = clock face </p> <p>2. Digital = numbers e.g. hours : minutes 7:55 am</p> <p>We use the hour and minute hand to help us write time in digital format</p> <p>In 24 hour clock, am times are the same except for midnight</p> <table><tr><td>12am</td><td>1am</td><td>2am</td><td>3am</td><td>4am</td><td>5am</td><td>6am</td><td>7am</td><td>8am</td><td>9am</td><td>10am</td><td>11am</td></tr><tr><td>0:00</td><td>1:00</td><td>2:00</td><td>3:00</td><td>4:00</td><td>5:00</td><td>6:00</td><td>7:00</td><td>8:00</td><td>9:00</td><td>10:00</td><td>11:00</td></tr></table> <p>To convert pm 12-hour clock times into 24-hour clock, add on 12 hours</p> <table><tr><td>12pm</td><td>1pm</td><td>2pm</td><td>3pm</td><td>4pm</td><td>5pm</td><td>6pm</td><td>7pm</td><td>8pm</td><td>9pm</td><td>10pm</td><td>11pm</td></tr><tr><td>12:00</td><td>13:00</td><td>14:00</td><td>15:00</td><td>16:00</td><td>17:00</td><td>18:00</td><td>19:00</td><td>20:00</td><td>21:00</td><td>22:00</td><td>23:00</td></tr></table> <p>When writing time in 24hr clock, you do not need to have am/pm on the end as it is obvious which one you are referring to.</p>	12am	1am	2am	3am	4am	5am	6am	7am	8am	9am	10am	11am	0:00	1:00	2:00	3:00	4:00	5:00	6:00	7:00	8:00	9:00	10:00	11:00	12pm	1pm	2pm	3pm	4pm	5pm	6pm	7pm	8pm	9pm	10pm	11pm	12:00	13:00	14:00	15:00	16:00	17:00	18:00	19:00	20:00	21:00	22:00	23:00	<p>Read, write and convert time between analogue and digital</p> <p>Understand digital time written in 24-hour clocks</p> <p>Convert units of time e.g. hour to minute</p>	<p>Solve problems involving converting from hours to minutes, minutes to seconds, years to months, weeks to days</p>
12am	1am	2am	3am	4am	5am	6am	7am	8am	9am	10am	11am																																								
0:00	1:00	2:00	3:00	4:00	5:00	6:00	7:00	8:00	9:00	10:00	11:00																																								
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12:00	13:00	14:00	15:00	16:00	17:00	18:00	19:00	20:00	21:00	22:00	23:00																																								
Year 5			<p>Solve problems involving converting between all units of time</p>																																																
Year 6			<p>Solve problems involving applying knowledge of time to interpreting timetables</p> <p>Solve problems involving adding and subtracting time, including calculating durations, and understanding the methods that are useful</p>																																																

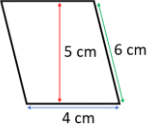
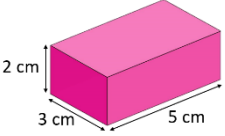
Area, Perimeter and Volume

Progression of Knowledge	<p>Children are introduced to the concept of perimeter in Year 3 once they have secure knowledge of 2D shapes and different lengths from KS1 Geometry and Measurement sequences of learning. In Year 4, this progresses to the perimeter of rectilinear shapes and once secure with perimeter, children move onto being introduced to the concept of area. This is firstly introduced in Year 4 as counting squares and links to knowledge of arrays and multiplication. It progresses towards a formula for different shapes throughout Upper Key Stage 2. Children explore the difference between perimeter and area in depth by Year 6.</p> <p>Children are first introduced to volume in Upper Key Stage 2 once they have a firm understanding of perimeter and area. It is explored as 1cm^3 blocks first in Year 5 to build concrete understanding before progressing to using a formulae for calculating volume in year 6. The link between area and volume is made explicit.</p>
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
Year 3	<p>Perimeter = total length around the edge of a 2D shape Length can be measured in mm, cm, m etc and so can perimeter.</p>  <p>Measure the sides – using a ruler Add them all up to find total length Use knowledge of shapes to help:</p> <ul style="list-style-type: none"> • All sides on a square will be equal length • Opposite sides of a rectangle will be equal 	<p>Measuring perimeter</p> <p>Calculating perimeter</p> <p>Finding the most efficient strategy for adding multiple values together e.g. use of doubles and number bonds.</p>	
Year 4	<p>Perimeter on a grid – can count the squares</p> <p>Only around the outside</p> <p>Apply knowledge of shapes to help</p>  	<p>Using efficient methods to calculate the perimeter</p> <p>length + width x 2 for a rectangle</p> <p>length x 4 for a square</p>	<p>Knowing the perimeter of a rectangle or square can be used to work out missing sides.</p>






























	<p>Rectilinear shape = a shape with straight sides and all sides meeting at right angles</p> <p>Add together the lengths of the sides to find the perimeter</p>  <p>Missing lengths can be found by using the sum of the parallel sides</p> <p>Area = the amount of space taken up by a 2D shape Find the area by counting squares</p>  <p>$6 \times 4 = 24$</p>	  <p>Measuring and calculating the perimeter of composite rectilinear shapes</p> <p>Finding the area of rectilinear shapes by counting squares</p> <p>Finding missing lengths on rectilinear shapes</p>	
Year 5	<p>We can apply knowledge of properties of shapes to help us work out missing sides to calculate the perimeter:</p> <ul style="list-style-type: none"> Equilateral triangles – all sides same length Isosceles triangles – 2 sides same length Parallelogram – opposite sides equal length <p>Area is measured in centimetres squared</p> <p>1 cm x 1 cm 1cm squared 1cm²</p>  <p>To save counting the squares, we can do length x width to find the area of a rectangle</p> 	<p>Measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres – including finding missing lengths</p> <p>Calculate the area of rectangles</p> <p>Estimate the area of irregular shapes</p> <p>Estimate volume</p>	<p>Solve problems where the area or perimeter is known and the other needs calculating (vice versa)</p> <p>Know and identify the conditions and contexts where area and perimeter would be useful – apply procedural knowledge to problem solve</p>




















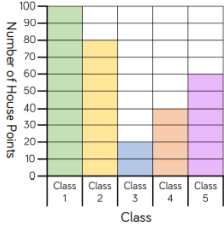














































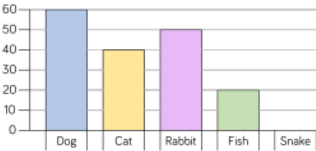














	<p>Area of a compound shape:</p> <ul style="list-style-type: none"> • split into rectangles • find the area ($l \times w$) • add back together • apply knowledge of finding missing lengths if needed  <p>Volume = amount of space an object takes up</p>  <p>Measured in centimetres cubed cm^3</p>		
Year 6	<p>Perimeter = add up all the sides Area of a rectangle = length x width</p> <p>Shapes with the same areas can have different perimeters Shapes with the same perimeters can have different areas</p> <p>Area of a triangle = $\text{base} \times \text{height} \times \frac{1}{2}$</p>  <p>Area of a parallelogram = $\text{base} \times \text{perpendicular height}$</p>	<p>Recognise when it is possible to use formula for area and volume of shapes</p> <p>Calculate the area of parallelograms and triangles</p> <p>Calculate the volume of cubes and cuboids</p>	<p>Solve multi-step problems involving application of all procedural and declarative knowledge relating to this area.</p>

	 <p>Volume of a cuboid = length x width x height</p> 		
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Statistics

Progression of Knowledge	Children first explore statistics in Year 2 where they look at basic tally charts, pictograms and block diagrams. Pupils explore the contexts and purpose of gathering data. This is developed in Year 3 where they build upon knowledge of pictograms, explore bar charts and spend more time eliciting and solving problems with information from these. In Year 4 and 5, children explore line graphs, bar charts and timetables and start to understand the differences between discrete and continuous data and the decisions that mathematicians make when representing data – such as which graph and which scale is most appropriate. In Year 6, children explore pie charts and apply knowledge of angles to help construct these.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'																						
Year 2	<p>Tally charts are used to count and record data One stick represents 1 We do the 5th stick across</p> 	<table><tr><td>Animals</td><td>Tally</td><td>Total</td></tr><tr><td>Horses</td><td>I</td><td>1</td></tr><tr><td>Dogs</td><td>II</td><td>2</td></tr><tr><td>Chickens</td><td>IIII II</td><td>7</td></tr><tr><td>Frogs</td><td>IIII</td><td>4</td></tr><tr><td>Sheep</td><td>IIII III</td><td>9</td></tr></table>	Animals	Tally	Total	Horses	I	1	Dogs	II	2	Chickens	IIII II	7	Frogs	IIII	4	Sheep	IIII III	9	<p>Counting and sorting categories by quantity</p> <p>Constructing tally charts, pictograms, block diagrams and tables.</p> <p>Interpreting tally charts, pictograms, block diagrams and tables. (pictograms within 2s, 5s and 10s)</p>	<p>Use knowledge and procedures to total and compare data</p>			
	Animals	Tally	Total																						
	Horses	I	1																						
Dogs	II	2																							
Chickens	IIII II	7																							
Frogs	IIII	4																							
Sheep	IIII III	9																							
	<p>We can then count the total easily by counting in 5s and 1s</p> <p>Pictograms use pictures to show data</p> <table><tr><th>Player</th><th>Goals scored</th></tr><tr><td>Alex</td><td></td></tr><tr><td>Jack</td><td></td></tr><tr><td>Mo</td><td></td></tr><tr><td>Rosie</td><td></td></tr><tr><td>Whitney</td><td></td></tr></table> <p>Pictures can represent more than one – there will be a key to show Count in that number to find the total</p> <p>Pictograms can be set out horizontally and vertically</p>	Player	Goals scored	Alex		Jack		Mo		Rosie		Whitney		<table><tr><th>Day</th><th>Chickens seen</th></tr><tr><td>Monday</td><td></td></tr><tr><td>Tuesday</td><td></td></tr><tr><td>Wednesday</td><td></td></tr><tr><td>Thursday</td><td></td></tr></table> <p>Key  = 10 chickens</p>	Day	Chickens seen	Monday		Tuesday		Wednesday		Thursday		
Player	Goals scored																								
Alex																									
Jack																									
Mo																									
Rosie																									
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	<div><div><div><div></div><div></div><div></div><div></div></div><div><div>Teddy</div><div>Annie</div><div>Amir</div><div>Whitney</div></div></div><div><table><tr><th>Player</th><th>Goals scored</th></tr><tr><td>Alex</td><td></td></tr><tr><td>Jack</td><td></td></tr><tr><td>Mo</td><td></td></tr><tr><td>Rosie</td><td></td></tr><tr><td>Whitney</td><td></td></tr></table></div></div> <div><table><tr><th>Name</th><th>Score</th></tr><tr><td>Ron</td><td>20</td></tr><tr><td>Eva</td><td>12</td></tr><tr><td>Amir</td><td>6</td></tr><tr><td>Mo</td><td>16</td></tr></table><p>Tables show data with numbers</p></div> <div><p>Block diagrams show data using blocks</p><p>We can use what we know about number lines to help with the scale</p><p>The scale could go up in different jumps but will always be the same jump e.g. 1s, 2s, 5s, 10s</p><p>How tall the blocks are shows the number that it represents</p><div><p>Block graph to show House Points Collected</p></div></div>	Player	Goals scored	Alex	 	Jack		Mo	     	Rosie	     	Whitney	   	Name	Score	Ron	20	Eva	12	Amir	6	Mo	16		
Player	Goals scored																								
Alex	 																								
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Ron	20																								
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Amir	6																								
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Year 3	<p>The key on a pictogram may show halves and quarters of the number</p> <div><div><p>Key</p><p>= 8 apples</p></div><table><tr><th>Group</th><th>Apples</th></tr><tr><td>1</td><td></td></tr><tr><td>2</td><td></td></tr><tr><td>3</td><td></td></tr><tr><td>4</td><td></td></tr><tr><td>5</td><td></td></tr></table></div> <p>Bar charts show information in bars</p> <p>The bars will not touch</p> <p>Scales will go up in the same jumps</p> <p>We can use the bars to see the information such as most popular and least popular</p> <div></div>	Group	Apples	1	   	2		3	  	4		5		<p>Interpret and present data using bar charts, pictograms and tables (pictograms to go beyond 2s,5s and 10s)</p> <p>Use pictograms, tables and tally charts to construct bar charts</p>	<p>Solve one-step and two-step questions [for example, 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables.</p>										
Group	Apples																								
1	   																								
2																									
3	  																								
4																									
5																									

<div>Year 4</div>	<div><p>Discrete data = shows stand alone data or information at a point in time e.g. favourite colours</p><p>The best way to show this is a bar chart, pictogram or table</p><div><table><tr><th>Activity</th><th>Number of votes</th></tr><tr><td>Bowling</td><td>9</td></tr><tr><td>Cinema</td><td>10</td></tr><tr><td>Swimming</td><td>7</td></tr><tr><td>Ice-skating</td><td>14</td></tr></table><div><p>How I travel to school</p></div><div><table><tr><th>Team</th><th>Number of house points</th></tr><tr><td>Sycamores</td><td>10</td></tr><tr><td>Oak</td><td>8</td></tr><tr><td>Beech</td><td>6</td></tr><tr><td>Ash</td><td>10</td></tr></table><p>■ = 20 points</p></div></div><p>Continuous data = shows data over time</p><p>The best way to show this is a time graph (line graph)</p><div><div><p>Plant Growth</p></div><div><p>A measurement of time will usually go along the x axis</p><p>What is being measured will go along the y axis</p><p>We can use this to see find information about one variable based on the other.</p></div></div></div>	Activity	Number of votes	Bowling	9	Cinema	10	Swimming	7	Ice-skating	14	Team	Number of house points	Sycamores	10	Oak	8	Beech	6	Ash	10	<div><p>Interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs.</p><p>Decide which scale will be most appropriate when representing a set of data</p></div>	<div>Solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs.</div>
Activity	Number of votes																						
Bowling	9																						
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<div>Year 5</div>	<div><p>Line graphs can be used to show data other than related to time – such as conversion graphs</p><div><div></div><div><p>Line graphs can be used to find out information about one point based on the other.</p></div></div><p>Tables show data and information in categories – we can use this to retrieve information and use it to compare.</p><table><tr><th>Planet</th><th>Time for revolution</th><th>Diameter (km)</th><th>Time for rotation</th></tr><tr><td>Mercury</td><td>88 days</td><td>4,878</td><td>59 days</td></tr><tr><td>Venus</td><td>225 days</td><td>12,104</td><td>116 days</td></tr><tr><td>Earth</td><td>365 days</td><td>12,756</td><td>24 hours</td></tr><tr><td>Mars</td><td>687 days</td><td>6,794</td><td>25 hours</td></tr></table></div>	Planet	Time for revolution	Diameter (km)	Time for rotation	Mercury	88 days	4,878	59 days	Venus	225 days	12,104	116 days	Earth	365 days	12,756	24 hours	Mars	687 days	6,794	25 hours	<div><p>Interpret and construct line graphs – finding the difference between 2 points, the amount of time spent above/below certain points and make inferences based on the information presented.</p><p>Complete, read and interpret information presented in tables.</p></div>	<div>Solve comparison, sum and difference problems using information presented in line graphs, tables and timetables</div>
Planet	Time for revolution	Diameter (km)	Time for rotation																				
Mercury	88 days	4,878	59 days																				
Venus	225 days	12,104	116 days																				
Earth	365 days	12,756	24 hours																				
Mars	687 days	6,794	25 hours																				

Two-way tables show more than one piece of information about each variable and show totals

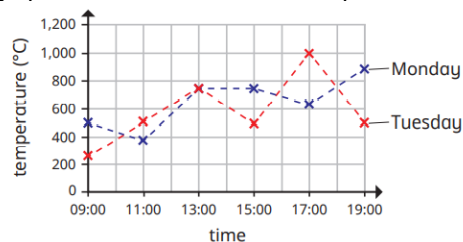
	No glasses	Glasses	Total
Constable	55	24	79
Sergeant	8	5	13
Inspector	2	4	6
Chief Inspector	1	1	2
Total	66	34	100

Timetables show information related to timings in a table

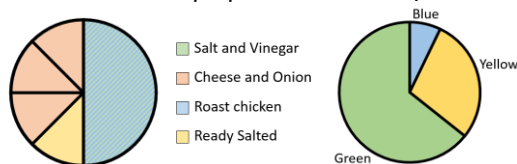
Bus terminal	09:32	10:02	10:22	10:32
Shopping centre	09:41	10:11	10:31	10:41
Football stadium	09:59	10:29	10:49	10:59
University campus	10:13	10:43	11:03	11:13
Library	10:16	10:46	11:06	11:16
Cinema	10:21	10:51	11:11	11:21
Museum	10:28	10:58	11:18	11:28

Year 6

Line graphs can show data with more than one line on the same graph. This can be useful to compare



Pie charts show the proportion of data represented in a circle



The larger the section, the larger the data that it represents
Halves and quarters are easily identifiable on a circle
Percentages can be used to help
The total that the pie chart represents is essential information

When drawing a pie chart, 360° represents 100% of the pie chart

Mean = average of a set of numbers

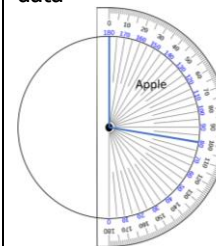
Mean = total of data set \div number of items

Interpret and construct line graphs

Interpret and construct pie charts:
Convert data into proportions of 360°

Fruit	Number of children	Number of degrees
Apple	10	$10 \times 10 = 100^\circ$
Banana	5	$5 \times 10 = 50^\circ$
Grapes	3	$3 \times 10 = 30^\circ$
Orange	18	$18 \times 10 = 180^\circ$
Total	36	$36 \times 10 = 360^\circ$

Use a protractor to represent proportions of data



Calculate the mean as an average

Can solve problems using line graphs including ones with multiple sets of data, trends and ones applying other areas of Mathematics e.g. negative numbers

Can apply knowledge of angles, fractions and percentages to interpret pie charts and solve problems involving data represented in a pie chart.

Know the conditions in which it is appropriate to find the mean of a data set.

Algebra



Progression of Knowledge	The concept of Algebra and the knowledge associated to it is only introduced in Year 6 once children are fully secure with the number system and how it operates. They will build upon knowledge from other year groups of using operations and their inverses to find missing numbers.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'												
Year 6	<p>Algebra uses letters to represent numbers</p> <p>Expression = way of writing something algebraically. The letter can have different values e.g. $h + 3$</p> <p>Algebra notation:</p> <ul style="list-style-type: none">To add or subtract use + and – e.g. $s + 2$, $6 - t$$3t = 3$ multiplied by $t = t + t + t$$\frac{n}{3} = n$ divided by 3 <p>These can be combined to form longer expressions with more than one step e.g. $3a + 1$</p> <p>We can find the value of an expression by substitution. We can substitute numbers in the place of letters. e.g. $3a + 1$ 3 multiplied by a then add 1 If $a = 4$, 3 multiplied by 4 is 12, then add 1 = 13</p> <p>A formula is a rule or relationship that uses letters to represent amounts which can be changed.</p> <p>Equation = like an expression but has an equals sign. The letter has a value to be found.</p> <div><div><p>Expression</p><p>$x + 5$</p><p>Different values depending on the value of x</p></div><div><p>Equation</p><p>$x + 5 = 11$</p><p>x is a specific unknown value</p></div></div>	<p>Form simple expressions</p> <div><div><div>h</div><div>3 cm</div></div><div>Rosie's new height</div><div>$h + 3$</div></div> <p>Substitute a value into an expression</p> <p>Use simple formula and find the nth term</p> <div><div><div></div><table><tr><td>Number triangles (t)</td><td>1</td><td>2</td><td>3</td><td>4</td><td>20</td></tr><tr><td>Number of straws (s)</td><td>3</td><td>5</td><td>7</td><td>9</td><td></td></tr></table></div></div> <p>Form equations by expressing missing number problems algebraically</p> <p>Solve one-step and two-step equations</p> <div><div><div>12</div><div><div>y</div><div>y</div><div>y</div><div>6</div></div></div></div>	Number triangles (t)	1	2	3	4	20	Number of straws (s)	3	5	7	9		<p>Solve problems with 2 unknown values, but where more than one piece of information is given, so that there is only one solution.</p> <p>Two apples and three bananas cost £1.02</p> <p>Two apples and five bananas cost £1.46</p> <div><div><div><div><div>£1.02</div><div></div></div><div></div><div><div>£1.46</div></div></div></div><p>What is the total cost of one apple and one banana?</p></div>
Number triangles (t)	1	2	3	4	20										
Number of straws (s)	3	5	7	9											

<p>Inverse operations are used to help solve equations. $c + 5 = 12$ $12 - 5 = c$</p> <p>2-step equations require 2 steps of the inverse – first isolate the letter $2a + 5 = 13$ $13 - 5 = 2a$ $8 = 2a$ $8 \div 2 = a$</p> <p>Equations may have 2 unknown values e.g $2b + c = 7$ We can work systematically to find all possible values e.g if $b = 1, c = 5$ if $b = 2, c = 3$ if $b = 3, c = 1$ We cannot know the exact values as we don't have enough information</p>	<p>Find pairs of numbers that satisfy an equation with two unknowns</p> <p>Enumerate possibilities of combinations of 2 variables</p> <div><div>$3a + 2b = 20$</div><div>$x + y = 5$</div></div> <table><tr><th>x</th><th>y</th><th>$x + y$</th></tr><tr><td>0</td><td>5</td><td>5</td></tr><tr><td></td><td></td><td>5</td></tr><tr><td></td><td></td><td>5</td></tr></table>	x	y	$x + y$	0	5	5			5			5	
x	y	$x + y$												
0	5	5												
		5												
		5												

Ratio

Progression of Knowledge	Children first experience simple problems relating to correspondence and scaling in years 4 and 5 linked to multiplication. Explicit ratio knowledge is only introduced in Year 6 once pupils have a firm understanding of the number system. Starting with exploring objects being linked to each other, children are then introduced to the language and notation before recognising contexts in which this information is useful.
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	Declarative knowledge 'I know that...'	Procedural knowledge 'I know how...'	Conditional knowledge 'I know when...'
Year 6	<p>Ratio represents a multiplicative relationship between two amounts. One value is related to another</p> <p>e.g. for every 2 red counters, there are 3 blue counters this would be written as a ratio using the symbol : The ratio of red to blue red : blue 2:3</p> <p>Ratios can be simplified – like fractions</p>  <p>Yellow : Blue 16 : 8 2 : 1</p> <p>Ratios can represent more than 2 values The bar model shows the ratio 2:3:4</p>  <p>When you multiply or divide one amount, you do the same to the other in the ratio</p> <p>Scale diagrams show something drawn not to size but in proportion</p>	<p>Write relationships using ratio notation and simplify ratios</p> <p>Use multiplication and division facts to work out simple ratios</p> <p>Find a scale factor of a drawing</p> <p>Enlarge or reduce a shape by a given scale factor</p>	<p>Solve a variety of problems using ratio:</p> <ul style="list-style-type: none"> Finding missing values using multiplication and division facts Where the ratio is given and one value is known Where the ratio is given and the total is known Where something is scaled up or down e.g. one-tenth the size Where proportions are used e.g. this recipe feeds 3 but we are cooking for 12 Where shapes are similar Where scale factors are used

	<p>Scale factor is the factor that something has been enlarged or reduced by</p> <div data-bbox="383 256 593 399"> </div> <p>To find a scale factor, we can use the dimensions and work out what it has been multiplied or divided by</p> <p>All sides will be enlarged/reduced by the same scale factor – they will be in proportion Angles will not change</p>		
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Mathematics – Knowledge progression

FS1 Long Term Plan 2021 – 2022 Maths

	Autumn 1		Autumn 2		Spring 1		Spring 2		Summer 1		Summer 2	
General Themes	My Favourite Colours		Special Times & Nursery Rhymes		Traditional Tales		The Wonder of Water!		Ready, Steady, Grow!		Creepy Crawly!	
Key Vocabulary	Colour Sort Same Different	Big Small Count Match	Bigger Biggest Smaller smallest	More Less None Zero	Number Shape name Sides Edges	Curve Straight Subitise	Number Shape name Sides Edges	Curve Straight Subitise	Order More Fewer Part	Numeral Amount Total	First, next, then etc Long, tall, short	Light/Heavy Capacity words Positional language
Number Numerical Patterns	Number Songs /Colours /Matching/ Sorting Children will: Recognise, name, match & sort by colour. • Sort by other attributes e.g. size • Rote count through songs & rhymes • Develop everyday maths vocabulary		Number 1/ Number 2 • Rote counting to 10 • Develop 1-1 correspondence to 5 – Giant’s footsteps! Number 1 • ‘One Wonderful Mel’ • 2D shape – Circles • ‘Circle’ – Mac Bennett • Use numeral & formation rhyme for 1 • One or lots? Number 2 • One & another one... • Identify 2D shape – semi-circle Classifying – circle/semi-circle • Subitise 1 & 2 • Use numeral & formation rhyme for 2 • Make pairs • Creating patterns		Number 3/Number 4/ Number 3 • Recognise 2D shape – triangle • Use positional language – build with shape • Subitise 1, 2 & 3 Number 4 • Find 4 objects & on no line • Subitise 1, 2, 3 & 4 • Represent 4 on 5 frame, on fingers etc • Recognize 2D shape – Squares and rectangles • Use numeral & formation rhymes to 4 • Make pattern with shape & numerals • Understand composition 4		Number 5/1 more & 1 fewer • Order numerals 1 – 5 • Find 5 objects & position on number line, • Represent 5 on 5 frame • Recognise 2D shape – stars & Pentagons • Use numeral & formation rhyme to 5 • Order numerals 1 – 5 • Represent 5 - marks, pictures, fingers • Match numerals & quantities • Understand the composition of 5 • Explore 1 more than/1 fewer than		Comparing amounts, sizes, capacity/ pattern Children will: • Use & extend the language of size • One-one principles, stable-order principle, cardinal principle, abstraction principle, order-irrelevance principle • Compare amount of objects • 2D shapes • 2D shapes		My Day /Capacity/ Positional Language Children will: • Order daily events • Understand and apply Long Short Tall • Understand and apply Light and heavy - comparing • Understand and apply Full/half-full/empty and comparing • Use language relating to position and direction	
End of Nursery Goals: •Children are able to subitise to 3. •Children are able to name & recognise some numbers up to 5. •Children are able to represent numbers 0-5 in various different ways. •Children are to know & be able to discuss properties of some 2D & 3D shape using informal language. •Children are able to use specific shape for purpose (use triangle for roof). Children are able to copy & continue a simple ABAB pattern.												

FS2 Long Term Plan 2021 – 2022

Maths

	Autumn 1		Autumn 2		Spring 1		Spring 2		Summer 1		Summer 2	
General Themes	Me and My Family		Seasons, Animals & Habitats		People Who Help Us		Living Things & Plants		Let's explore our neighbourhood		Under the Sea (Materials etc)	
Key Vocabulary	Count Time Days of the week	Fewer/fewest smaller/smallest	Recognise Compare Represent Compose	Positional language – in/in front of, behind, side, under	Recognise Compare Represent Compose	Pattern subitise	Recognise Compare Represent Compose	2D/ 3D shapes Height/length Order Number bonds	Recognise Bigger /smaller	Shape numbers bonds	Odd/ even measure	Amount Total Combine Add takeaway
Number Numerical Patterns	<p>Children will know:</p> <ul style="list-style-type: none">And can talk about passage of time through days of the week & months of the year.Children can follow AB ABB patterns.Children can orally count past 10.How to sort objects into different groupsHow to match objects that are the same as another.How to compare amounts into using smaller/smallest/ fewer/fewest		<p>Children will know:</p> <ul style="list-style-type: none">How to identify numbers 1 2,3,4 and 5.How to represent numbers 1 2 3 4 and 5How to compare numbers 1 2 3 4 and 5How to compose numbers 1 2 3 4 and 5How to use some positional language to describe the position of an object.How to recognise triangles and circles in different shapes and pictures.Children are able to recognise some numbers 0-10.		<p>Children will know:</p> <ul style="list-style-type: none">How to recognise numbers 4 and 5How to compare numbers 4 and 5How to represent numbers 4 and 5How to compose numbers 4 and 5Children can create & follow AB ABB patterns & be able to spot the rule.Children can orally count to 20 <p>Children can use units when measuring & comparing (weight, length capacity).</p> <p>Children can subitise to 5.</p>		<p>Children will know:</p> <ul style="list-style-type: none">How to recognise numbers 6 7 8 and 9How to represent numbers 6 7 8 and 9How to compare numbers 6 7 8 and 9How to compose numbers 6 7 8 and 9How to combine 2 groups together.How to compare objects for height and length using mathematical language.How to order 2 objects for height and length using mathematical languageChildren can describe properties of 2D and 3D shapes using mathematical language.Number bonds to 10.		<p>Children will know:</p> <ul style="list-style-type: none">How to recognise numbers to 20.Recognise patterns in numbers beyond 10. .Be able to name & recognise a range of numbers up to 10 & represent these numbers in various different ways.number bonds to 10How two add groups together.How to take away a smaller number from a bigger number to 10.Children are developing an awareness of shape, recognising shapes within shapes.		<p>Children will know:</p> <ul style="list-style-type: none">How to double a number to 10.How to share an equal amount between two or more groups.children can use mathematical language when comparing & measuring practically.How to spot & discuss simple number patterns such as odd & even numbers.Children are using units to measure & compare.	
<p>Early Learning Goals:</p> <ul style="list-style-type: none">Have a deep understanding of number to 10, including the composition of each number.Subitise (recognise quantities without counting) up to 5.Automatically recall (without reference to rhymes, counting or other aids). Number bonds up to 5 (including subtraction facts) & some number bonds to 10, including doublesVerbally count beyond 20, recognising the pattern of the counting system.Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity.Explore & represent patterns within numbers up to 10, including evens & odds, double facts & how quantities can be distributed equally.												

Mathematics – Arithmetic progression

Foundation stage 2:

I can count to 20 verbally from 0.
I can count back from 20 to 0.
I can count on or back from 0 to 20 starting from different points.
I can touch count starting verbally from 0 total amounts of objects to 10.
I can touch count starting verbally from 0 total amounts of objects to 20.
I can recognise digits to 10 in and out of order (rapid recall).
I can recognise digits to 20 in and out of order (rapid recall).
I can link a numeral to a cardinal number (amount) for each digit 0 – 3.
I can link a numeral to a cardinal number (amount) for each digit 3-5.
I can link a numeral to a cardinal number (amount) for each digit 5 - 10.
I can show number fingers to 3.
I can show number fingers to 5.
I can show number fingers to 10.
I can subitise to 3 WITHOUT counting.
I can subitise to 5 WITHOUT counting.
I can subitise to 10 WITHOUT counting.
I can write digits to 0-3.
I can write digits to 3-5.
I can write digits to 5-10.
I can write digits to 10 – 13 naming them correctly.
I can write digits to 13 – 15 naming them correctly.
I can write digits to 15 – 20 naming them correctly.
I can compare numbers and amounts using greater than, less than, equal to.
I can recognise the + symbol.

I can recognise the – symbol.
I can recognise the = symbol.
I know all numbers bonds to 5 (record small steps 1, 2, 3, 4, 5)
I know all numbers bonds to 10 (record small steps 6, 7, 8, 9 and 10)
I know all my doubles to 3/ 5/ 10.
I can count to say one more than any number 0 – 5/5 -10/ 10-15/ 15-20.
I can count to say one less than any number 0 – 5/5 -10/ 10-15/ 15-20.
I can add a 1-digit number to a 1-digit number.
I can subtract a 1-digit numbers from a 1-digit number
I can add a 1-digit number to a 2-digit number.
I can subtract 1-digit numbers from a 2-digit number
I can recognise simple 2D shapes.
I can draw a simple map.
I can use below, above, next to, in front, behind in relation to positions (sometimes on a simple map)
I can compare weight of objects.
I can compare length of objects.
I can use the vocabulary first, then, next to sequence time.
I can name the days of the week.
I can name the months of the year.
I can name the months of the year.

Year 1:

I can count 0 – 50.
I can count 50 – 100.
I can count back from 50 – 0.
I can count back from 100 – 0.
I can count on or back from 0 to 100 starting from different points.
I can recognise digits to 30/50/100 in and out of order (rapid recall).
I can recognise the tens in a 2-digit number. I can represent this.
I can recognise the ones in a 2-digit number. I can represent this.
I know all numbers bonds to 10 (record small steps 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 and 10)
I can count on/back in 2s to 24.
I can count on/back in 5s to 60.
I can count on/back in 10s to 100.
I can count 1 more with objects by counting or using a number line
I can count 1 more from any given number 0 –100.
I can count 1 less with objects by counting or using a number line
I can count 1 less from any given number 100 – 0.
I can form digits to 10 without reversals.
I can form digits to 20 without reversals.
I can recognise the + symbol.
I can recognise the – symbol.
I can recognise the = symbol.
I can add two 1-digit numbers.
I can add a 1-digit number to a 2-digit number.
I can subtract two 1-digit numbers.
I can subtract a 1-digit number from a 2-digit number.
I can solve missing number problems.
I can recognise ALL 2D shapes.

I can recognise ALL 3D shapes.
I can recognise and represent a half turn.
I can recognise and represent a full turn.
I can recognise $\frac{1}{2}$ of a shape, quantity or number.
I can recognise $\frac{1}{4}$ of a shape, quantity or number.
I can recognise and read the hour on a clock.
I can recognise and read half past/quarter past on a clock.
I can name the days of the week.
I can name the months of the year.

Year 2:

I can count forwards and backwards to/from 100 verbally from any given number.
I can count forwards and backwards to/from 100 verbally from any given number.
I can recognise digits to 100 (rapid recall)
I can recognise the tens in a 2-digit number. I can represent this.
I can recognise the ones in a 2-digit number. I can represent this.
I know ALL number bonds to 20 (0 – 5, 5 – 10, 10 – 15, 15 – 20.)
I can count on/back in 2s to 24 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 2s (from 0x to 12x/ in reverse)
Recall 2 times table facts in and out of order at pace.
I can count on/back in 5s to 60 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 5s (from 0x to 12x/ in reverse)
Recall 5x facts in and out of order.
I can count on/back in 10s to 100 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 10s. (from 0x to 12x/ in reverse)
Recall 10x facts in and out of order.
I can count on/back in 3s to 36 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 3s (from 0x to 12x/ in reverse)
Recall 3x facts in and out of order.
I can count 1 more with objects by counting or using a number line/hundred square
I can count 1 more from any given number 0 – 100 beginning to bridge past 100.
I can count 1 less from any given number 100 – 0 beginning to bridge past 100.
I can form digits correctly to 10/20/50/100 with no reversals.
I can recognise the +/ -/ = symbol.
I can recognise the X symbol.
I can recognise the ÷ symbol.
I can add a two-digit and 1-digit number with NO exchanging.
I can add a two-digit and 1-digit numbers WITH exchanging.

I can subtract a two-digit and 1-digit numbers with NO exchanging.
I can subtract a two-digit and 1-digit numbers WITH exchanging.
I can add two, two-digit numbers with NO exchanging.
I can add two, two-digit numbers WITH exchanging.
I can subtract two, two-digit numbers with NO exchanging.
I can subtract two, two-digit numbers WITH exchanging.
I can multiply a 1 digit number by a 1 digit number using arrays.
I can multiply a 2 digit number by a 1 digit number using arrays.
I can divide a 2 digit number by a 1 digit number with NO remainders.
I can recognise ALL 2D shapes.
I can recognise ALL 3D shapes.
I can recognise and represent a half turn.
I can recognise and represent a full turn.
I can recognise $\frac{1}{2}$ $\frac{1}{4}$ and $\frac{1}{3}$ of a shape, quantity or number.
I can recognise $\frac{2}{4}$ and $\frac{3}{4}$ of a shape, quantity or number.
I can recognise and read the hour on a clock.
I can recognise and read half past/quarter past on a clock.
I know the number of minutes in an hour and hours in a day.

Year 3:

I can recognise numbers to 100 (rapid recall)
I can recognise numbers to 500 (rapid recall)
I can recognise numbers to 1000 (rapid recall)
I can write numbers to 100.
I can write numbers to 500.
I can write numbers to 1000.
I know all number bonds to 10 (record small steps 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 and 10)
I know ALL number bonds to 20. (record small steps 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20)
I can count in 2s to 24 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 2s.
I can count in 3s to 36 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 3s.
I can count in 4s to 48 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 4s.
I can count in 5s to 60 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 5s.
I can count in 8s to 96 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 8s.
I can count in 10s to 100 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 10s.
I can count in 50s and 100s (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 50s.
I can recognise hundreds, tens and ones in a 3 digit number.
I can compare and order numbers to 100.
I can compare and order numbers to 1000.
I can form numbers to 10 correctly without reversals.
I can form numbers to 50 correctly without reversals.

I can form numbers to 100 correctly without reversals.
I can form ALL numbers correctly.
I can use manipulatives to represent numbers to 100.
I can use manipulatives to represent numbers to 1000.
I can recognise the $+$ $-$ \times \div symbol.
I can add/subtract 1 to a number mentally.
I can add/subtract 10 to a number mentally.
I can add/subtract 100 to a number mentally.
I can add two/three digit numbers with NO exchanging.
I can add two/three digit numbers WITH exchanging.
I can subtract two/three digit numbers with NO exchanging.
I can subtract two/three digit numbers WITH exchanging.
I can multiply a 2 digit number by a 1 digit number.
I can multiply two numbers using 2/ 5/ 10 times table facts.
I can multiply two numbers using 3 times table facts.
I can multiply two numbers using 4 times table facts.
I can multiply two numbers using 8 times table facts.
I can divide a 2 digit number by a 1 digit number with NO remainders.
I can divide a 2 digit number by a 1 digit number with WITH remainders.
I can recognise and use commutativity to solve problems.
I can recognise ALL 2D and 3D shapes.
I can recognise horizontal, vertical and parallel lines.
I can recognise a right angle.
I can measure the perimeter of a 2D shape.
I can recognise $\frac{1}{2}$ $\frac{1}{4}$ $\frac{1}{3}$ $\frac{2}{4}$ $\frac{3}{4}$ of a shape, quantity or number.
I can order fractions in a linear system.
I can add fractions with the same denominator.
I can subtract fractions with the same denominator.

I can recognise and read the hour and minutes on a clock.
I can recognise all coins and notes.

Year 4:

I can write numbers to 100 and form them correctly.
I can write numbers to 500 and form them correctly.
can write numbers to 1000 and form them correctly.
I can count backwards through 0 to include negatives up to -10
I can count backwards through 0 to include negatives beyond -10
I can count in 2s to 24
I can count in 2s to 100 (different starting points numbers).
I can count in 2s beyond 100 (different starting points.)
Recall of associated times tables facts for 2s.
I can count in 3s to 36
I can count in 3s to 100 (different starting points numbers).
I can count in 3s beyond 100 (different starting points.)
Recall of associated times tables facts for 3s.
I can count in 4s to 48 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 4s.
I can count in 5s to 60 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 5s.
I can count in 6s to 72 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 6s.
I can count in 7s to 84 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 7s.
I can count in 8s to 96 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 8s.
I can count in 9s to 108 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 9s.
I can count in 10s to 120 (and beyond/ different starting points/ into 3-digit numbers).

Recall of associated times tables facts for 10s.
I can count in 100s to 1,200 (and beyond/ different starting points/ into 4-digit numbers).
Recall of associated times tables facts for 100s.
I can count in 1000s to 12,000 (and beyond/ different starting points).
Recall of associated times tables facts for 1,000s.
I can recognise thousands, hundreds, tens and ones in a 4 digit number.
I can compare and order numbers to 1000.
I can read roman numerals to 100.
I can use manipulatives to represent numbers to 1000.
I can recognise the $+$ $-$ $=$ $X \div$ symbol.
I can add/subtract 1, 10 and 100 to a number mentally.
I can add two/three/four digit numbers with NO exchanging.
I can add two/three/four digit numbers WITH exchanging.
I can subtract two/three/four digit numbers with NO exchanging.
I can subtract two/three/four digit numbers WITH exchanging.
I can recall multiplication and division facts within 12×12
I can multiply two/three digit numbers by a one digit number.
I can divide a number by another including remainders
I can use commutativity and distributive law to solve problems.
I can solve 2 step problems. (e.g. $3 \times 4 + 6$)
I can recognise ALL 2D and 3D shapes.
I can recognise a right angle, acute and obtuse angles.
I can measure the perimeter and area of a 2D shape.
I can recognise and find a line of symmetry on a 2D shape.
I can convert mixed numbers to improper fractions.
I can add/subtract fractions with the same denominator.
I can add/subtract improper and mixed fractions including bridging.
I can recognise and write decimal equivalents of any number of tenths or hundreds and of $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$

I can draw polygons, specified by coordinates in the first quadrant, and translate within the first quadrant.
I can compare decimal numbers and round them to 1 or 2 places.
I can read, write and convert using analogue and digital clocks.
I can recognise and calculate using all coins and notes.
I can convert between different measures.

Year 5:

I can write numbers to 1000 / 10,000, 100,000 and with the correct number of digits and form them correctly
I can say what each digit represents 1000 / 10,000, 100,000
I can write numbers to 1,000,000 and with the correct number of digits and form them correctly
I can say what each digit represents 1,000,000
I can count forwards and backwards from different starting points up to 1,000,000
I can count forwards and backwards through 0 to include negatives.
I can count forwards and backwards from different starting points e.g. -3 backwards in ones
I can count in 2s to 24 (and beyond/ different starting points/ into 3-digit numbers).
I can count in 2s from different starting numbers, E.g. odd numbers
Recall of associated times tables facts for 2s.
I can count in 3s to 36 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 3s.
I can count in 4s to 48 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 4s.
I can count in 5s to 60 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 5s.
I can count in 6s to 72 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 6s.
I can count in 7s to 84 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 7s.
I can count in 8s to 96 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 8s.
I can count in 9s to 108 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 9s.
I can count in 10s to 120 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 10s.

I can count in 11s to 132 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 11s.
I can count in 12s to 144 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 12s.
I can count in 50s to 600 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 50s.
I can count in 100s to 1,200 (and beyond/ different starting points/ into 4-digit numbers).
Recall of associated times tables facts for 100s.
I can count in 1000s to 12,000 (and beyond/ different starting points).
Recall of associated times tables facts for 1,000s.
I can determine the value of each number within 1,000,000.
I can compare and order numbers to 1,000,000.
I can count forwards or backwards in steps of powers of 10 for any given number up to 1,000,000.
I can read roman numerals to 1000.
I can recognise the $+$ $-$ \times \div symbol.
I can add/subtract 1, 10, 100 and 1000 to a number mentally.
I can add and subtract whole numbers with more than 4 digits
I can use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy
I can multiply and divide using written formats for 2 digits problems.
I can multiply and divide involving decimals by 10, 100 and 1,000
I can solve multi step problems.
I can recall prime numbers to 19 and establish prime numbers to 100.
I can find and recall common factors of numbers.
I can recognise and use squared and cube numbers
I can recognise ALL 2D and 3D shapes.
I can recognise a right angle, acute and obtuse angles.
I can recognise, compare and draw angles given in degrees.
I can measure the perimeter and area of a 2D shape.

I can estimate volume
I can recognise and find a line of symmetry on a 2D shape.
I can convert mixed numbers to improper fractions. (e.g. $\frac{13}{4}$)
I can add/subtract fractions with the same denominator.
I can add/subtract improper and mixed fractions including bridging.
I can recognise mixed numbers and improper fractions and convert from one form to the other
I can recognise and write percentage and decimal equivalents of any number of tenths or hundreds, multiple of 10 or 25 and of $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{5}$, $\frac{2}{5}$, $\frac{4}{5}$
I can draw polygons, specified by coordinates in the first quadrant, and translate within the first quadrant.
I can compare decimal numbers and round them to 1 or 2 places.
I can read, write, order and compare numbers with up to 3 decimal places
I can read, write, convert and solve problems using analogue and digital clocks.
I can recognise and calculate using all coins and notes.
I can convert between different measures.

Year 6:

I can write numbers to 1,000,000 and form them correctly.
I can say what each digit represents 1,000,000
I can write numbers to 10,000,000 and form them correctly.
I can say what each digit represents 10,000,000
I can count forwards through 0 to include negatives.
I can count backwards through 0 to include negatives.
I can count and recall facts within 12x12
I can count in 2s to 24 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 2s.
I can count in 3s to 36 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 3s.
I can count in 4s to 48 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 4s.
I can count in 5s to 60 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 5s.
I can count in 6s to 72 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 6s.
I can count in 7s to 84 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 7s.
I can count in 8s to 96 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 8s.
I can count in 9s to 108 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 9s.
I can count in 10s to 120 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 10s.
I can count in 11s to 132 (and beyond/ different starting points/ into 3-digit numbers).

Recall of associated times tables facts for 11s.
I can count in 12s to 144 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 12s.
I can count in 50s to 600 (and beyond/ different starting points/ into 3-digit numbers).
Recall of associated times tables facts for 50s.
I can count in 100s to 1,200 (and beyond/ different starting points/ into 4-digit numbers).
Recall of associated times tables facts for 100s.
I can count in 1000s to 12,000 (and beyond/ different starting points).
Recall of associated times tables facts for 1,000s.
I can determine the value of each number within 10,000,000.
I can compare and order numbers to 10,000,000.
I can round any whole number to a required degree of accuracy.
I can recognise the + - = \times \div symbol.
I can solve addition and subtraction multi-step problems
I can use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy
I can multiply multi-digit numbers up to 4 digits by a two-digit whole number
I can divide numbers up to 4 digits by a two-digit whole number inc. remainders
I can multiply and divide involving decimals by 10, 100 and 1,000
I can identify common factors, common multiples and prime numbers
I can recognise, describe and build simple 3-D shapes and draw 2D shapes.
I can recognise angles.
I can recognise, compare and draw angles given in degrees.
I can measure the perimeter and area of a shape.
I can estimate and calculate volume
I can name parts of circles, including radius, diameter and circumference
I can use common factors to simplify fractions
I can compare and order fractions, including fractions >1
I can add and subtract fractions with different denominators and mixed numbers
I can multiply simple pairs of proper fractions

I can divide proper fractions by whole numbers
I can associate a fraction with division and calculate decimal fraction equivalents
I can solve problems involving the calculation of percentages
I can solve problems involving similar shapes where the scale factor is known or can be found
I can use simple formulae
I can express missing number problems algebraically
I can find pairs of numbers that satisfy an equation with 2 unknowns
I can enumerate possibilities of combinations of 2 variables
I can read, write, convert and solve problems using analogue and digital clocks.
I can recognise and calculate using all coins and notes.
I can convert between different measures.

Mathematics – Vocabulary progression

Foundation Stage	Number					
	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
zero	number	number	number	number	number	number
number	numeral	numeral	numeral	numeral	numeral	numeral
one, two, three ...	one, two, three ...	one, two, three ...	one, two, three ...	one, two, three ...	one, two, three ...	one, two, three ...
eleven, twelve ...	eleven, twelve ...	eleven, twelve ...	eleven, twelve ...	eleven, twelve ...	eleven, twelve ...	eleven, twelve ...
none	twenty, twenty-one ...	twenty, twenty-one ...	twenty, twenty-one ...	twenty, twenty-one ...	twenty, twenty-one ...	twenty, twenty-one ...
how many ...?	none	one hundred, two hundred ...	one hundred, two hundred ...	one hundred, two hundred ...	one hundred, two hundred ...	one hundred, two hundred ...
count	how many ...?	none	none	none	none	none
count (up) to	count	how many ...?	how many ...?	how many ...?	how many ...?	how many ...?
count on (from, to)	count (up) to	count	count	count	count	count
count back (from, to)	count on (from, to)	count (up) to	count (up) to	count (up) to	count (up) to	count (up) to
	count back (from, to)	count on (from, to)	count on (from, to)	count on (from, to)	count on (from, to)	count on (from, to)
	forwards	count back (from, to)	count back (from, to)	count back (from, to)	count back (from, to)	count back (from, to)
	backwards	forwards	forwards	forwards	forwards	forwards
	count in ones, twos ...	backwards	backwards	backwards	backwards	backwards
	equal to	count in ones, twos ...	count in ones, twos ...	count in ones, twos ...	count in ones, twos ...	count in ones, twos ...
	equivalent to	equal to	equal to	equal to	equal to	equal to
	is the same as	equivalent to	equivalent to	equivalent to	equivalent to	equivalent to
	more/ less	is the same as	is the same as	is the same as	is the same as	is the same as
	most/ least	more/ less	more/ less	more/ less	more/ less	more/ less
	many	most/ least	most/ least	most/ least	most/ least	most/ least
	odd/ even	tally	tally	tally	tally	tally
	multiple of	many	many	many	many	many
	few	odd	odd	odd	odd	odd
	pattern	even	even	even	even	even
	pair	multiple of	multiple of	multiple of	multiple of	multiple of
		sequence	factor of	factor of	factor of	factor of
		continue	sequence	sequence	factor pair	factor pair
		predict	continue	continue	sequence	sequence
		few	predict	predict	continue	continue

		<p>pattern</p> <p>pair</p> <p>rule</p> <p>> greater than</p> <p>< less than</p>	<p>few</p> <p>pattern</p> <p>pair</p> <p>rule</p> <p>relationship</p> <p>> greater than</p> <p>< less than</p> <p>roman numerals</p>	<p>few</p> <p>pattern</p> <p>pair</p> <p>rule</p> <p>relationship</p> <p>next</p> <p>consecutive</p> <p>> greater than</p> <p>< less than</p> <p>roman numerals</p> <p>integer</p> <p>positive</p> <p>negative</p> <p>above (below) zero</p> <p>minus</p> <p>negative numbers</p>	<p>predict</p> <p>few</p> <p>pattern</p> <p>pair</p> <p>rule</p> <p>relationship</p> <p>next</p> <p>consecutive</p> <p>> greater than or equal to</p> <p>< less than or equal to</p> <p>roman numerals</p> <p>integer</p> <p>positive</p> <p>negative</p> <p>above (below) zero</p> <p>minus</p> <p>negative numbers</p> <p>formula</p> <p>divisibility</p> <p>square number</p> <p>prime number</p> <p>ascending</p> <p>descending order</p>	<p>predict</p> <p>few</p> <p>pattern</p> <p>pair</p> <p>rule</p> <p>relationship</p> <p>next</p> <p>consecutive</p> <p>> greater than or equal to</p> <p>< less than or equal to</p> <p>roman numerals</p> <p>integer</p> <p>positive</p> <p>negative</p> <p>above (below) zero</p> <p>minus</p> <p>negative numbers</p> <p>formula</p> <p>divisibility</p> <p>square number</p> <p>prime number</p> <p>factorise</p> <p>prime factor</p> <p>ascending</p> <p>descending order</p> <p>digital total</p>
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Place Value						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
ones	ones	ones	ones	ones	ones	ones
tens	tens	tens	tens	tens	tens	tens
digit	digit	hundreds	hundreds	hundreds	hundreds	hundreds
the same number as	the same number as	digit	digit	digit	digit	digit
as many as	as many as	one-, two-, three-digit number	one-, two-, three-digit number	one-, two-, three-digit number	one-, two-, three-digit number	one-, two-, three-digit number
more	more	place	place	place	place	place
larger	larger	place value	place value	place value	place value	place value
bigger	bigger	stands for	stands for	stands for	stands for	stands for
greater	greater	represents	represents	represents	represents	represents
fewer	fewer	exchange	exchange	exchange	exchange	exchange
smaller	smaller	the same number as	the same number as	the same number as	the same number as	the same number as
less	less	as many as	as many as	as many as	as many as	as many as
fewest	fewest	more	more	more	more	more
smallest	smallest	larger	larger	larger	larger	larger
least	least	bigger	bigger	bigger	bigger	bigger
most	most	greater	greater	greater	greater	greater
biggest	biggest	fewer	fewer	fewer	fewer	fewer
largest	largest	smaller	smaller	smaller	smaller	smaller
greatest	greatest	less	less	less	less	less
one/ ten more	one/ ten more	fewest	fewest	fewest	fewest	fewest
one/ ten less	one/ ten less	smallest	smallest	smallest	smallest	smallest
compare	equal to	least	least	least	least	least
order	compare	most	most	most	most	most
size	order	biggest	biggest	biggest	biggest	biggest
first, second, third Twentieth	size	largest	largest	largest	largest	largest
last, last but one	first, second, third twentieth	greatest	greatest	greatest	greatest	greatest
before	last, last but one	one/ ten more	one/ ten/ hundred more	one/ ten/ hundred/ thousand more	one/ ten/ hundred/ thousand more	one/ ten/ hundred/ thousand more
after	before	one/ ten less	one/ ten/ hundred less	one/ ten/ hundred/ thousand less	one/ ten/ hundred/ thousand less	one/ ten/ hundred/ thousand less
next	after	equal to	equal to			

between	next	compare	compare	equal to	equal to	equal to
	between	order	order	compare	compare	compare
	half-way between	size	size	order	order	order
	above	first, second, third Twentieth	first, second, third Twentieth	size	size	size
	below	twenty-first, twenty-second ...	twenty-first, twenty-second ...	first, second, third Twentieth	first, second, third Twentieth	first, second, third Twentieth
		last, last but one	last, last but one	twenty-first, twenty-second ...	twenty-first, twenty-second ...	twenty-first, twenty-second ...
		before	before	last, last but one	last, last but one	last, last but one
		after	after	before	before	before
		next	next	after	after	after
		between	between	next	next	next
		half-way between	half-way between	between	between	between
		above	above	half-way between	half-way between	half-way between
		below	below	above	above	above
				below	below	below

Estimating						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
guess	guess	guess	guess	guess	guess	guess
how many ...?	how many ...?	how many ...?	how many ...?	how many ...?	how many ...?	how many ...?
estimate	estimate	estimate	estimate	estimate	estimate	estimate
nearly	nearly	nearly	nearly	nearly	nearly	nearly
close to	roughly	roughly	roughly	roughly	roughly	roughly
about the same as	close to	close to	close to	close to	close to	close to
just over	about the same as	about the same as	approximate(ly)	approximate(ly)	approximate(ly)	approximate(ly)
just under	just over	just over	about the same as	about the same as	about the same as	about the same as
too many	just under	just under	just over	just over	just over	just over
too few	too many	exact	just under	just under	just under	just under
enough	too few	exactly	exact	exact	exact	exact
not enough	enough	too many	exactly	exactly	exactly	exactly
	not enough	too few	too many	too many	too many	too many
		enough	too few	too few	too few	too few
		not enough	enough	enough	enough	enough
			not enough	not enough	not enough	not enough
			round	round	round	round
			nearest	nearest	nearest	nearest
			round to the nearest ten/ hundred	round to the nearest ten/ hundred/ thousand	round to the nearest ten/ hundred/ thousand/ ten thousand	round to the nearest ten/ hundred/ thousand/ ten thousand
			round up	round up	round up	round up
			round down	round down	round down	round down

Addition and Subtraction						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
add, more, and	addition	addition	addition	addition	addition	addition
make, sum, total	add, more, and	add, more, and	add, more, and	add, more, and	add, more, and	add, more, and
altogether	make, sum, total	make, sum, total	make, sum, total	make, sum, total	make, sum, total	make, sum, total
double	altogether	altogether	altogether	altogether	altogether	altogether
one more, two more ... ten more	double	double	double	double	double	double
how many more to make ...?	near double	near double	near double	near double	near double	near double
how many more is ... than ...?	half, halve	half, halve	half, halve	half, halve	half, halve	half, halve
how much more is ...?	one more, two more ... ten more	one more, two more ... ten more	one more, two more ... ten more	one more, two more ... ten more	one more, two more ... ten more	one more, two more ... ten more
take away	how many more to make ...?	... one hundred more	... one hundred more	... one hundred more	... one hundred more	... one hundred more
how many have gone?	how many more is ... than ...?	how many more to make ...?	how many more to make ...?	how many more to make ...?	how many more to make ...?	how many more to make ...?
one less, two less, ten less...	how much more is ...?	how many more is ... than ...?	how many more is ... than ...?	how many more is ... than ...?	how many more is ... than ...?	how many more is ... than ...?
how many fewer is ... than ...?	subtract	how much more is ...?	how much more is ...?	how much more is ...?	how much more is ...?	how much more is ...?
how much less is ...?	take away	subtract	subtract	subtract	subtract	subtract
difference between	how many have gone?	take away	take away	take away	take away	take away
	one less, two less, ten less...	how many have gone?	how many have gone?	how many have gone?	how many have gone?	how many have gone?
	how many fewer is ... than ...?	one less, two less, ten less ... one hundred less	one less, two less, ten less ... one hundred less	one less, two less, ten less ... one hundred less	one less, two less, ten less ... one hundred less	one less, two less, ten less ... one hundred less
	how much less is ...?	how many fewer is ... than ...?	how many fewer is ... than ...?	how many fewer is ... than ...?	how many fewer is ... than ...?	how many fewer is ... than ...?
	difference between	how much less is ...?	how much less is ...?	how much less is ...?	how much less is ...?	how much less is ...?
	equals	difference between	difference between	difference between	difference between	difference between
	is the same as	equals	equals	equals	equals	equals
	number bonds/pairs	is the same as	is the same as	is the same as	is the same as	is the same as
	missing number	number bonds/pairs/ facts	number bonds/pairs/ facts	number bonds/pairs/ facts	number bonds/pairs/ facts	number bonds/pairs/ facts
		tens boundary	tens boundary, hundreds boundary	tens boundary, hundreds boundary	tens boundary, hundreds boundary, ones boundary, tenths boundary	tens boundary, hundreds boundary, ones boundary, tenths boundary
		missing number	missing number	missing number	missing number	missing number
			inverse	inverse	inverse	inverse

Multiplication and Division						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
sharing	multiplication	multiplication	multiplication	multiplication	multiplication	multiplication
doubling	multiply	multiply	multiply	multiply	multiply	multiply
halving	multiplied by	multiplied by	multiplied by	multiplied by	multiplied by	multiplied by
number patterns	multiple	multiple	multiple, factor	multiple, factor	multiple, factor	multiple, factor
	division	groups of	groups of	groups of	groups of	groups of
	dividing	times	times	times	times	times
	grouping	once, twice, three times ... ten times	product	product	product	product
	sharing	repeated addition	once, twice, three times ... ten times	once, twice, three times ... ten times	once, twice, three times ... ten times	once, twice, three times ... ten times
	doubling	division	repeated addition	repeated addition	repeated addition	repeated addition
	halving	dividing, divide, divided by, divided into	division	division	division	division
	array	grouping	dividing, divide, divided by, divided into	dividing, divide, divided by, divided into	dividing, divide, divided by, divided into	dividing, divide, divided by, divided into
	number patterns	sharing, share, share equally	grouping	grouping	grouping	grouping
		left, left over	sharing, share, share equally	sharing, share, share equally	sharing, share, share equally	sharing, share, share equally
		one each, two each, three each ... ten each	left, left over, remainder	left, left over, remainder	left, left over, remainder	left, left over, remainder
		group in pairs, threes ... tens	one each, two each, three each ... ten each	one each, two each, three each ... ten each	one each, two each, three each ... ten each	one each, two each, three each ... ten each
		equal groups of	group in pairs, threes ... tens	group in pairs, threes ... tens	group in pairs, threes ... tens	group in pairs, threes ... tens
		doubling	equal groups of	equal groups of	equal groups of	equal groups of
		halving	doubling	doubling	doubling	doubling
		array	halving	halving	halving	halving
		row, column	array	array	array	array
		number patterns	row, column	row, column	row, column	row, column
		multiplication table	number patterns	number patterns	number patterns	number patterns
		multiplication fact, division fact	multiplication table	multiplication table	multiplication table	multiplication table
			multiplication fact, division fact	multiplication fact, division fact	multiplication fact, division fact	multiplication fact, division fact
				inverse	inverse	inverse
				square, squared	square, squared	square, squared
				cube, cubed	cube, cubed	cube, cubed

Fractions						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
parts of a whole	fraction	fraction	fraction	fraction	fraction, proper/improper fraction	fraction, proper/improper fraction
half	equal part	equivalent fraction	equivalent fraction	equivalent fraction	equivalent fraction	equivalent fraction
quarter	equal grouping	mixed number	mixed number	mixed number	mixed number	mixed number
	equal sharing	numerator, denominator	numerator, denominator	numerator, denominator	numerator, denominator	numerator, denominator
parts of a whole	equal part	equal part	equal part	equal part	equivalent, reduced to, cancel	equivalent, reduced to, cancel
half	equal grouping	equal grouping	equal grouping	equal grouping	equal part	equal part
one of two equal parts	equal sharing	parts of a whole	parts of a whole	parts of a whole	equal grouping	equal grouping
quarter	parts of a whole	half, two halves	half, two halves	half, two halves	equal sharing	equal sharing
one of four equal parts	one of two equal parts	one of two equal parts	one of two equal parts	one of two equal parts	parts of a whole	parts of a whole
	quarter, two quarters, three quarters	quarter, two quarters, three quarters	quarter, two quarters, three quarters	quarter, two quarters, three quarters	half, two halves	half, two halves
	one of four equal parts	one of four equal parts	one of four equal parts	one of four equal parts	one of two equal parts	one of two equal parts
	one third, two thirds	one third, two thirds	one third, two thirds	one third, two thirds	quarter, two quarters, three quarters	quarter, two quarters, three quarters
	one of three equal parts	one of three equal parts	one of three equal parts	one of three equal parts	one of four equal parts	one of four equal parts
		sixths, sevenths, eighths, tenths ...	sixths, sevenths, eighths, tenths ...	sixths, sevenths, eighths, tenths ...	one third, two thirds	one third, two thirds
			... hundredths	... hundredths	one of three equal parts	one of three equal parts
			decimal, decimal fraction, decimal point, decimal place, decimal equivalent	decimal, decimal fraction, decimal point, decimal place, decimal equivalent	sixths, sevenths, eighths, tenths ... hundredths, thousandths	sixths, sevenths, eighths, tenths ... hundredths, thousandths
			proportion	proportion	decimal, decimal fraction, decimal point, decimal place, decimal equivalent	decimal, decimal fraction, decimal point, decimal place, decimal equivalent
					proportion, in every, for every	proportion, in every, for every
					percentage, per cent, %	ratio
						percentage, per cent, %

Algebra						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
						formula, formulae equation unknown variable

Measurement						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
measure	measure	measure	measure	measure	measure	measure
size	measurement	measurement	measurement	measurement	measurement	measurement
compare	size	size	size	size	size	size
guess, estimate	compare	compare	compare	compare	compare	compare
enough, not enough	guess, estimate	measuring scale	measuring scale, division	unit, standard unit	unit, standard unit	unit, standard unit
too much, too little	enough, not enough	guess, estimate	guess, estimate	metric unit	metric unit, imperial unit	metric unit, imperial unit
too many, too few	too much, too little	enough, not enough	enough, not enough	measuring scale, division	measuring scale, division	measuring scale, division
nearly, close to, about the same as	too many, too few	too much, too little	too much, too little	guess, estimate	guess, estimate	guess, estimate
just over, just under	nearly, close to, about the same as	too many, too few	too many, too few	enough, not enough	enough, not enough	enough, not enough
	roughly	nearly, close to, about the same as	nearly, close to, about the same as, approximately	too much, too little	too much, too little	too much, too little
	just over, just under	roughly	roughly	too many, too few	too many, too few	too many, too few
		just over, just under	just over, just under	nearly, close to, about the same as, approximately	nearly, close to, about the same as, approximately	nearly, close to, about the same as, approximately
				roughly	roughly	roughly
				just over, just under	just over, just under	just over, just under

Length						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
metre	centimetre, metre	centimetre, metre	millimetre, centimetre, metre, kilometre, mile	millimetre, centimetre, metre, kilometre, mile	millimetre, centimetre, metre, kilometre, mile	millimetre, centimetre, metre, kilometre, mile, yard, foot, feet, inch, inches
length, height, width, depth	length, height, width, depth	length, height, width, depth	length, height, width, depth	length, height, width, depth, breadth	length, height, width, depth, breadth	length, height, width, depth, breadth
long, short, tall	long, short, tall	long, short, tall	long, short, tall	long, short, tall	long, short, tall	long, short, tall
high, low	high, low	high, low	high, low	high, low	high, low	high, low
wide, narrow	wide, narrow	wide, narrow	wide, narrow	wide, narrow	wide, narrow	wide, narrow
thick, thin	thick, thin	thick, thin	thick, thin	thick, thin	thick, thin	thick, thin
longer, shorter, taller, higher	longer, shorter, taller, higher	longer, shorter, taller, higher	longer, shorter, taller, higher	longer, shorter, taller, higher	longer, shorter, taller, higher	longer, shorter, taller, higher
longest, shortest, tallest, highest	longest, shortest, tallest, highest	longest, shortest, tallest, highest	longest, shortest, tallest, highest	longest, shortest, tallest, highest	longest, shortest, tallest, highest	longest, shortest, tallest, highest
far, near, close	far, near, close	far, further, furthest, near, close	far, further, furthest, near, close	far, further, furthest, near, close	far, further, furthest, near, close	far, further, furthest, near, close
	ruler	ruler	distance apart ... between ... to ... from	distance apart ... between ... to ... from	distance apart ... between ... to ... from	distance apart ... between ... to ... from
	metre stick	metre stick, tape measure	perimeter	edge, perimeter	edge, perimeter	edge, perimeter, circumference
			ruler	area, covers	area, covers	area, covers
			metre stick, tape measure	square centimetre (cm ²)	square centimetre (cm ²), square metre (m ²), square millimetre (mm ²)	square centimetre (cm ²), square metre (m ²), square millimetre (mm ²)
				ruler	ruler	ruler
				metre stick, tape measure	metre stick, tape measure	metre stick, tape measure

Weight						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
weigh, weighs, balances	kilogram, half kilogram	kilogram, half kilogram, gram	kilogram, half kilogram, gram	mass: big, bigger, small, smaller	mass: big, bigger, small, smaller	mass: big, bigger, small, smaller
heavy, light	weigh, weighs, balances	weigh, weighs, balances	weigh, weighs, balances	weight: heavy/light, heavier/lighter, heaviest, lightest	weight: heavy/light, heavier/lighter, heaviest, lightest	weight: heavy/light, heavier/lighter, heaviest, lightest
heavier than, lighter than	heavy, light	heavy, light	heavy, light	kilogram, half kilogram, gram	kilogram, half kilogram, gram	tonne, kilogram, half kilogram, gram, pound, ounce
heaviest, lightest	heavier than, lighter than	heavier than, lighter than	heavier than, lighter than	weigh, weighs, balances	weigh, weighs, balances	weigh, weighs, balances
scales	heaviest, lightest	heaviest, lightest	heaviest, lightest	heavy, light	heavy, light	heavy, light
	scales	scales	scales	heavier than, lighter than	heavier than, lighter than	heavier than, lighter than
				heaviest, lightest	heaviest, lightest	heaviest, lightest
				scales	scales	scales

Capacity and Volume						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
full	litre, half litre	litre, half litre, millilitre	litre, half litre, millilitre	litre, half litre, millilitre	litre, half litre, millilitre	litre, half litre, millilitre, centilitre
empty	capacity	capacity	capacity	capacity	capacity	cubic centimetres (cm ³), cubic metres (m ³), cubic millimetres (mm ³), cubic kilometres (km ³)
half full	volume	volume	volume	volume	volume	
holds	full	full	full	full	full	capacity
container	empty	empty	empty	empty	empty	volume
	more than	more than	more than	more than	more than	full
	less than	less than	less than	less than	less than	empty
	half full	half full	half full	half full	half full	more than
	quarter full	quarter full	quarter full	quarter full	quarter full	less than
	holds	holds, contains	holds, contains	holds, contains	holds, contains	half full
	container	container	container	container, measuring cylinder	container, measuring cylinder	quarter full
					pint, gallon	holds, contains
						container, measuring cylinder
						pint, gallon

Temperature						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
		temperature	temperature	temperature	temperature	temperature
		degree	degree	degree	degree	degree
			centigrade	centigrade	centigrade	centigrade

Time						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
time	time	time	time	time	time	time
days of the week (Monday, Tuesday...)	days of the week, (Monday, Tuesday...)	days of the week, (Monday, Tuesday...)	days of the week, (Monday, Tuesday...)	days of the week, (Monday, Tuesday...)	days of the week, (Monday, Tuesday...)	days of the week, (Monday, Tuesday...)
day, week	months of the year (January, February ...)	months of the year (January, February ...)	months of the year (January, February ...)	months of the year (January, February ...)	months of the year (January, February ...)	months of the year (January, February ...)
birthday, holiday	seasons: spring, summer, autumn, winter	seasons: spring, summer, autumn, winter	seasons: spring, summer, autumn, winter	seasons: spring, summer, autumn, winter	seasons: spring, summer, autumn, winter	seasons: spring, summer, autumn, winter
morning, afternoon, evening, night	day, week, weekend, month, year	day, week, weekend, fortnight, month, year	day, week, weekend, fortnight, month, year, century	day, week, weekend, fortnight, month, year, leap year, century, millenium	day, week, weekend, fortnight, month, year, leap year, century, millenium	day, week, weekend, fortnight, month, year, leap year, century, millenium
bedtime, dinner time, playtime	birthday, holiday	birthday, holiday	birthday, holiday	birthday, holiday	birthday, holiday	birthday, holiday
today, yesterday, tomorrow	morning, afternoon, evening, night	morning, afternoon, evening, night	morning, afternoon, evening, night	morning, afternoon, evening, night	morning, afternoon, evening, night	morning, afternoon, evening, night
before, after	bedtime, dinner time, playtime	bedtime, dinner time, playtime	bedtime, dinner time, playtime	bedtime, dinner time, playtime	bedtime, dinner time, playtime	bedtime, dinner time, playtime
next, last	today, yesterday, tomorrow	today, yesterday, tomorrow	today, yesterday, tomorrow	today, yesterday, tomorrow	today, yesterday, tomorrow	today, yesterday, tomorrow
now, soon, early, late	before, after	before, after	before, after	before, after	before, after	before, after
quick, quicker, quickest, quickly	earlier, later	earlier, later	earlier, later	earlier, later	earlier, later	earlier, later
slow, slower, slowest, slowly	next, first, last	next, first, last	next, first, last	next, first, last	next, first, last	next, first, last
old, older, oldest	midnight	midnight	midnight	noon, midnight	noon, midnight	noon, midnight
new, newer, newest	date	date	calendar, date	calendar, date, date of birth	calendar, date, date of birth	calendar, date, date of birth
takes longer, takes less time	now, soon, early, late	now, soon, early, late	now, soon, early, late, earliest, latest	now, soon, early, late, earliest, latest	now, soon, early, late, earliest, latest	now, soon, early, late, earliest, latest
hour, o'clock	quick, quicker, quickest, quickly	quick, quicker, quickest, quickly	quick, quicker, quickest, quickly	quick, quicker, quickest, quickly	quick, quicker, quickest, quickly	quick, quicker, quickest, quickly
clock, watch, hands	slow, slower, slowest, slowly	slow, slower, slowest, slowly	slow, slower, slowest, slowly	slow, slower, slowest, slowly	slow, slower, slowest, slowly	slow, slower, slowest, slowly
	old, older, oldest	old, older, oldest	old, older, oldest	old, older, oldest	old, older, oldest	old, older, oldest
	new, newer, newest	new, newer, newest	new, newer, newest	new, newer, newest	new, newer, newest	new, newer, newest
	takes longer, takes less time	takes longer, takes less time	takes longer, takes less time	takes longer, takes less time	takes longer, takes less time	takes longer, takes less time
	how long ago?	how long ago?	how long ago?	how long ago?	how long ago?	how long ago?
	how long will it be to ...?	how long will it be to ...?	how long will it be to ...?	how long will it be to ...?	how long will it be to ...?	how long will it be to ...?
	how long will it take to ...?	how long will it take to ...?	how long will it take to ...?	how long will it take to ...?	how long will it take to ...?	how long will it take to ...?
	how often?	how often?	how often?	how often?	how often?	how often?
	always, never, often, sometimes	always, never, often, sometimes	always, never, often, sometimes	always, never, often, sometimes	always, never, often, sometimes	always, never, often, sometimes
	usually	usually	usually	usually	usually	usually

	<p>once, twice</p> <p>hour, o'clock, half past, quarter past, quarter to</p> <p>clock, clock face, watch, hands</p> <p>hour hand, minute hand</p> <p>hours, minutes</p>	<p>once, twice</p> <p>hour, o'clock, half past, quarter past, quarter to</p> <p>5, 10, 15 ... minutes past</p> <p>clock, clock face, watch, hands</p> <p>digital/analogue clock/watch, timer</p> <p>hour hand, minute hand</p> <p>hours, minutes, seconds</p>	<p>usually</p> <p>once, twice</p> <p>hour, o'clock, half past, quarter past, quarter to</p> <p>5, 10, 15 ... minutes past</p> <p>a.m., p.m.</p> <p>clock, clock face, watch, hands</p> <p>digital/analogue clock/watch, timer</p> <p>hour hand, minute hand</p> <p>hours, minutes, seconds</p> <p>roman numerals</p> <p>12-hour clock time, 24-hour clock time</p>	<p>usually</p> <p>once, twice</p> <p>hour, o'clock, half past, quarter past, quarter to</p> <p>5, 10, 15 ... minutes past</p> <p>a.m., p.m.</p> <p>clock, clock face, watch, hands</p> <p>digital/analogue clock/watch, timer</p> <p>hour hand, minute hand</p> <p>hours, minutes, seconds</p> <p>timetable, arrive, depart</p> <p>roman numerals</p> <p>12-hour clock time, 24-hour clock time</p>	<p>usually</p> <p>once, twice</p> <p>hour, o'clock, half past, quarter past, quarter to</p> <p>5, 10, 15 ... minutes past</p> <p>a.m., p.m.</p> <p>clock, clock face, watch, hands</p> <p>digital/analogue clock/watch, timer</p> <p>hour hand, minute hand</p> <p>hours, minutes, seconds</p> <p>timetable, arrive, depart</p> <p>roman numerals</p> <p>12-hour clock time, 24-hour clock time</p>	<p>usually</p> <p>once, twice</p> <p>hour, o'clock, half past, quarter past, quarter to</p> <p>5, 10, 15 ... minutes past</p> <p>a.m., p.m.</p> <p>clock, clock face, watch, hands</p> <p>digital/analogue clock/watch, timer</p> <p>hour hand, minute hand</p> <p>hours, minutes, seconds</p> <p>timetable, arrive, depart</p> <p>roman numerals</p> <p>12-hour clock time, 24-hour clock time</p> <p>Greenwich Mean Time, British Summer Time, International Date Line</p>
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Money						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
money	money	money	money	money	money	money
coin	coin	coin	coin	coin	coin	coin
penny, pence, pound	penny, pence, pound	penny, pence, pound	penny, pence, pound	penny, pence, pound	penny, pence, pound	penny, pence, pound
price, cost	price, cost	price, cost	price, cost	price, cost	price, cost	price, cost
buy, sell	buy, sell	buy, bought, sell, sold	buy, bought, sell, sold	buy, bought, sell, sold	buy, bought, sell, sold	buy, bought, sell, sold
spend, spent	spend, spent	spend, spent	spend, spent	spend, spent	spend, spent	spend, spent
pay	pay	pay	pay	pay	pay	pay
	change	change	change	change	change	change
	dear, costs more	dear, costs more	dear, costs more	dear, costs more	dear, costs more	dear, costs more
	cheap, costs less, cheaper	cheap, costs less, cheaper	cheap, costs less, cheaper	cheap, costs less, cheaper	cheap, costs less, cheaper	cheap, costs less, cheaper
	costs the same as	costs the same as	costs the same as	costs the same as	costs the same as	costs the same as
	how much ...?	how much ...?	how much ...?	how much ...?	how much ...?	how much ...?
	how many ...?	how many ...?	how many ...?	how many ...?	how many ...?	how many ...?
	total	total	total	total	total	total
					discount	discount
					currency	currency
						profit, loss

Properties of Shape						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
shape, pattern	shape, pattern	shape, pattern	shape, pattern	shape, pattern	shape, pattern	shape, pattern
flat	flat	flat	flat	flat, line	flat, line	flat, line
curved, straight	curved, straight	curved, straight	curved, straight	curved, straight	curved, straight	curved, straight
round	round	round	round	round	round	round
hollow, solid	hollow, solid	hollow, solid	hollow, solid	hollow, solid	hollow, solid	hollow, solid
sort	sort	sort	sort	sort	sort	sort
make, build, draw	make, build, draw	make, build, draw	make, build, draw	make, build, construct, draw, sketch	make, build, construct, draw, sketch	make, build, construct, draw, sketch
size	size	surface	perimeter	perimeter	perimeter	perimeter
bigger, larger, smaller	bigger, larger, smaller	size	surface	centre	centre, radius, diameter	centre, radius, diameter
symmetrical	symmetry, symmetrical, symmetrical pattern	bigger, larger, smaller	size	surface	surface	circumference, concentric, arc, net, open, closed
pattern, repeating pattern	pattern, repeating pattern	symmetry, symmetrical, symmetrical pattern, line symmetry	bigger, larger, smaller	angle, right-angled	angle, right-angled	surface
match	match	pattern, repeating pattern	symmetry, symmetrical, symmetrical pattern, line symmetry	base, square-based	congruent	angle, right-angled
		match	pattern, repeating pattern	size	base, square-based	congruent
			match	bigger, larger, smaller	size	intersecting, intersection
				symmetry, symmetrical, symmetrical pattern, line symmetry	bigger, larger, smaller	plane
				reflect, reflection	symmetry, symmetrical, symmetrical pattern, line symmetry	base, square-based
				pattern, repeating pattern	reflect, reflection	size
				match	axis of symmetry, reflective symmetry	bigger, larger, smaller
				regular, irregular	pattern, repeating pattern	symmetry, symmetrical, symmetrical pattern, line symmetry
					match	reflect, reflection
					regular, irregular	axis of symmetry, reflective symmetry
						pattern, repeating pattern
						match
						regular, irregular

2-D Shape						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
vertex, vertices, edge	vertex, vertices, edge	vertex, vertices, edge	vertex, vertices, edge	2-D, two-dimensional	2-D, two-dimensional	2-D, two-dimensional
rectangle (including square)	point, pointed	point, pointed	point, pointed	vertex, vertices, edge	vertex, vertices, edge	vertex, vertices, edge
circle	rectangle (including square)	rectangle (including square), rectangular	rectangle (including square), rectangular	point, pointed	point, pointed	point, pointed
triangle	circle	circle, circular	circle, circular	rectangle (including square), rectangular, oblong	rectangle (including square), rectangular, oblong	rectangle (including square), rectangular, oblong
	triangle	triangle, triangular	triangle, triangular	rectilinear	rectilinear	rectilinear
		pentagon	pentagon, pentagonal	circle, circular	circle, circular	circle, circular
		hexagon	hexagon, hexagonal	triangle, triangular	triangle, triangular	triangle, triangular
		octagon	octagon, octagonal	equilateral triangle, isosceles triangle, scalene triangle	equilateral triangle, isosceles triangle, scalene triangle	equilateral triangle, isosceles triangle, scalene triangle
			quadrilateral	pentagon, pentagonal	pentagon, pentagonal	pentagon, pentagonal
			right-angled	hexagon, hexagonal	hexagon, hexagonal	hexagon, hexagonal
			parallel, perpendicular	heptagon	heptagon	heptagon
				octagon, octagonal	octagon, octagonal	octagon, octagonal
				quadrilateral	quadrilateral	quadrilateral
				parallelogram, rhombus, trapezium	parallelogram, rhombus, trapezium	parallelogram, rhombus, trapezium, kite
				polygon	polygon	polygon
				right-angled	right-angled	right-angled
				parallel, perpendicular	parallel, perpendicular	parallel, perpendicular
					x-axis, y-axis, quadrant	x-axis, y-axis, quadrant

3-D Shape						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
face, edge, vertex, vertices	face, edge, vertex, vertices	face, edge, vertex, vertices	face, edge, vertex, vertices	3-D, three-dimensional	3-D, three-dimensional	3-D, three-dimensional
cube	cube, cuboid	cube, cuboid	cube, cuboid	face, edge, vertex, vertices	face, edge, vertex, vertices	face, edge, vertex, vertices
pyramid	pyramid	pyramid	pyramid	cube, cuboid	cube, cuboid	cube, cuboid
sphere	sphere	sphere	sphere, hemisphere	pyramid	pyramid	pyramid
cone	cone	cone	cone	sphere, hemisphere, spherical	sphere, hemisphere, spherical	sphere, hemisphere, spherical
	cylinder	cylinder	cylinder	cone	cone	cone
			prism, triangular prism	cylinder, cylindrical	cylinder, cylindrical	cylinder, cylindrical
				prism, triangular prism	prism, triangular prism	prism, triangular prism
				tetrahedron, polyhedron	tetrahedron, polyhedron	tetrahedron, polyhedron
					octahedron	octahedron
						dodecahedron
						net, open, closed

Position and Direction						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
position	position	position	position	position	position	position
over, under	over, under, underneath	over, under, underneath	over, under, underneath	over, under, underneath	over, under, underneath	over, under, underneath
above, below	above, below	above, below	above, below	above, below	above, below	above, below
top, bottom, side	top, bottom, side	top, bottom, side	top, bottom, side	top, bottom, side	top, bottom, side	top, bottom, side
on, in	on, in	on, in	on, in	on, in	on, in	on, in
outside, inside	outside, inside	outside, inside	outside, inside	outside, inside	outside, inside	outside, inside
around	around	around	around	around	around	around
in front, behind	in front, behind	in front, behind	in front, behind	in front, behind	in front, behind	in front, behind
front, back	front, back	front, back	front, back	front, back	front, back	front, back
beside, next to	beside, next to	beside, next to	beside, next to	beside, next to	beside, next to	beside, next to
opposite	opposite	opposite	opposite	opposite	opposite	opposite
apart	apart	apart	apart	apart	apart	apart
between	between	between	between	between	between	between
middle, edge	middle, edge	middle, edge	middle, edge	middle, edge	middle, edge	middle, edge
corner	centre	centre	centre	centre	centre	centre
direction	corner	corner	corner	corner	corner	corner
left, right	direction	direction	direction	direction	direction	direction
up, down	journey	journey, route	journey, route	journey, route	journey, route	journey, route
forwards, backwards, sideways	left, right	left, right	left, right	left, right	left, right	left, right
across	up, down	up, down	up, down	up, down	up, down	up, down
next to, close, near, far	forwards, backwards, sideways	higher, lower	higher, lower	higher, lower	higher, lower	higher, lower
along	across	forwards, backwards, sideways	forwards, backwards, sideways	forwards, backwards, sideways	forwards, backwards, sideways	forwards, backwards, sideways
through	next to, close, near, far	across	across	across	across	across
to, from, towards, away from	along	next to, close, near, far	next to, close, near, far	next to, close, near, far	next to, close, near, far	next to, close, near, far
movement	through	along	along	along	along	along
slide	to, from, towards, away from	through	through	through	through	through
roll	movement	to, from, towards, away from	to, from, towards, away from	to, from, towards, away from	to, from, towards, away from	to, from, towards, away from
turn	slide	clockwise, anticlockwise	clockwise, anticlockwise	clockwise, anticlockwise	clockwise, anticlockwise	clockwise, anticlockwise
stretch, bend	roll	movement	compass point	compass point	compass point	compass point

whole turn, half turn	turn stretch, bend whole turn, half turn, quarter turn, three-quarter turn	slide roll turn stretch, bend whole turn, half turn, quarter turn, three-quarter turn right angle straight line	north, south, east, west, N, S, E, W horizontal, vertical, diagonal movement slide roll turn stretch, bend whole turn, half turn, quarter turn, three-quarter turn angle ... is a greater/smaller angle than... right angle acute angle obtuse angle straight line	north, south, east, west, N, S, E, W north-east, north-west, south-east, south-west, NE, NW, SE, SW horizontal, vertical, diagonal translate, translation movement slide roll turn stretch, bend whole turn, half turn, quarter turn, three-quarter turn rotate, rotation angle ... is a greater/smaller angle than... degree right angle acute angle obtuse angle reflection straight line ruler, set square angle, measurer, compass	north, south, east, west, N, S, E, W north-east, north-west, south-east, south-west, NE, NW, SE, SW horizontal, vertical, diagonal translate, translation coordinate movement slide roll turn stretch, bend whole turn, half turn, quarter turn, three-quarter turn rotate, rotation angle ... is a greater/smaller angle than... degree right angle acute angle obtuse angle reflection straight line ruler, set square angle, measurer, compass, protractor	north, south, east, west, N, S, E, W north-east, north-west, south-east, south-west, NE, NW, SE, SW horizontal, vertical, diagonal translate, translation coordinate movement slide roll turn stretch, bend whole turn, half turn, quarter turn, three-quarter turn rotate, rotation angle ... is a greater/smaller angle than... degree right angle acute angle obtuse angle reflex angle reflection straight line ruler, set square angle, measurer, compass, protractor
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Statistics						
Foundation Stage	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
count, sort	count, sort, vote	count, tally, sort, vote	count, tally, sort, vote	count, tally, sort, vote	count, tally, sort, vote	count, tally, sort, vote
group, set	group, set	graph, block graph, pictogram	graph, block graph, pictogram	survey, questionnaire, data	survey, questionnaire, data, database	survey, questionnaire, data, database
list	list, table	represents	represents	graph, block graph, pictogram	graph, block graph, pictogram	graph, block graph, pictogram
		group, set	group, set	represents	represents	represents
		list, table	list, table, chart, bar chart, frequency table	group, set	group, set	group, set
		label, title	carroll diagram, venn diagram	list, table, chart, bar chart, frequency table	list, table, chart, bar chart, frequency table, bar line chart	list, table, chart, bar chart, frequency table, bar line chart
		most popular, most common	label, title, axis, axes	carroll diagram, venn diagram	carroll diagram, venn diagram	carroll diagram, venn diagram
		least popular, least common	diagram	label, title, axis, axes	line graph	line graph
			most popular, most common	diagram	label, title, axis, axes	pie chart
			least popular, least common	most popular, most common	diagram	label, title, axis, axes
				least popular, least common	most popular, most common	diagram
					least popular, least common	most popular, most common
					maximum/ minimum value	least popular, least common
					outcome	maximum/ minimum value
						outcome
						mean (mode, median, range as estimates for this)
						statistics, distribution